# **Original Research Article**

# ENERGETICS OF THE BASIC ALLOTROPES OF CARBON

## ABSTRACT

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An effort was made in this work to calculate the total ground state energy and electronic band structure of Fullerenes (C<sub>60</sub>), Graphite and Diamond using FHI-aims Density Functional Theory (DFT) code. The density functionals used are the local-density approximation (LDA) in the parameterization by Perdew and Wang 1992, Perdew and Zunger 1981, the generalized gradient functional PBE, and PBE+vdW approach as defined by Tkatchenko and Scheffler. The results obtained from the computations of the ground state energies of diamond, fullerenes and graphite were -2072.569 eV, - 1027.178 eV and -2070.938 eV respectively. These results agrees well when compared to the various exchange and correlation functionals used in this study. Similarly, the results obtained from the computations of the Kohn Sham electronic band gaps of graphite and diamond were 0.00072eV and 5.57611eV, respectively. These are also in agreement when compared to the experimental values of 0eV and 5.45eV. These band gaps are within reasonable overestimation errors of 0.0% and 1.43% respectively. However, fullerenes band gap of 8.21131eV is not in agreement with theoretical and experimental values of 1.83eV and 2.3eV, respectively. This is probably due to the Bucky-ball nature of Fullerenes as well as the lattice constants and physical settings used.

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Keywords: DFT, LDA, GGA, Band Gap, HOMO, LUMO and Total Ground state Energy.
 **1. INTRODUCTION**

Carbon is found naturally in the earth crust and in the atmosphere. It is abundant and forms a major part of our life. Carbon is a unique and versatile element. It exists in many forms with different structures and properties. It can also be synthesized to form new forms of materials [1]. Carbon is the basic building block of the following Carbon materials: graphite, diamond, fullerene, graphene, Carbon-fiber, Carbon nanotube, lonsdaleite, carbyne and buckydiamonds. Recently, new Carbon form called penta-graphene was discovered using Vienna Ab initio Simulation Package (VASP) [2]. Similarly, novamene [3] was also discovered and the stable equilibrium structure was computed using Quantum Espresso code. The ability of Carbon to exist in many forms with different structures and
 properties led researchers into a rigorous research on Carbon nanomaterial.

The principal allotropes of Carbon are graphite, diamond and Fullerenes. Diamond is associated with the sp<sup>3</sup> hybrid orbital, all four electrons are used to form a tetravalent sigma  $\sigma$  bond in a 3D structure. In each unit cell, diamond has eight Carbon atoms. The bond length is equidistant between the four Carbon atoms, thereby forming a strong covalent bond with bond angle of 109.5<sup>0</sup>. Diamond is the hardest known material, it is used in cutting, drilling and grinding. It is transparent in the visible range of the electromagnetic spectrum, making it a good candidate for jewelry. It has a high thermal conductivity (more than copper) and low thermal expansion [1 and 4]

Graphite has a flat layered (planar) structure. Each Carbon atom forms trivalent (sigma  $\sigma$ ) bond with three (sp<sup>2</sup> hybrid orbital) other Carbon atoms in a hexagonal shape. The layers are bonded to one another by weak Van-der-Waal forces. This allows the layers to slip over each other. The p<sub>z</sub> – orbitals electrons, do also interact: they form a  $\pi$ -mobile electron. Graphite is the most stable and most strongly covalently bonded Carbon allotrope (within the layer). It is soft, opaque, black, used in pencil, lubrication and in nuclear reactor moderator [1 and 4].

34 In recent time, a new Carbon allotrope was discovered by Curl, Kroto and Smalley at Rice University. 35 It is spherical (soccer ball) in shape. It resembles a geodesic dome constructed by an architect in 36 person of Richard Buckminster Fuller. Hence, it was named in his honour as buckminsterfullerene, 37 shortened as fullerenes (also called buckyballs). It has sixty (60) Carbon atoms arranged in both 38 pentagonal and hexagonal shape. For it to have a spherical shape, it must satisfy the pentagon rule i.e. it must have 12 pentagons and 20 hexagons. Basic Fullerene molecular formula is  $C_{60}$  [1 and 4]. 39 Unlike graphite and diamond, fullerene molecule has both sp<sup>3</sup> and sp<sup>2</sup> hybrid orbitals, i.e., It has both 40 41 sigma and pi bond. Fullerene is used as a high temperature superconductor when doped with K or 42 Rb, it is a possible lubricating aid and is also used in medicine [1 and 5].

Nowadays, Density Functional Theory (DFT) is one of the leading tools used in studying the electronic
structure, stability, synthesis, defects, semiconducting and superconducting properties of Carbon
materials. DFT is a special computational quantum mechanical first principle method of describing
and predicting the electronic structures and properties of atoms, molecules and solids. [19] *used DFT GAUSSIAN 3 software to* compute the ground state energies and stable structures of diamond,
graphite and fullerenes. [20] calculated the stable atomic structure of fullerenes using FHI-aims code.

They reported that the most stable structure crystallizes in fcc structure. This crystal structure was
 used in this study for fullerenes computations.

51 In this work, using FHI-aims DFT package [6] structural units of Carbon basic allotropes were 52 simulated.

#### 53 2. MATERIAL AND METHODS

54 First principles, or *ab initio* calculations represent the pinnacle of electronic structure calculations. 55 Starting with the fundamental constants and Schrodinger's equation as a postulate, these methods 56 proceed to describe the nature of atomistic systems to a degree that is almost irrefutable. The 57 methods applied in solving Schrodinger's equation break into two main types: Hartree-Fock (HF) 58 based methods and Density Functional Theory (DFT) methods. While both make approximations to 59 make calculations possible, they represent the best available methods for atomistic modeling. The 60 first task is to have a Linux based operating system (0S) (Ubuntu 16.04 version installed for this 61 research work) on a computer. FHI-aims (Fritz Haber Institute-ab initio molecular simulations) is not 62 supported on windows. Since FHI-aims is distributed in source code form, the next task is to compile 63 a powerful executable program. For this, the following mandatory prerequisites are needed [6]:

• A working FORTRAN compiler. A good example is Intel's ifort compiler.

A compiled version of the lapack library, and a library providing optimized basic linear algebra
subroutines (BLAS). Standard commercial libraries such as Intel's mkl provide both lapack and BLAS
support. Having an optimized BLAS library for a specific computer system is critical for the
performance of FHI-aims.

FHI-aims requires two input files — control.in and geometry.in—located in the same directory from where the FHI-aims binary is invoked. An output file contains the basic information and result of the calculation such as the total energy, atomic forces, etc. The geometry.in file contains all information concerning the atomic structure of the system. This includes the nuclear coordinates, which are specified by the keyword; atom, followed by Cartesian coordinates (in units of Å) and the descriptor of the species (chemical elements) [7].The control.in file contains all other physical and technical settings for accurate and efficient convergence of the computations. 76 The full algorithmic framework embodied in the FHI-aims computer program package is described in

77 [6]. The algorithms are based on numerically tabulated atom-centered orbitals (NAOs) to capture a

- 78 wide range of molecular and materials properties from quantum-mechanical first principles. FHI-aims
- 79 is a very important code because, an all-electron / full-potential treatment that is both computationally
- 80 efficient and accurate is achieved for periodic and cluster geometries on equal footing, including
- 81 relaxation and *ab initio* molecular dynamics. The primary production method for total energies and
- 82 gradients is density functional theory (LDA and GGA). Additional functionality includes quantum-
- 83 chemical approaches (Hartree-Fock, hybrid functionals, MP2) and self-energy-based methods (e.g.,
- 84 GW) for electronic spectroscopic properties. FHI-aims allows fully quantum-mechanical simulations
- 85 for systems up to thousands of atoms, and performs efficiently also on massively parallel platforms
- 86 with possibly thousands of CPUs [6].
- 87 However, choosing the central computational settings consistently for series of calculations greatly
- 88 enhances the accuracy of any resulting energy differences (error cancellation). In FHI-aims, the key
- 89 parameters regarding computational accuracy are actually sub-keywords of the species keyword of
- 90 control.in, controlling the basis set, all integration grids, and the accuracy of the Hartree potential.
- 91 These settings of course were not retyped from scratch for every single calculation; on the other
- 92 hand, they remained obvious, since these are the central handles to determine the accuracy and
- 93 efficiency of a given calculation.
- 94 FHI-aims therefore provides preconstructed default definitions for the important sub-keywords
- 95 associated with different species from Z=1-102 (H-Md). These can be found in the species\_defaults
- 96 subdirectory of the distribution, and are built for inclusion into a control.in file by simple copy-paste.
- 97 For all elements, FHI-aims offers three different levels of *species\_defaults*, however we used only two
- 98 of these levels of species\_defaults in this work:
- 99 *light* : Out-of-the-box settings for fast pre-relaxations, structure searches, etc. Actually, no obvious
- 100 geometry / convergence errors resulted from these settings, and are recommended for many
- 101 household tasks. For "final" results (meV-level converged energy differences between large molecular
- 102 structures etc.), any results from the light level should be verified with more accurate post-processing
- 103 calculations, e.g. *tight*.
- 104 *tight* : Regarding the integration grids, Hartree potential, and basis cutoff potentials, the settings
- 105 specified here are rather safe, intended to provide meV-level accurate energy differences also for

106 large structures. In the tight settings, the basis set level is set to tier 2 for the light elements 1-10, a

107 modified tier 1 for the slightly heavier AI, Si, P, S, CI (the first spdfgd radial functions are enabled by

108 default), and tier 1 for all other elements. This reflects the fact that, for heavy elements, tier 1 is

109 sufficient for tightly converged ground state properties in DFT-LDA/GGA, but for the light elements (H-

110 Ne), *tier* 2 is, e.g., required for meV-level converged energy differences. For convergence purposes,

- 111 the specification of the basis set itself (tier 1, tier 2, etc.) may still be decreased / increased as needed
- 112 <mark>[6].</mark>

## 113 2.1 COMPUTATIONAL DETAILS

Various computations were done for the pw\_lda, pz\_lda and pbe\_GGA XC functionals. The Gaussian occupation broadening width of 0.01eV was selected. The convergence criterion for the SCF of eigenvalues, total energy and density were set to 10<sup>-2</sup>eV, 10<sup>-5</sup>eV and 10<sup>-4</sup>eV, respectively. The structure geometry with a convergence minimum of 10<sup>-2</sup>eV was optimized, while for the unit cell geometry optimization we selected full unit cell relaxation option. The corresponding convergence criteria for the SCF of the energy derivatives was chosen to be 10<sup>-4</sup>eV.

Tier 1 basis functions of FHI-aims light species\_default basis set was used for the geometry optimization, however, tier 2 tight basis set was used for the post relaxation of the relaxed geometry. BFGS (Broyden, Fletcher, Goldfarb and Shanno) structure optimization algorithm was selected for the geometry relaxation. FHI-aims keyword k\_grid was set to 12x12x12 k\_grid data point. For the long range correlation energy interaction effect, we used VdW correction based on Tkatchenko and Scheffler long range interaction correction.

#### 126 3. RESULTS AND DISCUSSION

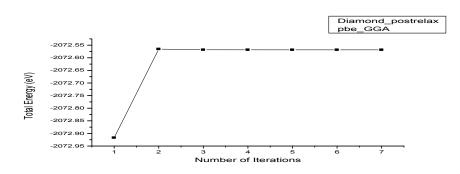
127 The following tables summarize the output data obtained during FHI-aims computations, and are used 128 in discussing the minimum and stable ground state energies for the relaxed/post relaxed 129 computations of the various XC functionals for the three bulk structures.

130 Table 4.1: Diamond Ground State Energies for Relaxed/Post Relaxed Computations.

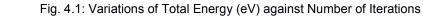
| Functionals  | Pw_lda       | Ground | Pz_lda Ground State | Pbe (GGA) Ground  |
|--------------|--------------|--------|---------------------|-------------------|
| Computations | State Energy | / (eV) | Energy (eV)         | State Energy (eV) |

| Relaxed Geometry     | -2056.94097548 | -2056.90780088 | -2072.47722687 |
|----------------------|----------------|----------------|----------------|
| (Light)              |                |                |                |
| Postrelaxed Geometry | -2057.03098622 | -2056.99760599 | -2072.56851605 |
| (Tight)              |                |                |                |

132 From table 4.1, it can be observe that pbe XC functional has the minimum ground state energy for 133 diamond bulk structure. This is in agreement with theory, because pbe (GGA) is theoretically a better 134 approximation to XC energy functional than the rest LDA and LSDA [8 and 9]. However, pw\_lda is a 135 bit better approximation when compared to pz\_lda. Similarly, comparing light and tight FHI-aims 136 species\_default settings for relaxed and postrelaxed computations, tight gives an efficient and 137 accurate converged ground state energies than the light settings. This is a good indication that 138 diamond crystalline structure has been well optimized in the relaxed/postrelaxed FHI-aims 139 computations. The following graphs summarize the output data obtained during FHI-aims 140 computations, and are used in obtaining the binding curve pattern for the total energy and the number 141 of iterations.



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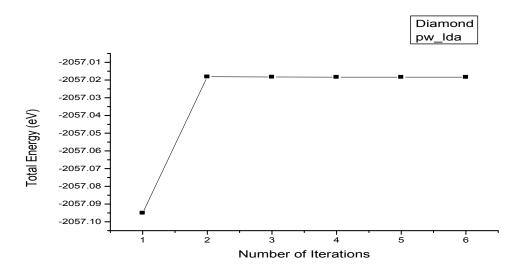
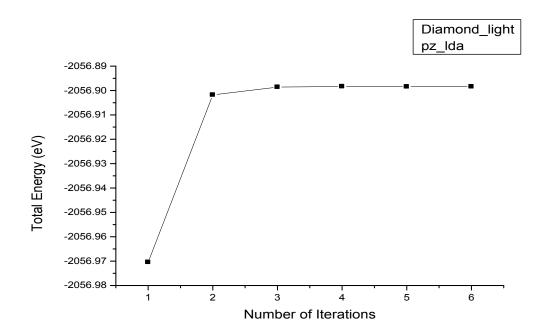




Fig. 4.2: Variations of Total Energy (eV) against Number of Iterations.





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Fig. 4.3: Variations of Total Energy (eV) against Number of Iterations.

The binding curve in Fig. 4.1 shows that the total energy of the bulk crystal of diamond increases as the number of iteration increases and converges steadily. The resulting binding curve indicates a stable total energy and also the best converged energy of -2072.56851605eV for diamond. This variation pattern for diamond total energy against the number of iterations was found to be the same for the remaining XC functionals used in this study. 154 Fig. 4.2 and Fig. 4.3 also illustrate the variations of diamond's ground state energies against the 155 number of iterations. It is clear that the graphs variations are almost the same, except that the total energies values are different. In Fig. 4.2 graph, the total energy value increases steadily from the 1st 156 iteration to the 2<sup>nd</sup> iteration, from where this value decreases a bit and is later maintained until 157 158 convergence is reached. However, fig. 4.3 shows a slight different trend. The total energy value rather 159 increases in the third iteration, this value was maintained until convergence was obtained. The 160 resulting binding curve in Fig. 4.3 indicates a stable total energy and also the best converged energy 161 of -2056.89840811eV for diamond.

162 Table 4.2: Graphite Ground State Energies for Relaxed/Post Relaxed Computations

| Functionals          | Pw_lda Ground     | Pz_Ida Ground State | Pbe (GGA) Ground  |
|----------------------|-------------------|---------------------|-------------------|
|                      | State Energy (eV) | Energy (eV)         | State Energy (eV) |
| Computations         |                   |                     |                   |
| Relaxed Geometry     | -2044.81236553    | -2044.81251118      | -2061.63381564    |
| (Light)              |                   |                     |                   |
| Postrelaxed Geometry | -2054.61937938    | -2054.63065901      | -2070.93836837    |
| (Tight)              |                   |                     |                   |

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From table 4.2, it can be observe that pbe XC functional also has the minimum ground state energy for graphite bulk structure. This is in agreement with theory, because pbe (GGA) is theoretically a better approximation to XC energy than the rest pw\_Ida and pz\_Ida [9]. However, pw\_Ida is slightly a better approximation when compared to pz\_Ida. Similarly, comparing light and tight species\_default settings for relaxed and postrelaxed computations, tight gives an efficient and accurate converged ground state energies than the light settings. This is also a good indication that graphite crystalline structure has been well optimized in the relaxed/postrelaxed FHI-aims computations.

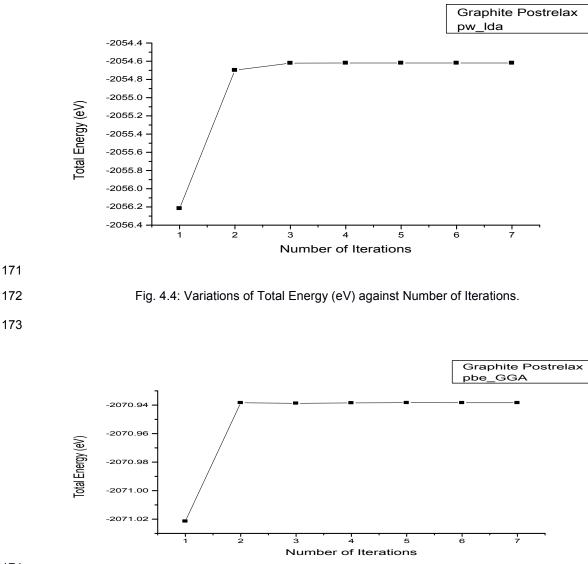




Fig. 4.5: Variations of Total Energy (eV) against Number of Iterations.

Fig. 4.4 and Fig. 4.5 illustrate the variations of ground state energies against number of iterations for graphite bulk structure. The trend in both Figures increases upwardly to create a curve pattern until it reaches stability at the 3<sup>rd</sup>, 4<sup>th</sup>, 5<sup>th</sup>, 6<sup>th</sup> and 7<sup>th</sup> iterations, this can be attributed to the covalent bonding and simple planar hexagonal stacking that exist in the bulk atom of graphite [10]. The resulting binding curve in Fig. 4.5 indicates a stable total energy and also the best converged energy of -2070.93836837 eV for graphite.

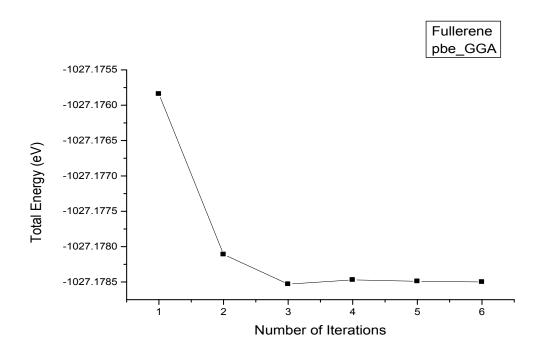
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184 Table 4.3: Fullerenes Ground State Energies for Light and Tight Settings.

| Functionals  | Pw_lda       | Ground | Pz_Ida Ground State | Pbe (GGA) Ground  |
|--------------|--------------|--------|---------------------|-------------------|
|              | State Energy | / (eV) | Energy (eV)         | State Energy (eV) |
| Computations |              |        |                     |                   |
| Light        | -1018.35981  | 067    | -1018.35683745      | -1027.17026568    |
| Tight        | -1018.36680  | 612    | -1018.36379535      | -1027.17849607    |

186 For Fullerenes, ground state energies for relaxed/postrelaxed computations were not successful, 187 because FHI-aims could not write out the geometry.in\_next\_step file let alone post relax processing. We suggest this could be due to the dimension of fullerenes lattice constant of 14.17A<sup>o</sup>, physical 188 189 settings used and/or its spherical shape However, we computed the ground state energies for 190 light/tight settings without structure optimization. Table 4.3 shows fullerenes ground state energies for 191 the three XC functionals using light/tight default settings. The table also shows that, tight default 192 settings gives a more accurate converged minimum ground state energy when compared to the light 193 default settings. This is in good agreement with the theory behind FHI-aims code [6]. Also looking at 194 the XC functional total energy values, it is obvious that pbe gives the minimum ground state energy 195 follow by pw\_lda and then pz\_lda. Hence, in accordance with theory pbe is much better in 196 approximating the XC energy functional than pw\_lda and pz\_lda [8 and 9].



198 Fig. 4.6: Variations of Total Energy (eV) against Number of Iterations.

Figure 4.6 illustrates the variations of Fullerenes ground state energies for the pbe XC functionals against number of iterations. The trend in Fig. 4.6 decreases downwardly to create a curve pattern until it becomes stable at the 4<sup>th</sup>, 5<sup>th</sup> and 6<sup>th</sup> iterations, this can be attributed to the covalent bonding and spherical shape that exist in the bulk atom of fullerenes [10 and 11].

In this paper, we find out that all the three variants of the total energy from FHI-aims output file are the same for diamond structure but are all different in the case of graphite and fullerenes. This shows that fullerenes and graphite have narrow and zero HOMO-LUMO gap respectively, while diamond has a wide HOMO-LUMO gap. These results are in good agreement with experimental and theoretical literatures [10 and 12]. Tables 4.4-4.6 show estimated values for lowest unoccupied state (CBM), highest occupied state (VBM), overall HOMO-LUMO gap and smallest direct gap for diamond, graphite and fullerenes as obtained from the three XC functionals used in this study.

| 210 | Table 4.4: Diamond Electronic Band Structure for Postrelaxed Computa | ations |
|-----|--|--------|
|-----|--|--------|

| Functionals         | ;    | Pw_lda       | Ground | Pz_lda Ground State | Pbe (GGA) Ground  |
|---------------------|------|--------------|--------|---------------------|-------------------|
|                     |      | State Energy | y (eV) | Energy (eV)         | State Energy (eV) |
| Bands               |      |              |        |                     |                   |
| Valence             | Band | -8.54310497  | ,      | -8.53387243         | -8.10988403       |
| Maxima (VBM)        |      |              |        |                     |                   |
| Conduction          | Band | -4.34300078  | }      | -4.34356041         | -3.95778618       |
| Minima (CBM)        |      |              |        |                     |                   |
| HOMO-LUMO Gap       |      | 4.20010419   |        | 4.19031201          | 4.15209785        |
| Smallest Direct Gap |      | 5.61457427   |        | 5.60711319          | 5.57611325        |

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From table 4.4, using the estimated overall HOMO-LUMO gap, FHI-aims code predicted that diamond appears to be an indirect band gap. This agrees well with the report of Pierson, 1993. The smallest direct gap of 5.57611325eV for pbe\_GGA is in good agreement with theoretical and experimental values [10 and 21] with an overestimation percentage error of 1.43%. According to FHI-aims output file, since the gap value is above 0.2eV, the system is most likely an insulator or a semiconductor. This FHI-aims output file comment agrees exactly with theoretical and experimental data. Diamond was characterized in many literatures to be an insulator [4], however, it was also considered as an

- 219 indirect wide band gab semiconductor [1] that is suitable for high temperature electronic applications.
- 220 The rest XC functionals pw\_lda and pz\_lda Smallest Direct Gap are also in good agreement with
- 221 experimental values of 5.5eV [10] with an overestimation error of 1.96%.
- 222 Table 4.5: Graphite Electronic Band Structure for Postrelaxed Computations

| Functionals         | Pw_lda Ground State | Pz_lda Ground State | Pbe (GGA) Ground  |
|---------------------|---------------------|---------------------|-------------------|
|                     | Energy (eV)         | Energy (eV)         | State Energy (eV) |
| Bands               |                     |                     |                   |
| Valence Band Maxima | -7.07415413         | -7.33934792         | -6.81313445       |
| (VBM)               |                     |                     |                   |
| Conduction Band     | -7.06569011         | -7.33861834         | -6.80852692       |
| Minima (CBM)        |                     |                     |                   |
| HOMO-LUMO Gap       | 0.00846402          | 0.00072958          | 0.00460753        |
| Smallest Direct Gap | 0.21308645          | 0.41541884          | 0.30724683        |
| ·                   |                     |                     |                   |

224 From table 4.5, using the estimated overall HOMO-LUMO gap, FHI-aims predicted that graphite also 225 appears to be an indirect band gap. The smallest direct gap of 0.21308645eV for pw\_lda is in good 226 agreement with theoretical [13] and experimental values [10]. According to FHI-aims output file, since 227 the HOMP-LUMO gap value (0.00072958eV) is rather small (approximately zero gap) and we use a 228 finite k-point grid, the material is most likely metallic in the sense that there are states at or near the 229 Fermi level. This FHI-aims output comment shows that graphite is a conductor, and it agrees exactly 230 with theoretical [13] and experimental data . Also, the approximately zero gap value of FHI-aims 231 output file is in agreement with the literature [10]. The rest XC functionals pz Ida and pbe GGA 232 Smallest Direct Gap are also in good agreement with experimental values within small overestimation 233 percentage errors.

234 Table 4.6: Fullerenes Electronic Band Structure for Tight Settings Computations

| Functionals     | Pw_lda Ground State | Pz_lda Ground State | Pbe (GGA) Ground  |
|-----------------|---------------------|---------------------|-------------------|
| Bands           | Energy (eV)         | Energy (eV)         | State Energy (eV) |
| Valence Band    | -13.60248641        | -13.60706560        | -13.71228408      |
| Maxima (VBM)    |                     |                     |                   |
| Conduction Band | -5.39117210         | -5.39539613         | -5.25904269       |

| Minima (CBM)        |            |            |            |
|---------------------|------------|------------|------------|
| HOMO-LUMO Gap       | 8.21131431 | 8.21166947 | 8.45324138 |
| Smallest Direct Gap | 8.21131432 | 8.21166948 | 8.45324139 |

236 From table 4.6, using the estimated overall HOMO-LUMO gap, FHI-aims predicted that fullerenes also 237 appears to be an indirect band gap. The smallest direct gap of 8.21131432eV for pw Ida and the 238 remaining XC functionals values do not agree with theoretical value of 1.83eV [12] and experimental 239 value of 2.3eV [Byun 2012, PhD Dissertation, Pennsylvania State University]. According to FHI-aims 240 output file, since the gap value is above 0.2 eV. The system is most likely an insulator or a 241 semiconductor. This FHI-aims output prediction agrees exactly with theoretical and experimental data, 242 fullerenes was reported to be a band insulator, direct band-gap semiconductor [1]. In addition, 243 fullerenes can be converted from a semiconductor into a conductor or even superconductor when 244 doped with alkali metals [14]. The rest XC functionals pz\_lda and pbe\_GGA Smallest Direct Gap are 245 also not in good agreement with theoretical [12] and experimental values.

246 It can be easily observed that all the electronic band gaps above are overestimated by certain

247 percentage errors. This is because generally, DFT overestimates the band gap energy of solids [8].

#### 248 **5. CONCLUSION**

249 The total ground state energy and electronic band structure of Fullerenes (C<sub>60</sub>) for University]. 250 According to FHI-aims output file, since the gap value is 2 eV. The system is most likely an insulator 251 or a semiconductor. This FHI-aims output prediction agrees exactly with theoretical and experimental 252 data, Fullerenes was reported to be a band insulator, direct band-gap semiconductor above 0. [1]. In 253 addition, fullerenes can be converted from a semiconductor into a conductor or even superconductor when doped with alkali metals [14]. FCC, Graphite for hcp and Diamond crystal were calculated using 254 255 the local-density approximation (LDA) in the parameterization by [15-17], and PBE+vdW approach as 256 defined by [18]. The results of the total energy required for binding/stability of the ground state during 257 the optimized process were found to converge faster with the 12x12x12 k-grid points in the Brillouin 258 zone of the FHI-aims code. Similarly, FHI-aims tight/postrelaxed settings were found to give more 259 accurate converged results. In terms of the XC functionals, pbe GGA was better in approximating the 260 XC energy functional than LDA. The result presented above have confirmed a faster and more 261 accurate prediction of the electronic band structure and total energies of solids considered when 262 compared to literature report of other studies reporting similar band gaps and/or total energies. Major findings of this research are; Graphite is a zero gap conductor (0.00072958eV), diamond is a wide band gap semiconductor (5.57611325eV). These are in good agreement with experimental values of 0eV and 5.45eV, respectively. However, fullerenes is also a wide band gap semiconductor (8.21131431eV). This band gap does not agree with what was obtainable in the literature (1.83eV and 2.3eV). This discrepancy might probably be due to the present DFT calculations of the solid fullerene's lattice constant, spherical shape and the optimized parameters used in the study.

270 is suitable for high temperature thermal electronic devices, while fullerenes is a good material for

Conversely, Graphite is a suitable candidate for optoelectronic and other electronic devices. Diamond

271 conversion into conductors and superconductors.

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