Magnetic properties of a quasi-two-dimensional Heisenberg antiferromagnet α-RbCrF₄

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ABSTRACT

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We synthesized a quasi-two-dimensional Heisenberg antiferromagnet on a square lattice formed in α -RbCrF₄ by improving the pretreatment method before primary sintering. From X-ray diffraction measurements, the crystal structure was found to consist of a TIAIF₄-type structure, which shows a good two-dimensionality. But the splitting of the fundamental peak indicating a superstructure in the *ab*-plane appeared. Temperature dependence of magnetic susceptibility shows a broad peak, which indicates typical low-dimensional antiferromagnets, at $T_{\text{max}} \approx 47 \text{ K}$. Furthermore, a sharp peak which indicates an antiferromagnetic phase transition also appeared at $T_{\text{N}} = 29.3(2)$ K. Following several previous theoretical investigations, we estimated intra-layer (J_{intra}) and inter-layer (J_{inter}) exchange interactions to be $J_{\text{intra}} / k_{\text{B}} = -6.6(1) \text{ K}$ and $J_{\text{inter}} / J_{\text{intra}} \approx 0.05$, respectively. As a result, we found that α -RbCrF₄ is a quasi-two-dimensional Heisenberg antiferromagnet.

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18 Keywords: Quasi-two-dimensional magnet, X-ray diffraction, magnetic susceptibility, α -19 RbCrF₄

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21 1. INTRODUCTION

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23 Recently, magnetoelectric multiferroic materials have received much attention because of 24 the possibility of either "magnetic control of ferroelectric domains" or "electric control of magnetic domains"[1,2,3]. In ferromagnetics and ferroelectrics, the switching from one 25 26 domain orientation to another occurs because of the application of external perturbation, 27 which changes the preferred, lowest energy orientation of the order parameter from one state to another. In addition to magnetic and electric fields, mechanical stress can have a 28 29 switching effect in ferroelastic materials. In addition to magnetic and electric fields, 30 mechanical stress can have a switching effect in ferroelastic materials. Using point groups of prototypic and ferroic phases, Aizu classified the cases where ferromagneticity, 31 32 ferroelectricity, and ferroelasticity coexist and completely couple with each other[4].

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Many investigations have been reported for successive structural phase transitions in $A^{I}M^{III}F_{4}$ compounds, where the $M^{III}F_{6}$ octahedra are centered in a square-based

36 parallelepiped of A^+ cations in the so-called TIAIF₄-type structure[5]. Figure 1 shows an aristotype $A^{I}M^{III}F_{4}$ structure. The corner-sharing $M^{III}F_{6}$ octahedra result in a square lattice 37 with each layer separated by A^{I} cations, leading to a good two-dimensionality in $A^{I}M^{III}F_{4}$ 38 39 compounds. For example, in non-magnetic compounds TIAIF₄ and RbAIF₄[6,7], internal strains were investigated and the switching of ferroelastic domains by uniaxial stress was 40 41 demonstrated, although a ferroelastic-ferroelectric effect can not be expected because of the 42 non-polar space group of these materials. Furthermore, in magnetic compounds with S =43 5/2. RbFeF₄ and CsFeF₄[8.9.10.11], an orthorhombic (mmm)-tetragonal (4/mmm) structural 44 phase transition causes spontaneous strain, and then, an antiferromagnetic phase transition 45 occurs far below the structural phase transition temperature. Temperature (7) dependence 46 of magnetic susceptibilities (χ) of RbFeF₄ and CsFeF₄ shows a typical two-dimensional 47 antiferromagnetic behavior. On the other hand, in magnetic compound with S = 1, 48 CsVF₄[12,13], a sharp $\chi(T)$ peak corresponding to an antiferromagnetic phase transition 49 appeared at a magnetic field (H) of 200 Oe, and the $\chi(T)$ curves for field cooling (FC) and 50 zero-field cooling (ZFC) overlapped. At $H \ge 5$ kOe, a ferromagnetic moment was induced by 51 the magnetic field and the splitting of $\chi(T)$ curves for the FC and ZFC appeared. Therefore, 52 we hope that mechanical stress can be used to switch the magnetic and/or ferroelectric domains in ferroelastic $A^{I}M^{III}F_{4}$ compounds. 53

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Previously, we have intensively studied a series of chromium fluorides, $A^{\rm I}{\rm Cr}_{\rm F_4}$ ($A^{\rm I}$ = K and 55 Cs), because of their highly frustrated magnetic structures such as triangular spin 56 tubes[14,15]. Table 1 presents the structural phase diagram of A^{1} CrF₄ (A^{1} = K, Rb, Cs), as 57 58 previously reported by Kozak[16]. In equilateral triangular spin tube CsCrF₄, no structural 59 isomer exists below the melting point. However, a structural isomer was observed in KCrF₄ and RbCrF₄ when the sintering temperature was varied. In KCrF₄, non-equilateral triangular 60 61 spin tube α -KCrF₄ was crystallized below 768 °C [15], whereas β -KCrF₄ consisting of the CsCrF₄-type structure was crystallized above 768 °C. In RbCrF₄, α -RbCrF₄ consisting of a 62 63 TIAIF₄-type structure was crystallized below 750 °C [17], whereas β -RbCrF₄, consisting of a CsCrF₄-type structure, is crystallized above 750 $^{\circ}$ C. The magnetic properties of RbCrF₄ 64 65 were studied without any distinction between the α - and β -phases[18,19].

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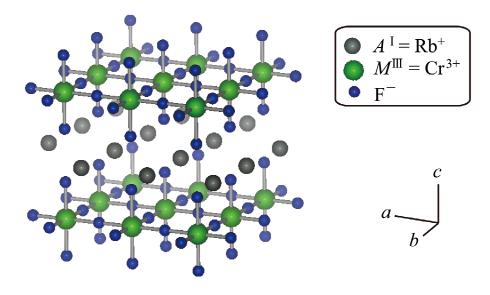
We have previously observed that the magnetic susceptibility of CsCrF₄ is strongly affected 67 68 by a small amount of paramagnetic impurities and/or imperfect crystallization[14,15]. A crystallization method that enables the synthesis of high-quality α -RbCrF₄ must be 69 70 developed to confirm the magnetic ground state. Figure 1 shows the aristotype structure of α -RbCrF₄, which we believe a quasi-two-dimensional Heisenberg antiferromagnet with S = 71 72 3/2. In this study, we obtained highly crystalline α -RbCrF₄ and performed X-ray diffraction 73 (XRD) and magnetic susceptibility measurements to confirm that high-guality samples were 74 prepared and to confirm the heretofore unreported structural and magnetic properties of α -75 RbCrF₄.

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77 Table 1: Structural phase diagram of $A^{1}CrF_{4}$ ($A^{I} = K$, Rb, and Cs) in Ref. 16.

	lpha - phase (low-T phase)	Critical Temperature (°C)	eta - phase (high- T phase)
KCrF ₄	non-equilateral triangular spin tube	768	CsCrF₄-type
RbCrF₄	square lattice (TIAIF ₄ -type)	750	CsCrF ₄ -type
$CsCrF_4$	equilateral triangular spin tube	No structural isomer below melting point.	

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Figure 1: Schematic of aristotype structure of $A^{I}M^{III}F_{4}$ compound. Each layer is stacked without translation in the *ab*-plane. In α -RbCrF₄, A^{I} and M^{III} correspond to Rb⁺ and Cr³⁺, respectively.

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84 2. SAMPLE PREPARATION

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86 We prepared polycrystalline samples of α -RbCrF₄ using a method similar to that employed 87 in the synthesis of high-quality CsCrF₄, i.e., using a conventional solid-state reaction method[15]. We mixed the RbF and CrF₃·4H₂O starting materials in accordance with the 88 stoichiometry and then heated them at 200 °C for more than 48 h under vacuum with 89 $P < 1 \times 10^{-3}$ Pa to dehydrate the crystals. Sintering was then performed at various 90 91 temperatures below 750 °C. The final sample color was dark green. To further purify the samples, we improved the pretreatment method before primary sintering, as discussed in the 92 93 next section.

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95 To examine the sample crystal structure and phase purity, we performed powder XRD measurements at room temperature. The XRD data were collected for $5^{\circ} < 2\theta < 70^{\circ}$ by a 96 Philips X'pert Pro MPD using the Bragg-Brentano geometry with Cu $K\alpha$ radiation. Because 97 98 the antiferromagnetic ground state in CsVF₄ was found to be broken by $H \ge 5 \text{ kOe}$ [12,13], a weaker magnetic field should be applied to α -RbCrF₄. The temperature dependence of χ 99 100 was measured using a superconducting quantum interference device magnetometer 101 (Quantum Design, MPMS-XL) from 2 K to 350 K. In this study, we defined the magnetic susceptibility as $\chi \equiv M/H$. The FC and ZFC data were collected after applying H = 10 Oe 102 103 and 1 kOe at T = 350 K and 2 K, respectively. Because the $\chi(T)$ curves for the FC and ZFC 104 data overlapped, the ZFC data were omitted in the following discussion.

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106 3. EXPERIMENTAL RESULTS AND DISCUSSION

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Figure 2(a) presents the sharp XRD peak profiles obtained after sintering at 640 °C. 108 According to the previous studies, the space group of α -RbCrF₄ is *P*mmn ($2a \times 2b \times c$), and 109 the lattice constants are 2a = 7.348 Å and c = 6.442 Å [16,17,20]. On the basis of the *P*mmn 110 111 $(2a \times 2b \times c)$ space group, we can denote the all fundamental peaks using the indices shown in Fig. 2(a). However, as observed in the inset of Fig. 2(a), the splitting of the fundamental 112 113 peak indicates the appearance of a superstructure beyond the wavelength difference 114 between Cu $K\alpha_1$ and Cu $K\alpha_2$. We believe that the basic crystal system is orthorhombic but the origin of additional XRD peaks is distorted square lattice caused by the tilting of CrF_{6} 115 116 octahedra rather than impurities. In $A^{I}M^{III}F_4$, the *P*mmn ($2a \times 2b \times c$) space group is 117 expected a ferroelastic state from Aizu's 4/mmm Fmmm notation.

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We determined the best sintering temperature to be 640 °C and then post-annealed the 119 120 samples at 500 °C under HF gas; we denote this as the usual method[15]. As shown in Fig. 2(b), we measured the T dependence of χ for α -RbCrF₄ at H = 10 Oe to prevent the 121 122 saturation of impurity-induced weak ferromagnetic moments at high magnetic fields. As observed in $\chi(T)$ data for the samples obtained by the usual method, an anomaly indicating 123 124 a weak ferromagnetic moment appeared at T'=15.0(5) K. As shown in Fig. 2(b), when we 125 crystallized several samples under the same conditions, the transition temperatures T' 126 remained unchanged; however, the values of χ at 2.0 K varied widely among different batches. We believe that this magnetic transition at T' is due to extrinsic properties, i.e., the 127 128 presence of some magnetic impurities and/or poor crystallization.

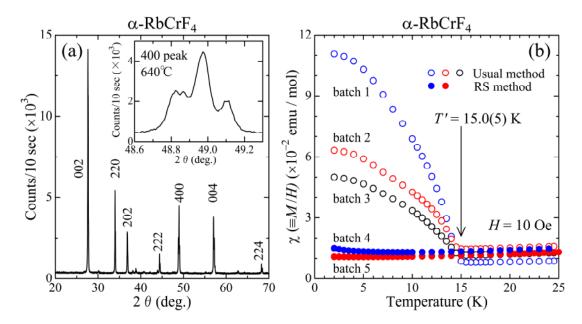
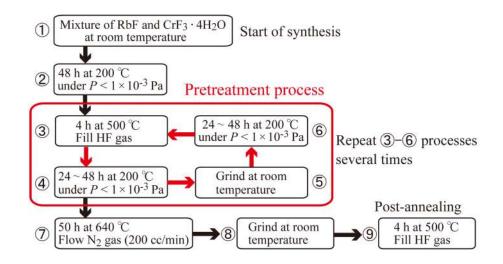


Figure 2: (a) X-ray diffraction pattern for α -RbCrF₄ after sintering at 640 °C. 130 Fundamental peaks are denoted by the indices on the basis of the *P*mmn ($2a \times 2b \times c$) 131 space group. As shown in the inset, the (400) peak splitting that indicates a 132 133 superstructure appeared beyond the wavelength difference between Cu $K\alpha$, and **Cu** $K\alpha_{n}$ (b) Low-temperature magnetic susceptibility [$\chi(T)$] for samples obtained 134 using the usual method in the three different batches (open circles) and the RS 135 136 method in the two batches (closed circles). The all datasets agree with one another 137 above T'=15.0(5) K. However, an anomaly indicating the weak ferromagnetic moment 138 appeared in the data for the samples obtained by the usual method, whereas no anomaly appeared in the data for the samples obtained by the RS method. 139

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141 To further purify polycrystalline α -RbCrF₄, we improved the pretreatment of the sample before primary sintering at 640 °C. Figure 3 presents the scheme of the improved 142 143 pretreatment, i.e., processes 3-6 were repeated several times before primary sintering. 144 Finally, the samples were heated at 640 $^\circ C$ for 50 h under N₂ gas flow (200 cc/min) and then post-annealed at 500 °C under HF gas. We will denominate the improved pretreatment 145 146 "the return to synthetic precursor method" (abbreviated as the RS method). As observed in Fig. 2(b), when we compare the data for the samples obtained using the RS method with 147 148 those obtained using the usual method, the $\chi(T)$ curves for both methods agree with each other above 15 K; however, no anomaly appeared below 15 K in the data for the samples 149 obtained by the RS method and its tendency showed high reproducibility. On the other hand, 150 151 the weak ferromagnetic moment at 2.0 K for the samples using the usual method showed a 152 large sample dependence. Therefore, we concluded that the impurity-induced weak 153 ferromagnetic moments appeared in the samples using the usual method. Regretfully, the 154 samples obtained by the two methods are indistinguishable based on the XRD data. In 155 future, we will refine the superstructure for α -RbCrF₄ by another experimental methods such as EXAFS or XANES experiment to obtain high-quality α -RbCrF₄ where the magnetic 156 157 phase transition at T' will be absent.



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160 Figure 3: Schematic of the improved pretreatment for α -RbCrF₄. Processes 3-6 were 161 repeated several times before primary sintering at 640 °C. We will denominate the 162 improved pretreatment "the return to synthetic precursor method" (abbreviated as the 163 RS method).

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165 Figure 4(a) shows the $\chi(T)$ curves at H = 1 kOe over the entire temperature range for the high-quality α -RbCrF₄. A broad $\chi(T)$ peak indicating a typical low-dimensional 166 antiferromagnetic behavior appeared at $T_{\rm max} \approx 47~{\rm K}$ [21]. As observed in the inset of Fig. 167 4(a), a sharp $\chi(T)$ peak appeared with the curvature similar to that of CsVF₄ at H = 200 168 Oe[12]. Therefore, we conclude that an antiferromagnetic phase transition occurs at T_N = 169 29.3(2) K in α -RbCrF₄. Figure 4(b) shows the 1/ χ (T) curve. We fitted the 1/ χ (T) data 170 above 250 K to the Curie-Weiss law [$\chi(T) = C/(T - \Theta_{cw})$ and $C = N_{A}g^{2}\mu_{B}J(J+1)/(3k_{B})$]; the 171 172 resulting Weiss temperature (Θ_{cw}) and effective magnetic moment were -67(3) K and 173 $3.98(3)\,\mu_{\rm B}$, respectively. The effective magnetic moment agrees with the spin-only value 174 $3.87(3) \mu_{\rm B}$ within the experimental error. Applying the molecular field theory to solve the 175 Hamiltonian given by

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$$H_{\text{cal}} = -2\sum_{\langle i,j \rangle} J_{i,j} S_i \cdot S_j , \quad (3.1)$$

177 the Weiss temperature is written as

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$$\Theta_{\rm CW} = \frac{2zJS(S+1)}{3k_{\rm B}},$$
 (3.2)

where *z* is the number of nearest neighbors and *J* is the isotropic exchange interaction, provided that this equation is valid for $T > |\Theta_{cw}|$. Applying $\Theta_{cw} = -67(3)$ K and z = 4, we estimated the intra-layer exchange interaction to be $J_{intra} / k_{B} = -6.7(3)$ K.

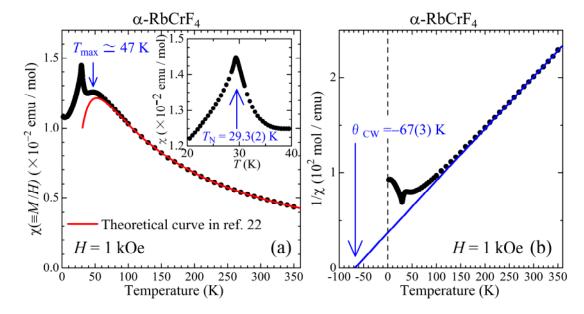




Figure 4: (a) Temperature dependence of the magnetic susceptibility (χ) for the highquality α -RbCrF₄. A broad $\chi(T)$ peak appeared at $T_{\text{max}} \approx 47$ K. The solid line is the best fit of the theoretical formula reported by Lines in Ref. 22, which yields $J_{\text{intra}} / k_{\text{B}} = -6.6$ K and $\chi_{\text{const}} = -9.4 \times 10^{-5}$ emu/mol. The inset shows a sharp peak for $\chi(T)$, indicating an antiferromagnetic phase transition at $T_{\text{N}} = 29.3(2)$ K. (b) Temperature dependence of $1/\chi(T)$. The solid line is the Curie-Weiss law; the resulting Weiss temperature is $\Theta_{\text{CW}} = -67(3)$ K.

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191 For a quadratic-layer Heisenberg antiferromagnet, the magnetic susceptibility reported by 192 Lines can be expressed in the high-temperature region [$\chi_{2D}(T)$] by a series expansion[22]. To subtract the T-independent term (χ_{const}), i.e., the diamagnetic contribution and Van Vleck 193 term, we attempted to use $[\chi_{2D}(T) + \chi_{const}]$ with the experimental data in the 200-350 K 194 temperature range far above $|\Theta_{cw}|$. For the best-fit curve shown in Fig. 4(a), the values of 195 $J_{_{intra}}$ and χ_{const} are determined to be -6.6(1) K and $-9.4(1) \times 10^{-5} \text{ emu/mol}$, respectively. 196 The values of J_{intra} obtained by the different analyses are in good agreement. Using the 197 198 relation between we further obtained J_{intra} and $T_{\rm max}$ $J_{intra}/k_{\rm B} = -T_{\rm max}/[1.12 \times S(S+1) + 0.10] = -5.5(2)$ K [22]. This value is smaller than the others. 199 The broad $\chi(T)$ peak in α -RbCrF₄ is necessary to re-consider not only the development of 200 an antiferromagnetic short-range order accompanied with the inter-layer exchange 201 interaction (J_{inter}) but also the existence of the inequivalent magnetic sites, i.e., the tilting of 202 CrF₆ octahedra in the opposite manner[20]. Based on the theoretical investigations of the 203

effect of J_{inter} by Ginsberg, $\chi_{2D}(T)$ must be modified at $T < |\Theta_{CW}|$, but the value of T_{max} is 204 almost invariant[23]. According to Yasudas' theoretical investigations of the relation between 205 206 J_{inter} and T_{N} in both quantum and classical two-dimensional antiferromagnets, we obtained $J_{\text{inter}}/J_{\text{inter}} \approx 0.05$ from Fig. 3 in Ref. 24, where we roughly estimated 207 $(k_{\rm B}T_{\rm N})/[2|J_{\rm intra}|S(S+1)] \approx 0.6$. Based on the magnetic susceptibility and neutron diffraction 208 experiments on CsVF₄, the magnetic ground state may change from the antiferromagnetic 209 state to some other state with ferromagnetic moments at a critical magnetic field (H_c) [12,13]. 210 211 In α -RbCrF₄, we re-expressed H_c at T = 0 K as $|g_1 - g_2| \mu_B H_C = 6 |J_{inter}|$, where g_1 and g_2 correspond to the g-value of each inequivalent magnetic site in antiferrodistortive CrF₆ 212 octahedra[12]. Because $|g_1 - g_2| \approx 0.01 - 0.05$ in Cr³⁺ compounds[25], we roughly estimated 213 the critical field as $H_{\rm C} \approx 2 \times 10^3 - 1 \times 10^4 |J_{inter}|/(g\mu_{\rm B})$. Consequently, we found that the $\chi(T)$ 214 data at H = 1 kOe shown in Fig. 4 indicate the presence of an intrinsic antiferromagnetic 215 216 ground state. Thus, the absence of the differences between the FC and ZFC $\chi(T)$ curves is 217 due to the absence of a ferromagnetic moment.

- 219 4. CONCLUSIONS
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We successfully synthesized high-quality α -RbCrF₄, a quasi-two-dimensional Heisenberg 221 222 antiferromagnet with S = 3/2 using the RS method, which is an improved pretreatment 223 method. The RS method can be applied to many powdered polycrystalline or monocrystalline fluorides before primary sintering. XRD experiments revealed that α -224 RbCrF₄ consists of a TIAIF₄-type structure, which shows a good two-dimensionality. The 225 splitting peak indicating the superstructure in the *ab*-plane appeared owing to the distorted 226 227 square lattice caused by the tilting of CrF₆ octahedra. Magnetic susceptibility experiments 228 did not find any extrinsic anomaly due to impurities at T = 15.0(5) K. The intrinsic $\chi(T)$ curve exhibited a broad $\chi(T)$ peak at $T_{\text{max}} \approx 47 \text{ K}$ and showed the occurrence of an 229 antiferromagnetic phase transition at $T_{\rm N}$ = 29.3(2) K. Using the $\chi(T)$ data in the high-T 230 region, we obtained $J_{intra} / k_B = -6.6(1) \text{ K}$ and $J_{intra} \approx 0.05$. As a result, the $\chi(T)$ data at 231 H = 1 kOe indicate the presence of an intrinsic antiferromagnetic ground state. If the degree 232 233 of the good two-dimensionality is increased, the antiferromagnetic ground state may change under low magnetic fields because of the competition between the Zeeman energy and $J_{\rm int}$. 234 We expect that the singular curvature of the $\chi(T)$ peak at $T_N = 29.3$ K is because of the 235 236 existence of inequivalent magnetic sites, i.e., the different tilting schemes of the F octahedra surrounding the Cr³⁺ ions at different sites. In future, the superstructure will be determined to 237 clarify whether ferromagneticity, ferroelectricity, and ferroelasticity coexist in this material. 238 Furthermore, the temperature dependence of the heat capacity under high magnetic fields 239 240 and high field magnetization process will be measured to confirm the magnetic-field-induced phase transition. 241

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251 COMPETING INTERESTS

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253 The authors declare that no competing interests exist.

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255 **AUTHORS' CONTRIBUTIONS**

All aspects of this work were carried out in close collaboration between both authors. Both authors read and approved the final manuscript.

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