1

2

Original Research Articles

Application of Gamma-Ray Attenuation in Studying Soil Properties

3

4 ABSTRACT

5 The total mass attenuation coefficients, effective atomic numbers and electron densities in some soil samples have been calculated for total and partial photon 6 interactions in the wide energy range of 1 keV–100 GeV. The values of these parameters 7 8 have been found to change with composition of soil and change in energy whereas their behavior has been found to be identical with all energies. The variations of these 9 parameters with energy are shown graphically for all photon interactions. WinXCOM 10 11 program was used to calculate theoretically soil mass attenuation coefficients. There is a satisfactory agreement between experimental and theoretical values. The reported data 12 should be useful for comparing these soil in terms of radiation sensitivity and radiation 13 detection. 14

Kew words: Soil; Mass attenuation coefficients; Effective atomic number; Effective electron number.

17 **INTRODUCTION**

Soils have many important functions. Perhaps the best appreciated is the function to support the growth of agricultural crops. The soil's natural cycles go a long way in ensuring that the soil can provide an adequate physical, chemical and biological medium for crop growth. Soil has very much attractive for future not only due to its potential applications in the field of agriculture but also in other applications in constructions, electronics and energy efficient savers. So, it is important to study all possible interactions between photons and atomic nuclei in the superconductor materials. The

25 mass attenuation coefficients, effective atomic number, effective electron density, are
26 basic quantities required to study all possible interactions, they depend on the incident
27 photon energy and the nature of the absorbing material.

In literature, a variety of work relevant to estimating of mass attenuation coefficients, effective atomic numbers for different compound materials has been published by several authors in different categories such as chemical compounds, alloys, glass, minerals, and biological materials and so on. The objective of this study is to calculate mass attenuation, effective atomic numbers and electron densities of some soil samples.

33 METHOD OF COMPUTATION AND THEORETICAL BASIS

When a material of thickness x is placed in the path of a beam of monoenergetic γ-ray
or X-ray radiations, the intensity of the beam will be attenuated according to the Beer–
Lambert's law,

$$I = I_0 e^{-\mu x}$$

(1)

where I₀ and I are the incident and attenuated photon intensity, respectively, and μ (cm⁻¹) is the linear attenuation coefficient of the material. Mass attenuation coefficient is a density-independent and more accurately characterizing a given material. Mathematical rearrangement of Eq. (1) yields the following equation for the mass attenuation coefficient (cm².g⁻¹):

43
$$\frac{\mu}{\rho} = \frac{1}{\rho x} ln \left(\frac{l_0}{l}\right)$$
(2)

44 where ρ (g.cm⁻³) is the measured density of the material. The total mass attenuation for a 45 material composed of multi elements is the sum of the $(\mu/\rho)_i$ values of each constituent 46 element by the following mixture rule:

47
$$\left(\frac{\mu}{\rho}\right) = \sum_{i} c_{i} \left(\frac{\mu}{\rho}\right)_{i}$$
(3)

48 where c_i and $(\mu/\rho)_i$ are the weight fraction and the mass attenuation coefficient of the *i*-th 49 component in the absorber, with the condition that: 50 $\sum_i c_i = 1$ (4) 51 For a chemical compound the weight fraction is given by:

52 53 $c_i = \frac{n_i A_i}{\sum_j n_j A_j}$ (5)

54 The average atomic cross-section σ_a can be obtained by dividing the molecular cross-

section by the total number of formula units as follows:

56
$$\sigma_a = \sigma_m \frac{1}{\sum_i n_i}$$
(2)

57 Similarly, the average electronic cross-section σ_e is given by

58
$$\sigma_e = \frac{1}{N_A} \sum_i \frac{f_i A_i}{Z_i} \left(\frac{\mu}{\rho}\right)_i$$
(3)

where $f_i = n_i / \sum_j n_j$ and Z_i are fractional abundance and atomic number of constituent element, respectively. n_j is the number of atoms of the constituent element, $\sum_j n_j = n$ is the total number of atoms present in the molecular formula. The effective atomic number, Z_{eff} can now be defined through the relation:

$$Z_{eff} = \frac{\sigma_a}{\sigma_e} \tag{4}$$

The effective electron number or electron density N_{el} (number of electrons per unit mass)
of the material can be derived from:

66
$$N_{el} = \frac{\left(\frac{\mu}{\rho}\right)}{\sigma_e} = \left(\frac{Z_{eff}}{M}\right) N_A \sum_i n_i$$
(5)

67 **RESULTS AND DISCUSSION**

Calculations of the mass attenuation coefficients of soil samples were carried out by
the WinXCOM program (Gerward et al., 2004). The software can generate cross-sections
and attenuation coefficients for elements, compounds or mixtures in the energy range
between 1 keV and 100 GeV.

The mass attenuation coefficients (μ/ρ), Z_{eff} and N_{el} of all soil samples were 72 calculated. The result of total mass attenuation coefficients of the studied 73 superconductors is shown in Fig.1. The variation of (μ/ρ) due to chemical composition is 74 energy dependent. In the low energy region, mass attenuation coefficients have the 75 highest values, where the photoelectric absorption is significant and its cross-section is 76 proportional to Z^4 . In the intermediate energy region, there is a linear Z-dependence of 77 incoherent scattering and the mass attenuation coefficient is found to be constant. In the 78 79 high energy region, mass attenuation coefficients increase again, where the pair production is significant and mass attenuation is proportional to Z^2 . 80

For total photon interaction process, the variations of Z_{eff} and N_{el} with photon energy 81 82 are shown in Figs. 2 and 3. In all materials, the interaction of gamma- or X-rays is related to Z_{eff} value of materials and the energy of photons. There is energy transfer from photon 83 84 to matter in these interactions. Although the dependence on the photon energy is dominant in interaction with low energies, it can be negligible at high energies. From Fig. 85 2, it is clear Z_{eff} increases in the investigated superconductors and then decreases up to 10 86 MeV. Above 100 MeV, Z_{eff} remains almost constant. This may be due to the dominance 87 of pair production in high energy region. The effective atomic numbers of almost all soil 88 higher due to the presence of some high Z constituent elements. 89

90 The behavior of Z_{eff} for total interaction reflects the importance of the partial photon interaction processes. At low-energy range (E < 0.01 MeV), the maximum value of Z_{eff} is 91 found. At intermediate energies (0.05 MeV < E < 5 MeV), where Compton scattering is 92 the main photon interaction process, Z_{eff} is approximately equal to the arithmetic mean of 93 the atomic number calculated from the chemical formula of the soil samples, $\langle Z \rangle =$ 94 $\frac{1}{n}\sum_{i} n_i Z_i$. At high energies, (E > 100 MeV), Z_{eff} is again constant but smaller than in the 95 low-energy range. This is due to the dominance of pair production and the cross-section 96 has Z^2 dependence. It is seen from Table 1, there is a good agreement in Compton 97 98 scattering region is the main photon interaction process.

The variations of N_{el} with photon energy for total interaction processes (Fig.3) are similar to that of Z_{eff} and can be explained on the similar manner. It can be seen that the value of N_{el} is were found to lie within range of 2.94–3.07×10²³ electron.g⁻¹ as shown in Table 2. This expected behavior for electron densities can be explained on the similar basis as for Z_{eff} . Calculated atomic and electronic cross section of the investigated soil is shown in Fig.4 and 5. Both of σ_a and σ_e are decreased sharply up to 10 MeV and then it is increased slightly with photon energy.

106

107 CONCLUSION

108 The present study has been undertaken to get some information on the mass 109 attenuation coefficients and related parameters, effective atomic numbers and electron 110 density for different types of soil samples. The results of this work can stimulate research 111 for other soil samples. In the interaction of photons with the matter, (μ/ρ) values are

112 dependent on the chemical compositions of the samples. The obtained values of (μ/ρ) are varied with photon energy regions (photoelectric absorption, Compton scattering and pair 113 production). The electron density and effective atomic number are closely related and 114 they are qualitative energy dependence. The dependence on the atomic number indicates 115 116 that soil having high Z_{eff} absorb powerfully incoming photons. The minimum value is found in the intermediate region, where Compton scattering is dominating and Z_{eff} is 117 approximately equal to the mean atomic number of the soil. The maximum value of Zeff 118 119 is found in the low energy range, where photoelectric absorption is dominating.

- 120 **REFERENCES**
- 121 1.Antoniassi, M., Conceição, A.L.C., Poletti, M.E., 2011. Study of effective atomic
 122 number of breast tissues determined using the elastic to inelastic scattering ratio.
 123 Nucl. Inst. and Meth. A 652, 739–743.
- 2.Baştuğ, A., İçelli, O., Gürol, A., Şahin, Y., 2011. Photon energy absorption
 parameters for composite mixtures with boron compounds. Ann. Nucl. Energy, 38,
 2283–2290
- 3.Baştuğ, A., Gürol, A., İçelli, O, Şahin, Y., 2010. Effective atomic numbers of some
 composite mixtures including borax. Ann. Nucl. Energy, 37, 927–933.
- 4.Batlas, H., Cevik, U., 2008. Determination of the effective atomic numbers and
 electron densities for YBaCuO superconductor in the range 59.5–136 keV. Nucl.
 Inst. and Meth. B 266, 1127-1131.
- 5.Gerward, L., Guilbert, N., Jensen, K.B., Levring, H., 2004. WinXCom-a program for
 calculating X-ray attenuation coefficients. Radiat. Phys. Chem. 71, 653–654.

134	6.Han, I., Aygun, M., Demir, L., Sahin, Y., 2012. Determination of effective atomic
135	numbers for 3d transition metal alloys with a new semi-empirical approach. Ann.
136	Nucl. Energy, 39, 56–61.
137	7. Icelli O, 2009. Measurement of effective atomic numbers of holmium doped and

- 7.Içelli O, 2009. Measurement of effective atomic numbers of holmium doped and
 undoped layered semiconductors via transmission method around the absorption
 edge, Nucl. Instr. Meth. Phys. Res. A, 600, 635–639
- 8.Kaewkhao, J., Limsuwan, P., 2010. Mass attenuation coefficients and effective
 atomic numbers in phosphate glass containing Bi2O3, PbO and BaO at 662 keV.
 Nucl. Instr. Meth. Phys. Res. A, 619, 295–297.
- 9.Limkitjaroenporn, P., Kaewkhao, J., Chewpraditkul, W., P. Limsuwan, P., 2012.
 Mass attenuation coefficient and effective atomic number of Ag/Cu/Zn alloy at
 different photon energy by Compton scattering technique. Procedia Engineering,
 32, 847–854.
- 147 10. Manohara, SR., Hanagodimath, S.M., Gerward, L., 2010. Energy absorption
 148 buildup factors for thermoluminescent dosimetric materials and their tissue
 149 equivalence. Radiat. Phys. Chem., 79, 575–582.
- 150 11. Manohara, SR., Hanagodimath, S.M., Thind, K.S., Gerward, L., 2008. On the
 151 effective atomic number and electron density: A comprehensive set of formulas for
 152 all types of materials and energies above 1 keV Instr. Meth. Phys. Res. B, 266,
 153 3906–3912.
- 154 12. Medhat M.E., 2012a. Study of the mass attenuation coefficients and effective
 155 atomic numbers in some gemstones. J. Radioanal Nucl. Chem., 293, 555–564.

156	13. Medhat, M.E., 2012b. Gamma absorption technique in elemental analysis of						
157	composite materials, Ann Nucl Energy, 47, 204–209.						
158	14. Medhat, M.E., 2012c. Application of gamma-ray transmission method for						
159	investigation of the properties of cultivated soil. Ann Nucl Energy, 40, 53-59.						
160	15. Medhat M.E., 2011. Studies on effective atomic numbers and electron densities in						
161	different solid state track detectors in the energy range 1 keV-100 GeV. Ann Nucl						
162	Energy, 38, 1252–1263.						
163	16. Polat, R., Yalçın, Z., İçelli, O., 2011. The absorption jump factor of effective						
164	atomic number and electronic density for some barium compounds, Nucl. Instru						
165	Meth. Phys. Res. A., 629, 185–191.						
166							
167	Table 1. Effective atomic number (Z_{eff}) of investigated soils at different energy (MeV) for total						

168

photon interaction.

Energy	Soil 1	Soil 2	Soil 3	Soil 4	Soil 5
$\frac{(1016 \text{ v})}{10^{-3}}$	11.20	10.57	9.96	10.49	10.59
10 ⁻²	10.67	10.11	9.49	10.06	10.11
10^{-1}	11.15	10.43	9.85	10.32	10.45
10^{0}	11.38	10.50	10.18	10.39	10.54
10^{1}	11.28	10.47	10.07	10.36	10.50
10^{2}	11.14	10.14	9.94	10.31	10.44
10^{3}	11.14	10.40	9.93	10.30	10.34
10^{4}	11.13	10.40	9.93	10.30	10.34
10 ⁵	11.13	10.40	9.93	10.30	10.34

169

170 Table 2. Effective electron number ($N_e \times 10^{23}$ electrons/g)) of investigated soil at different

171

energy (MeV) for total photon interaction.

Energy	Soil 1	Soil 2	Soil 3	Soil 4	Soil 5

(MeV)					
10-3	2.94	3.08	2.94	3.09	3.07
10^{-2}	2.80	2.94	2.80	2.97	2.93
10^{-1}	2.93	3.03	2.91	3.04	3.03
10^{0}	2.99	3.06	3.00	3.06	3.05
10^{1}	2.96	3.05	2.97	3.05	3.04
10^{2}	2.92	3.03	2.93	3.04	3.02
10^{3}	2.92	3.03	2.93	3.04	3.02
10^{4}	2.92	3.03	2.93	3.04	3.02
10 ⁵	2.92	3.03	2.93	3.04	3.02





Fig. 1.Variation of photon mass attenuation coefficient of some soil samples with photonenergy for total photon interaction.

180



181 Fig. 2.Variation of Z_{eff} with photon energy of the soil samples for total photon interaction.



183 Fig. 3.Variation of N_{el} with photon energy of the soil samples for total photon interaction











Fig. 5. Variation of atomic cross sections σ_e (b/atom) with photon energy. 199