1 <u>Original research paper</u> 2 RIEMANNIAN ACCELERATION IN CARTESIAN 3 COORDINATE BASED UPON THE GOLDEN 4 METRIC TENSOR

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8 ABSTRACT

Geometric quantities in all orthogonal curvilinear co-ordinates are built upon Euclidean geometry .This geometry is founded on a well known metric tensor called the Euclidean metric tensor. Riemannian geometry which is assumed to be more general than the Euclidean geometry was founded on an unknown metric tensor for spacetimes in gravitational fields. Therefore the Riemannian geometry itself could not be opened up for exploration and exploitation, let alone the possible application to theoretical physics. But with the discovery of a general Riemannian metric tensor called the golden metric tensor, exploitation of Riemannian geometry is now possible. we are in a position to calculate all the theoretical predictions of Riemanni's geometrical and physical concepts and principles and compare them with experimental physical evidence. In this paper, we use the golden metric tensor to develop Riemannian acceleration in the Cartesian coordinate for application in theoretical physics and other related fields.

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Keywords: Riemannaian geometry, golden metric tensor, Riemannain acceleration,
 Cartesian coordinate

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14 **1. INTRODUCTION**

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Right from 1854, when the German mathematician, George Riemann published his 16 geometry for spacetime known as Riemann geometry, it was assumed to be more general 17 18 than the Euclidean geometry. It is generally accepted that Riemannian geometry has the 19 potential of providing a more general foundation for theoretical physics [1]. However, the 20 problem with the Riemannian geomentry is that it was not founded on a known metric tensor 21 therefore its exploitation and possible applications to theoretical physics eluded the world. 22 Riemann during his own time (1816-1866) could not find the metric tensor(s) implicit in his 23 geometry. Riemann therefore left behind the problem of finding the metric tensors for all 24 gravitational field. Einstein tried to solve this problem in his contribution to classical 25 mechanics: Einstein's Geometrical Gravitational Field Equations [1]. It has since been believed that Einstein's Geometrical Gravitational Field Equations could lead to the 26 construction of the metric tensors for all gravitational fields in nature. In 1916, Karl 27 Schwarzschild introduced a metric tensor for all the gravitational field due to static 28 homogeneous spherical distribution of mass. This metric tensor was called Schwarzschild's 29 metric tensor. This metric tensor has been the basis for the development of Einstein's 30 Geometrical Theory of classical mechanics in the Gravitational field known as General 31 32 Relativity. In spite of the great fame since 1915, Einstein's Geometrical Gravitational Field 33 Equations cannot be applied to generate any natural metric tensor for the gravitational fields 34 due to any distribution of mass in nature. These equations have to be abandoned and 35 confined to archives of history in the search for metric tensors for the gravitational fields in 36 nature.

37 It is interesting to know that a metric tensor called the golden metric tensor for all gravitational fields in nature has been developed [1]. This metric tensor is valid for all four 38 39 co-ordinates of spacetime and in all the regular geometries in nature and for all regular distributions of mass. In the limit of $\mathcal{C}^{\mathbb{P}}$, it reduces to the well known Euclidean metric tensor 40 for all spacetimes in gravitational fields in nature, in perfect agreement with the principle of 41 42 equivalence of mathematics and the principle of equivalence of physics. We are in a position to calculate all the theoretical predictions of Riemann's geometrical and physical concepts 43 44 and principles and compare them with experimental physical evidence. In this paper, we use 45 the golden metric tensor to develop Riemannian acceleration in the coordinate for application in theoretical physics and other related fields 46

48 2. THEORY

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50 The spherical polar coordinate $(r_{,,}\varphi, x^{0})$ are defined in terms of the Cartesian coordinates 51 (x, y, z, x^{0}) by [2, 3]

$$52 \quad x = rsin\theta cos\varphi \tag{1}$$

$$53 \quad y = rsin\theta sin\varphi \tag{2}$$

$$\begin{array}{ccc} 54 & z = r \cos \varphi \\ 55 & \text{Where} \end{array} \tag{3}$$

56
$$r = (x^2 + y^2 + z^2)^{\frac{4}{2}}$$
 (4)

$$\theta = \cos^{-1} \left\{ \frac{1}{(x^2 + y^2 + z^2)^{\frac{1}{2}}} \right\}$$
57
$$(5)$$

$$\varphi = \tan^{-1} \left(\frac{2}{x}\right)$$
(6)
The Golden Metrix tensor for all gravitational fields in nature is given in the spherical polar

The Golden Metrix tensor for all gravitational fields in nature is given in the spherical polar coordinates $(r_{,,}, \varphi, x^{0})$ as [3]

$$g_{11} = \left(1 + \frac{2}{c^2}f\right)^{-1} \tag{7}$$

$$\begin{array}{l} 62 \qquad g_{22} = r^2 \left(1 + \frac{2}{c^2}f\right) \\ a = r^2 \sin^2 \theta \left(1 + \frac{2}{c}f\right)^{-1} \end{array} \tag{8}$$

$$\begin{array}{l} 65 \quad \boldsymbol{g}_{\mu\nu} = \mathbf{U}; \quad otherwise \qquad (11) \\ 66 \quad \text{Now we have to transform this matrix tensor into the cartesian coordinate system using the second second$$

66 Now we have to transform this metric tensor into the cartesian coordinate system using the 67 well known transformation relation in the theory of vector and tensor analysis given as [3];

$$\overline{g}_{qs} = \frac{\partial x^{q}}{\partial x^{q}} \frac{\partial x^{s}}{\partial x^{s}} g_{qs}$$
(12)

Applying the transformation relation given by (12), the metric tensor for all gravitational fields in the Cartesian coordinates are

$$g_{11} = \left(1 + \frac{2}{c^2}f\right)^{-1}$$
(13)
$$g_{22} = \left(1 + \frac{2}{c^2}f\right)^{-1}$$

$$72 \quad g_{22} = \left(1 + \frac{1}{c^2}\right) \tag{14}$$

$$g_{33} = \left(1 + \frac{2}{c^2}f\right)^{-1}$$
(15)

$$g_{00} = -\left(1 + \frac{2}{C^2}f\right)$$
(16)

$$g_{\mu\nu} = 0; \text{ otherwise}$$
(17)
Therefore, the contravariant tanger of the matrix tanger is given as:

$$-11 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}^2 = \begin{pmatrix} 2 \\ 1 \end{pmatrix}$$

77
$$g' = (1 + \frac{2}{c^2}f)$$
 (18)
70 $g^{22} = (1 + \frac{2}{c^2}f)$ (18)

$$g^{33} = \left(1 + \frac{2}{c^2}f\right)$$
(19)

$$g^{00} = -\left(1 + \frac{2}{c^2}f\right)^{-1}$$
(21)

$$g_{\mu\nu} = 0; otherwise$$

Also from our knowledge of vector and tensor analysis, the Riemannain linear velocity is
 given by

$$84 \qquad (U_R)_{x^0} = (g_{00})^{\frac{1}{2}} \dot{x}^0 \tag{22}$$

85
$$(U_R)_x = (g_{11})^{\frac{1}{2}\dot{x}}$$
 (23)

$$\begin{array}{c} (U_R)_y = (g_{22})^{\overline{2}} \dot{y}^2 \\ g_7 \\ (24) \end{array}$$

$$(U_R)_s = (g_{33})^{\frac{1}{2}} \dot{z}^3$$

$$And explicitly, taking x^0 = ct we can express this velocity as$$

$$(25)$$

And explicitly, taking x^* = ct we can express this velocity as

$$90 \qquad (U_R)_{x^0} = -c \left(1 + \frac{2}{c^2} f\right)^{\frac{1}{2}} t$$
(26)

91
$$(U_R)_x = (1 + \frac{1}{c^2}f)^{-1}x$$
 (27)

92
$$(U_R)_y = \left(1 + \frac{1}{c^2}f\right)^{-\frac{1}{2}} y$$
 (28)

93
94
$$(U_R)_z = \left(1 + \frac{1}{c^2}f\right)^{-2}\dot{z}$$
 (29)

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100 2.1 THE GOLDEN RIEMANNIAN LINEAR ACCELERATION TENSOR.

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103 We want to recall the definition of the linear acceleration tensor for all gravitational fields in 104 nature and show how to express them in terms of the Golden metric tensor in the Cartesian 105 coordinate. According to the theory of tensor analysis the linear acceleration tensor in 4-106 dimensional spacetime, a_{R}^{μ} , is given in all gravitational fields and all orthogonal curvilinear 107 coordinates x^{μ} by

all

$$\begin{array}{l} 142 \\ 143 \\ 143 \end{array} = -\frac{1}{c^2} \left(1 + \frac{2}{c^2} f \right)^{-2} f, 0 \\ \Gamma_{00}^1 = \frac{1}{c} g^{11} \left(g_{01,0} + g_{10,0} - g_{00,1} \right) \end{array}$$
(45) (46)

$$\begin{aligned} &= -\frac{1}{2}g^{11}g_{00,1} \\ &= \frac{1}{c^2}\left(1 + \frac{2}{c^2}f\right)f, 1 \end{aligned}$$
(47)

$$\Gamma_{11}^{1} = \frac{1}{2}g^{11}(g_{11,1} + g_{11,1} - g_{11,1})$$

$$= -\frac{1}{2}g^{11}g_{11,1}$$

$$= -\frac{1}{c^2} \left(1 + \frac{2}{c^2} f \right)^{-1} f_{,1}$$

$$= -\frac{1}{c^2} \left(1 + \frac{2}{c^2} f \right)^{-1} f_{,1}$$

$$(48)$$

$$= -\frac{1}{c^2} \left(1 + \frac{2}{c^2} f \right)^{-1} f_{,1}$$

$$(48)$$

$$\begin{array}{c} 149 \\ 150 \end{array} = \frac{1}{2}g^{11}g_{11,2} \\ 160 \end{array}$$

$$151 = -\frac{1}{a^2} \left(1 + \frac{2}{a^2} f \right)^{-1} f, 2$$

$$\Gamma_{12}^{1} = \frac{1}{a} a^{11} \left(a_{122} + a_{123} - a_{123} \right)$$
(50)

$$\begin{array}{c} 152 \\ 153 \end{array} = \frac{1}{2} g^{11} g_{11,3} \\ \frac{1}{2} (1 + \frac{2}{3} - 2)^{-1} c c \end{array}$$

$$\begin{array}{l} 154 \\ 155 \end{array} = -\frac{1}{c^2} \left(1 + \frac{1}{c^2} f \right) \quad f, 3 \\ \Gamma_{10}^1 = \frac{1}{c} g^{11} \left(g_{11,0} + g_{10,1} - g_{10,1} \right) \end{array}$$
(51) (52)

$$\frac{1}{156} = \frac{1}{2}g^{11}g_{11,0}$$
(52)

$$\begin{aligned} &= -\frac{1}{c^2} \left(1 + \frac{2}{c^2} f \right)^{-1} f, 0 \end{aligned} (53) \\ &158 \qquad \Gamma_{22}^1 = \frac{1}{c} g^{11} \left(g_{12,2} + g_{12,2} - g_{22,2} \right) \end{aligned} (54)$$

$$\begin{array}{l} = -\frac{1}{2}g^{11}g_{22,1} \\ = \frac{1}{c^2}\left(1 + \frac{2}{c^2}f\right)^{-1}f,1 \end{array}$$
(55)

$$\Gamma_{33}^{i} = \frac{1}{2} g^{11} (g_{13,3} + g_{13,3} - g_{33,1})$$

$$= -\frac{1}{2} e^{11} e^$$

$$\begin{array}{rcl}
 & = -\frac{1}{2}g^{11}g_{33,1} \\
 & = \frac{1}{c^2}\left(1 + \frac{2}{c^2}f\right)^{-1}f, 1 \\
 & = \frac{1}{c^2}\left(1 + \frac{2}{c^2}f\right)^{-1}f, 1
\end{array}$$
(57)

$$\Gamma_{00}^{1} = \frac{1}{2}g^{22}(g_{20,0} + g_{20,0} - g_{00,2})$$

$$= -\frac{1}{2}g^{22}g_{00,2}$$
(58)

$$\frac{166}{167} = \frac{1}{c^2} \left(1 + \frac{2}{c^2} f \right) f, 2$$

$$\frac{1}{c^2} \left(1 + \frac{2}{c^2} f \right) f, 2$$

$$\frac{1}{c^2} \left(1 + \frac{2}{c^2} f \right) f, 2$$

$$(59)$$

$$\begin{array}{ccc} 168 & 11 & -29 & (321,2 + 321,2 - 911,2) \\ 169 & = -\frac{1}{2}g^{22}g_{11,2} \end{array} \tag{60}$$

$$\frac{1}{170} = \frac{1}{c^2} \left(1 + \frac{2}{c^2} f \right)^{-1} f, 2$$
(61)

$$\begin{array}{rcl}
=& \frac{1}{2}g^{32}g_{32,1} \\
_{201} &= -\frac{1}{c^2}\left(1 + \frac{z}{c^2}f\right)^{-1}f, 1 \\
\end{array} \tag{81}$$

$$\Gamma_{30}^{3} = \frac{1}{2} g^{33} (g_{33,0} + g_{30,3} - g_{30,3})$$

$$= \frac{1}{2} g^{33} g_{33,0}$$
(81)

$$203 - 2^{g} y_{33,0} = -\frac{1}{c^2} \left(1 + \frac{2}{c^2} f\right)^{-1} f, 0$$

$$(82)$$

$$205 \quad I_{02} = \frac{1}{2} g^{22} (g_{20,2} + g_{22,0} - g_{02,2})$$

$$= \frac{1}{2} g^{22} g_{22,0}$$
(83)

$$206 = \frac{1}{2}g^{-1}g_{22,0}$$

$$= -\frac{1}{c^2}\left(1 + \frac{2}{c^2}f\right)^{-1}f, 0$$
(84)
208

Hence, applying (32)-(84) in (31) we obtain the golden Riemannain acceleration vector in the
Cartesian coordinate as
$$a_{R}^{0} = \vec{x}^{0} + \Gamma_{\alpha\beta}^{0} \vec{x}^{\alpha} \vec{x}^{\beta}$$

(85)

$$\begin{array}{rcl}
211 & a_{R}^{0} = \ddot{x}^{0} + \Gamma_{\alpha\beta}^{0} \dot{x}^{\alpha} \dot{x}^{\beta} \\
212 & (85) \\
213 & = \ddot{x}^{0} + \frac{1}{c^{2}} \left(1 + \frac{2}{c^{2}} f \right)^{-1} f_{,0} (\dot{x}^{0})^{2} \\
+ \frac{2}{c^{2}} \left(1 + \frac{2}{c^{2}} f \right)^{-1} f_{,1} \dot{x}^{0} \dot{x} \\
215 & + \frac{2}{c^{2}} \left(1 + \frac{2}{c^{2}} f \right)^{-1} f_{,2} \dot{x}^{0} \dot{y} \\
216 & + \frac{2}{c^{2}} \left(1 + \frac{2}{c^{2}} f \right)^{-1} f_{,2} \dot{x}^{0} \dot{z} \\
217 & - \left(1 + \frac{2}{c^{2}} f \right)^{-3} f_{,0} (\dot{x})^{2} \\
\end{array}$$

218
219

$$-\left(1+\frac{2}{c^2}f\right)^{-2}f_{,0}(y)^2$$

$$-\left(1+\frac{2}{c^2}f\right)^{-2}f_{,0}(z)^2$$

(86)

221
$$a_{R}^{1} = \ddot{x}^{1} + \Gamma_{\alpha\beta}^{1} \dot{x}^{\alpha} \dot{x}^{\beta}$$

222 $= \ddot{x} + \frac{1}{c^{2}} \left(1 + \frac{2}{c^{2}} f \right) f_{,1} (\dot{x}^{0})^{2}$
223 $- \frac{2}{c^{2}} \left(1 + \frac{2}{c^{2}} f \right)^{-1} f_{,0} \dot{x}^{0} \dot{x}$
224 $- \frac{2}{c^{2}} \left(1 + \frac{2}{c^{2}} f \right)^{-1} f_{,1} (\dot{x})^{2}$

225
$$-\frac{2}{c^2}\left(1+\frac{2}{c^2}f\right)^{-1}f_{,2}\dot{x}\dot{y}$$
$$-\frac{2}{c^2}\left(1+\frac{2}{c^2}f\right)^{-1}f_{,2}\dot{x}\ddot{z}$$

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228
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$$-\frac{1}{c^2} \left(1 + \frac{2}{c^2} f\right)^{-1} f_{,1}(\psi)^2$$

$$-\frac{1}{c^2} \left(1 + \frac{2}{c^2} f\right)^{-1} f_{,1}(z)^2$$

(87)

 $\begin{aligned} \alpha_R^2 &= \dot{x}^2 + \Gamma_{\alpha\beta}^2 \dot{x}^{\alpha} \dot{x}^{\beta} \\ &= \dot{y} + \frac{1}{c^2} \left(1 + \frac{2}{c^2} f \right) f_{,2} (\dot{x}^0)^2 \end{aligned}$ 230 231 $+\frac{1}{c^2}\left(1+\frac{2}{c^2}f\right)^{-1}f_{i^2}(x)^2$ 232 $-\frac{2}{c^2}\left(1+\frac{2}{c^2}f\right)$ f_{.1}żý 233 $\left(1+\frac{2}{c^2}f\right)$ faýż 234 $\frac{1}{c^2}\left(1+\frac{2}{c^2}f\right)$ $f_{,2}(\mathbf{y})^2$ 235 $+\frac{1}{a^2}\left(1+\frac{2}{a^2}f\right)^{-1}f_{,2}(z)^2$ 236 (88)237 $a_R^3 = \ddot{x}^3 + \Gamma_{\alpha\beta}^3 \dot{x}^\alpha \dot{x}^\beta$ 238 $= \ddot{z} + \frac{1}{c^2} \left(1 + \frac{2}{c^2} f \right) f_{,2}(\dot{x}^0)^2$ 239 $+\frac{1}{c^2}\left(1+\frac{2}{c^2}f\right)^{-1}f_{2}(x)^2$ 240 $+\frac{1}{c^{2}}\left(1+\frac{2}{c^{2}}f\right)^{2}$ $-\frac{1}{c^{2}}\left(1+\frac{2}{c^{2}}f\right)^{2}$ $f_{\beta}(\dot{y})^2$ 241 $f_{z}(z)^{2}$ 242 $-\frac{2}{c^2}\left(1+\frac{2}{c^2}f\right)$ f,zýż 243 $-\frac{2}{c^2} \left(1 + \frac{2}{c^2} f\right)^{-1} f_{c1} \dot{x} \dot{z}$ 244 $-\frac{2}{c^2}\left(1+\frac{2}{c^2}f\right)^{-1}f_0\dot{x}^0\dot{z}$ 245 (89)246 247 248 2.2 THE GOLDEN RIEMANNIAN LINEAR ACCELERATION VECTOR 249 250 251 The golden Riemannian linear acceleration tensor have corresponding Riemannian linear 252 acceleration vector given as $(a_{z})_{x} = (g_{11})^{\frac{1}{2}} a_{z}^{1}$ 253 (90) $(a_R)_{\gamma} = (g_{22})^{\frac{1}{2}} a_R^2$ 254 (91) $(a_g)_g = (g_{33})^{\frac{1}{2}} a_g^3$ 255 (92) $(a_R)_{x^0} = (g_{00})^{\frac{1}{2}} a_R^0$ 256 (93) Given $x^0 = ct$ we express the golden Riemannian acceleration vector as follows; 257 258 $(a_R)_{\mathcal{R}} = \ddot{x} \left(1 + \frac{2}{c^2}f\right)^{-\frac{1}{2}} + \left(1 + \frac{2}{c^2}f\right)^{\frac{1}{2}} f_{-1}(t)^2$ 259 $-\frac{2}{c}\left(1+\frac{2}{c^2}f\right)^{-\frac{2}{2}}f_{,0}xt$ 260 $-\frac{1}{c^2}\left(1+\frac{2}{c^2}f\right)^{-\frac{3}{2}}f_{-1}(x)^2$ 261 $-\frac{z}{c^2}\left(1+\frac{z}{c^2}f\right)^{-\frac{3}{2}}f_{2}\dot{x}\dot{y}$ 262

 $-\frac{z}{c^2} \left(1 + \frac{z}{c^2} f\right)^{-\frac{2}{2}} f_{-2} \dot{x} \dot{z}$ 263 $-\frac{1}{c^2}\left(1+\frac{2}{c^2}f\right)^{-\frac{2}{2}}f_{1}(y)^2$ 264 $-\frac{1}{c^2}\left(1+\frac{2}{c^2}f\right)^{-\frac{3}{2}}f_{-1}(z)^2$ 265 (94) 266 $(a_{R})_{y} = \left(1 + \frac{2}{c^{2}}f\right)^{-\frac{1}{2}} \dot{y} + \left(1 + \frac{2}{c^{2}}f\right)^{\frac{1}{2}} f_{'2}(t)^{2}$ 267 $+\frac{1}{c^2}\left(1+\frac{2}{c^2}f\right)^{-\frac{2}{2}}f_{2}(x)^2$ 268 $-\frac{2}{c^2}\left(1+\frac{2}{c^2}f\right)^{-\frac{2}{2}}f_{11}\dot{x}\dot{y}$ 269 $-\frac{2}{c^2}\left(1+\frac{2}{c^2}f\right)^{-\frac{3}{2}}f_{-2}\dot{y}\dot{z}$ 270 $-\frac{1}{c^2}\left(1+\frac{2}{c^2}f\right)^{-\frac{3}{2}}f_{,2}(\psi)^2$ 271 $+\frac{1}{c^2}\left(1+\frac{2}{c^2}f\right)^{-\frac{3}{2}}f_{,2}(z)^2$ 272 (95) 273 $(a_R)_z = \left(1 + \frac{2}{c^2}f\right)^{-\frac{1}{2}} \ddot{z} + \left(1 + \frac{2}{c^2}f\right)^{\frac{1}{2}} f_{s^2}(t)^2$ 274 $+\frac{1}{c^2}\left(1+\frac{2}{c^2}f\right)^{-\frac{2}{2}}f_{,2}(\dot{x})^2$ 275 $+\frac{1}{c^2}\left(1+\frac{2}{c^2}f\right)^{-\frac{2}{2}}f_{,2}(\psi)^2$ 276 $-\frac{1}{c^2}\left(1+\frac{2}{c^2}f\right)^{-\frac{2}{2}}f_{,3}(z)^2$ 277 $-\frac{2}{c^2}\left(1+\frac{2}{c^2}f\right)^{-\frac{3}{2}}f_{z}\dot{y}\dot{z}$ 278 $-\frac{z}{c^2}\left(1+\frac{z}{c^2}f\right)^{-\frac{3}{2}}f_{,1}xz$ 279 $-\frac{2}{2}\left(1+\frac{2}{c^2}f\right)^{-\frac{2}{2}}f_{0}t\dot{z}$ 280 (96)281 $(a_{R})_{x^{0}} = c \left(1 + \frac{2}{c^{2}}f\right)^{-\frac{1}{2}} \tilde{t} + \left(1 + \frac{2}{c^{2}}f\right)^{-\frac{3}{2}} f_{,0}(t)^{2}$ 282 $+\frac{2}{c}\left(1+\frac{2}{c^2}f\right)^{-\frac{3}{2}}f_{11}\dot{x}\dot{t}$ 283 $+\frac{2}{c}\left(1+\frac{2}{c^2}f\right)^{-\frac{4}{2}}f_{c2}t\dot{y}$ 284 $+\frac{2}{c}\left(1+\frac{2}{c^2}f\right)^{-\frac{3}{2}}f_{c2}t\dot{z}$ 285 $-\frac{1}{c^2}\left(1+\frac{2}{c^2}f\right)^{-\frac{1}{2}}f_{,0}(x)^2$ 286 $-\frac{1}{a^2}\left(1+\frac{2}{a^2}f\right)^{-\frac{1}{2}}f_{,0}(\psi)^2$ 287 $-\frac{1}{c^2}\left(1+\frac{2}{c^2}f\right)^{-\frac{1}{2}}f_{,0}(z)^2$ 288 (97) 289 290

291 3. RESULTS AND DISCUSSION

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293 Equations (26), (27), (28) and (29) are the Riemannian velocity in the cartesian coordinate 294 system using the golden metric tensor while (94), (95), (96) and (97) are the Riemannian 295 acceleration in the cartesian coordinate using the golden metric tensor. These results are 296 mathematically most elegant, physically most natural and satisfactory for describing the motion of particles of nonzero rest masses and its consequences in the cartesian coordinate. 297 298 They also correspond to a generalization of the equations of motion and all the 299 foundamental quantities in the cartesian coordinate

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302 4. CONCLUSION

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304 It is most interesting and instructive to note that the Riemannian velocity and Riemannian acceleration obtained reduces, in the limit of c⁰ to the pure Euclidean results and otherwise 305 306 contain post Euclidean corrections of all orders of c⁻².

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