

## **Original Research Articles**

# **Climate Sensitivity Parameter in the Test of the Mount Pinatubo Eruption**

### **ABSTRACT**

The author has developed one dimensional dynamic model (1DDM) to simulate the surface temperature change ( $\Delta T$ ) caused by the eruption of Mount Pinatubo. The main objectives have been 1) to test the climate sensitivity parameter ( $\lambda$ ) values of  $0.27 \text{ K/(Wm}^{-2}\text{)}$  and  $0.5 \text{ K/(Wm}^{-2}\text{)}$ , 2) to test the time constants of a simple first-order dynamic model, and 3) to estimate and to test the downward longwave radiation anomaly ( $\Delta \text{LWDN}$ ). The simulations show that the calculated  $\Delta T$  of 1DDM follows very accurately the real temperature change rate. This confirms that theoretically calculated time constants of earlier studies for the ocean (2.74 months) and for the land (1.04 months) are accurate and applicable in the dynamic analyses. The 1DDM-predicted  $\Delta T$  values are close to the measured value, if the  $\lambda$ -value of  $0.27 \text{ K/(Wm}^{-2}\text{)}$  has been applied but the  $\lambda$ -value of  $0.5 \text{ K/(Wm}^{-2}\text{)}$  gives  $\Delta T$  values, which are about 100 % too large in the early phases of the eruption. The main uncertainty in the Mount Pinatubo analyses is the  $\Delta \text{LWDN}$  flux, because there are no direct measurements available during the eruption. The author has used the measured ERBS fluxes and has also estimated  $\Delta \text{LWDN}$  flux using the apparent transmission measurements. This estimate gives the best and most consistent results in the simulation. A simple analysis shows that two earlier simulations utilising General Circulation Models (GCM) by two research group are depending on the flux value choices as well as the measured  $\Delta T$  choices. If the commonly used minimum value of  $-6 \text{ Wm}^{-2}$  would have been used for the shortwave anomaly in the GCM simulations, instead of  $-4 \text{ Wm}^{-2}$ , the  $\Delta T$  values would differ from the measured  $\Delta T$  values almost 100 %. The main reason for this error seems be the  $\lambda$ -value of  $0.5 \text{ K/(Wm}^{-2}\text{)}$ . The mean  $\lambda$ -value of  $1.0 \text{ K/(Wm}^{-2}\text{)}$  commonly used in GCMs would give 200 % too high values.

*Keywords: Global warming, climate sensitivity parameter, climate response time, radiative forcing response, downward radiative fluxes, Mount Pinatubo eruption.*

## **1. INTRODUCTION**

### **1.1 Objectives and Symbols**

The Mount Pinatubo eruption in 1991 caused a global cooling during the next five years as the incoming shortwave radiation was reduced by  $6 \text{ W/m}^2$  offering a unique opportunity to test and to analyse the various phenomenon of the climate system. The first objective of this paper is to test the two climate sensitivity parameter values which have been commonly used in the scientific studies. The second objective is to test the climate system time constants describing the dynamic behaviour of the climate exposed to a relative big and sudden change. The third objective is to estimate and to test the downward longwave radiation anomaly ( $\Delta \text{LWDN}$ ). In the simulations a theoretical feedback property of the climate system has been also tested.

28 Table 1 includes all the symbols, abbreviations, acronyms and definitions used repeatedly in  
29 this paper.

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31 **Table 1. List of symbols, abbreviations, and acronyms**

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Acronym	Definition
1DDM	One dimensional dynamic model
AT	Apparent transmission
ENSO	El Niño Southern Oscillation
ERBS	NASA's Earth Radiation Budget Satellite
ECS	Equilibrium climate sensitivity
GCM	General Circulation Model
ISCCP	International Satellite Cloud Climatology Project
LW	Longwave
LWDN	LW radiation flux downward
LWUP	LW radiation flux upward
LWSRF	LW radiation emitted by the surface
ONI	Oceanic Niño Index
RF	Radiative forcing change
SW	Shortwave
SWATM	SW radiation flux absorbed by the atmosphere
SWIN	SW radiation flux incoming at the TOA
SWSRF	SW radiation flux incoming at the surface
TOA	Top of the atmosphere
TPW	Total precipitable water
T	Surface temperature
T <sub>m</sub>	1DDM-predicted surface temperature change
T <sub>av</sub>	Average surface temperature by four datasets
T <sub>msu</sub>	Surface temperature by UAH MSU dataset
T <sub>av-e</sub>	T <sub>av</sub> with ENSO correction
T <sub>msu-e</sub>	T <sub>msu</sub> with ENSO correction
TCS	Transient climate sensitivity
$\lambda$	Climate sensitivity parameter
$\Delta$	Anomaly or change

33 Subscript<sub>n</sub> means step n in time domain.

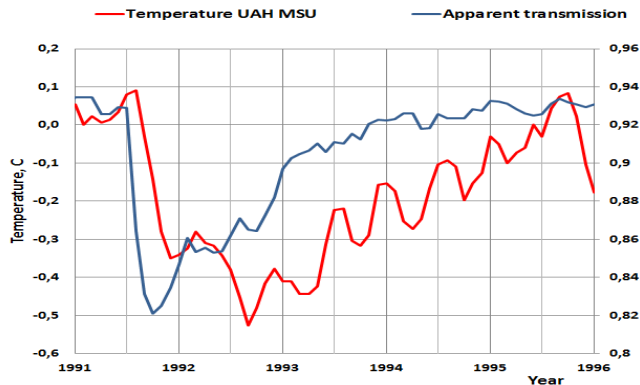
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## 35 1.2 The Mount Pinatubo eruption

36 The main eruption of the Mount Pinatubo volcano (15.1 °N, 120.3 °E) on the island of Luton  
37 in the Philippines began on the 3<sup>rd</sup> of June, 1991 and concluded on the next day. Four large  
38 explosions generated eruption columns reaching the heights of up to 24 km in the  
39 stratosphere. The estimate of the stratospheric mass increase was 14 – 20 Mt of SO<sub>2</sub>, which  
40 created 21-40 Mt of H<sub>2</sub>SO<sub>4</sub>-H<sub>2</sub>O aerosols [1]. The eruption also injected vast quantities of  
41 minerals and metals into the troposphere and stratosphere in the form of ash particles. The  
42 aerosols formed a global layer of sulfuric acid haze over the globe and the global  
43 temperatures dropped about 0.5 °C in the years 1991 – 1993.

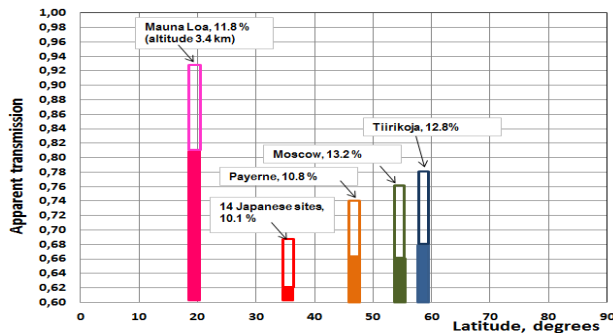
44 The sulphate aerosols caused scattering of the visible light and therefore the incoming  
45 radiation scattered more effectively back into space. Thus the albedo of the Earth increased  
46 leading to a cooling at the Earth's surface. On the other hand the plants utilized the climate  
47 conditions, because they could photosynthesize more effectively in the diffuse sunlight [2]-  
48 [3]. As a result of the more intensive photosynthesis, there was a negative anomaly of the  
49 global CO<sub>2</sub> concentration increase rate.

Because the eruption happened at one point, it took several weeks before the global effect was fully developed. The volcanic aerosol cloud encircled the Earth in 21 days driven by the easterly winds in the tropical stratosphere. It covered about 42 % of the Earth in two weeks [4]. In Fig. 1 are depicted the global temperature [5] and the apparent transmission measured at Mauna Loa [6] (19.3 °N, 155.4 °W). It can be seen that there is delay between the temperature response and the apparent transmission (AT) describing the reduction of the incoming shortwave (SW) radiation.



**Fig.1. The global surface temperature and the apparent transmission measured at Mauna Loa, Hawaii.**

In Fig. 2 the apparent transmissions (AT) are depicted at the various sites on the northern hemisphere [7]. It can be seen that the absolute values of the AT values are different depending mainly on the local conditions. For example, the low values of the Japanese sites describe the air quality of the local conditions. The large value of the Mauna Loa is due to the fact that it is at the altitude of 3.4 km in the middle of the Pacific. An important feature thinking the analysis methods of this study is that the percentage decreases are very close to each other in the range from 10.1 % to 13.2 %.



**Fig. 2. The apparent transmission values at the various sites. The percentage values show the maximum decreases of the apparent transmissions after the eruption.**

The sites in Fig. 2 cover almost 85 % of the northern hemisphere. It can be assumed that the same development happened on the southern hemisphere as well. The reason why the decrease of apparent transmission value is almost the same at the high latitudes as in the tropics is probably due to the zenith angle. Even though the sulphate cloud would be thinner at the high latitudes, the sunlight has a longer pathway through the atmosphere. This compensates the effects of thinner cloud conditions and causes finally the same decrease in the SW insolation flux.

Two conclusions can be drawn from these figures. The global delay called a dead time in process dynamics, is estimated to be 1.6 months between the incoming SW radiation change and the global surface temperature response. This value is used in the dynamical analyses of this study.

Another conclusion is that after the fully developed coverage of the sulphate cloud in the stratosphere, the radiation effect changes can be estimated to happen simultaneously over the globe. Therefore it is justified to use the one dimensional (1D) approach in developing a dynamic model (called 1DDM) for analysing the temperature versus radiation flux relationships.

### 1.3 Earlier studies

There have been numerous Pinatubo studies on the three major fields. The first is on the aerosol and chemical effects of the Pinatubo particles. The second is focused on optical properties of the aerosol particles and on the radiative forcing. The third is on the responses to the forcing affecting the temperature and the circulation patterns.

This paper concentrates on the dynamic behaviour of the surface temperature changes caused by the radiative flux changes. Therefore the survey of the earlier studies covers only the subjects which are relevant for this study.

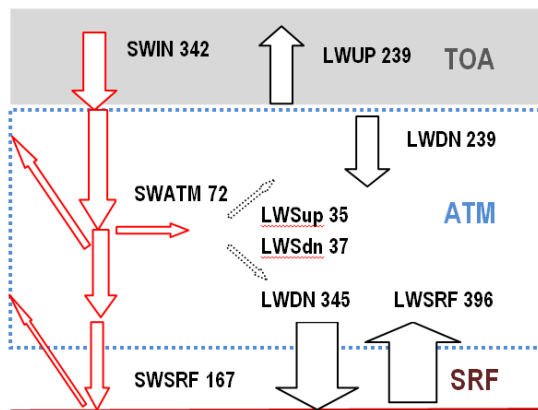
Even though the Pinatubo eruption is the best documented major eruption so far, there was an essential radiative flux, which was not directly measured during the eruption. This was the LW downward radiation flux (LWDN), which is essential, because it compensates the major portion of the cooling effects of the reduced SW downward radiation flux (SWIN) decrease during the early phases of the eruption [8].

The World Climate Research Programme (WCRP) Radiative Fluxes Working Group initiated a new Baseline Surface Radiation Network (BSRN) to support the research projects. Some years later the BSRN was incorporated into the WCRP Global Energy and Water Cycle Experiment (GEWEX). The BSRN network stations started to operate in 1992 and that is why these valuable measurements were not available during the Pinatubo eruption. In October 2010 the Eyjafjallajökull volcano in Iceland erupted, covering the major part of Europe with the ash cloud. Strange enough – even though there were 10 operational BSRN stations in this area - none of them was measuring LWDN fluxes during the eruption. So another case was missed in detecting this essential radiative flux during a volcano eruption.

There has been a special GEWEX project to assess the surface radiation budget datasets [9] based on the available data at TOA. By studying the GEWEX results, the author's conclusion is that the LWDN fluxes could not be estimated reliably in this project based on the other existing flux data. Therefore a major challenge in this study is to estimate the  $\Delta$ LWDN flux trend during the Pinatubo eruption.

In Fig. 3 the radiative fluxes of the Earth are illustrated [10]-[11]. The climate forcing effect of a volcano eruption can be analysed in the same way as the cloud change forcing. Normally the cloud forcing has been calculated as the sum of changes in the downward SW flux change and outgoing LW flux change between the clear and all-sky conditions. Applying this same method, the radiative forcing (RF) caused by the eruption, is the sum of  $\Delta$ SWIN and  $\Delta$ LWUP and it is called aerosol radiative forcing [12]. The change in the flux values is calculated between the normal conditions and during or after the eruption. Because the outgoing LW flux is reduced during the early phases of the eruption, it is a sign that there is cooling happening on the surface.

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**Fig. 3. The main radiative fluxes of the Earth's energy balance.**

136 The RF value calculated in this way is normally called radiative or climate forcing (RF).  
 137 Actually it is only a measure of the real RF. There are two fluxes which have the real forcing  
 138 effect on the Earth's surface temperature (T) and they are SWIN and LWDN. In the case of  
 139 cloudy sky and the all-sky, the change of LWUP is  $11 \text{ Wm}^{-2}$  and the change of LWDN is  $14.3$   
 140  $\text{Wm}^{-2}$ , showing that the changes are not equal even though they are close to each other [11].

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142 The small particle sizes less than  $1 \mu\text{m}$  are more effective in reflecting the SW solar radiation  
 143 SWIN than they are at reflecting the LW radiation emitted by the surface. According to a  
 144 comprehensive study [1], the smallest particles were sulphuric acid/water droplets and the  
 145 largest particles were ash fragments. The cooling and warming effects of the aerosols and  
 146 particles depend on the particle sizes. The LWDN flux increases especially during the early  
 147 phases of the eruption because there are larger aerosol particles more in the atmosphere  
 148 than in the later phases. Therefore the warming effect of LWDN is the most effective at the  
 149 same time as the cooling is in maximum [1]. The stratospheric ash layer settled down just  
 150 above the troposphere staying there until March 1992. The particle size measurements [1]  
 151 showed that there was a peak in both small and large particle sizes after a few months after  
 152 the eruption but by 1993 the high measurements values were decaying back to pre-eruption  
 153 values.

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155 The ash cloud in the high altitudes of the atmosphere absorbs and emits radiation. This ash  
 156 cloud had a measureable warming effect on the northern hemisphere winter temperatures  
 157 [13]-[14]. The ash cloud has about the same effect as the clouds have in the cold climate  
 158 conditions that it will prevent the cooling of the surface. In this way it has a net warming  
 159 effect.

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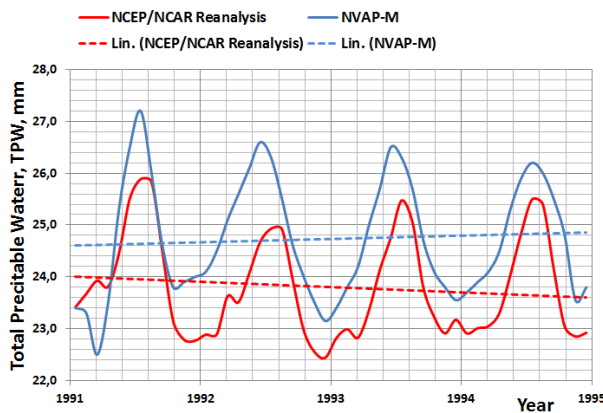
161 The forcing studies can be classified into two categories namely forcing calculations utilising  
 162 General Circulation Models (GCM) 1) for simulations of spatial flux and temperature changes  
 163 [12], [14]-[19], and 2) other simulations resulting the surface temperature change. In respect  
 164 to this study only the latter studies are relevant.

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166 One of the earliest studies was that of Hansen et al. [20]. They used the GISS global climate  
 167 model to assess the preliminary impacts of the Pinatubo eruption. In their calculations they  
 168 used the peak value of  $-4 \text{ Wm}^{-2}$  for  $\Delta\text{SWIN}$  and they could show that the simulated  $\Delta T$  was  
 169 about  $-0.5 \text{ }^{\circ}\text{C}$ . The most common value of  $\Delta\text{SWIN}$  has been  $-6 \text{ Wm}^{-2}$  [12]-[13], [16]-[17], [21].  
 170 This value is also used in this study.

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In the later study [22] Hansen et al. applied the same peak value of  $-4 \text{ Wm}^{-2}$  in the GCM simulations by name SI94 and GRL92. Soden et al. [23] applied a GCM and as input data they used ERBS fluxes in calculating the RF values. They also included the absolute atmospheric water content as a variable. The peak value of  $-4 \text{ Wm}^{-2}$  was used for  $\Delta \text{SWIN}$ . Their major result was the GCM simulations could calculate the  $\Delta T_m$  values close to the measured value, if the positive water feedback was included. The water content was calculated using the NASA Water Vapor Project (NVAP) values [24]. In Fig. 4 the NVAP dataset values as well the NCEP/NCAR (National Center for Environmental Prediction / National Center for Atmospheric Research) values are depicted [25]. The graphs show that there are opposite trends in these datasets during the Pinatubo eruption. It is quite impossible to know, which of these datasets is correct and therefore the question of positive or negative water feedback cannot be reliably tested utilising the Pinatubo case.



**Fig. 4. The graphs of water contents according to NVAP-M and NCEP/NCAR datasets.**

The radiative forcing (RF) at TOA has a linear relationship to the global mean surface temperature change  $\Delta T$ , if the equilibrium state is assumed [26]:

$$\Delta T = \lambda \text{RF}, \quad (1)$$

where  $\lambda$  is the climate sensitivity parameter. According to IPCC [27]  $\lambda$  is a nearly invariant parameter having a value of  $0.5 \text{ K/(Wm}^{-2})$ . IPCC uses this value in calculating the transient climate sensitivity (TCS) value of  $1.75 \text{ }^{\circ}\text{C}$  [26] ( $0.5 \text{ K/(Wm}^{-2}) * 3.7 \text{ Wm}^{-2} = 1.75 \text{ K}$ ). Actually there should not be any of IPCC's own climate models, but in reality the structure and the values of such a model called "Radiative Forcing by Emissions and Drivers" has a summary leading to the value of  $2.34 \text{ Wm}^{-2}$  [28]. According to IPCC's own definition, the  $\Delta T$  of this model should be  $1.17 \text{ }^{\circ}\text{C}$  in 2111. IPCC does not show this temperature increase in the latest Assessment Report 5 and a reason might be that it is 38 % greater than the observed value.

Ollila has analysed [29] the future warming values based on the RF values of greenhouse gases. In these analyses of the different RCPs (Representative Concentration Pathways), IPCC uses the  $\lambda$  value of about  $0.36 \text{ K/(Wm}^{-2})$ . Thus it appears that IPCC is very inconsistent in using the  $\lambda$ .

IPCC has made a summary of 30 GCMs in the Assessment Report 5 (AR5). The  $\lambda$  values used in their summary vary between 0.6 and 1.6 totally in 23 GCMs and the model mean is  $1.0 \text{ K/(Wm}^{-2})$ . A so high  $\lambda$  should be used only in calculating the equilibrium climate sensitivity (ECS). EQS is roughly twice the value of TCS and it takes hundreds of years to reach the equilibrium state [28]. The TSC can be reached in less than a year, because the

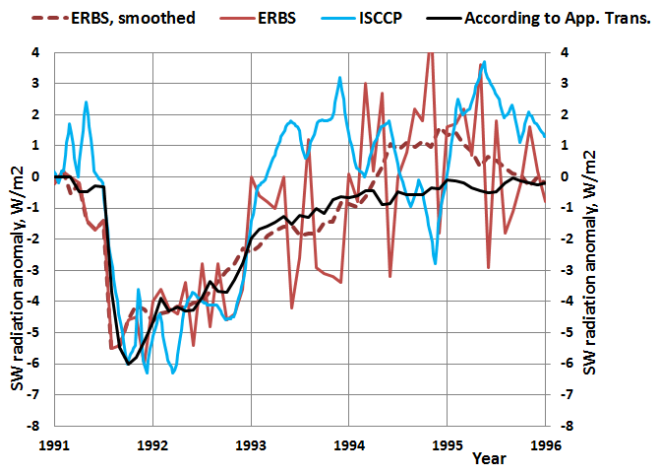


water feedback reacts very quickly to the temperature changes. The possible water feedback is the only essential feedback in TCS calculations. In the referred GCM studies applied in the Pinatubo analyses, there are no specifications about the  $\lambda$  value of these GCMs.

There are several studies, which have calculated the climate sensitivity value to be about 1.0 – 1.2 °C [30]-[33] using the same radiative forcing value of  $3.7 \text{ Wm}^{-2}$  for  $\text{CO}_2$  as IPCC uses. It means a lower  $\lambda$  value of about  $0.3 \text{ K}/(\text{Wm}^{-2})$ . Some researchers have calculated even lower values like 0.6 °C for climate sensitivity [29], [34] or 0.7 °C [35]. Ollila [29] has calculated the  $\lambda$  value using three different methods and his results vary between 0.245 and 0.331 the most reliable value being  $0.268 \text{ K}/(\text{Wm}^{-2})$ . In this study these two most common values have been applied:  $0.27 \text{ K}/(\text{Wm}^{-2})$  and  $0.5 \text{ K}/(\text{Wm}^{-2})$ .

## 2. RADIATIVE FLUXES AND FORCING ANOMALIES CAUSED BY THE ERUPTION

The two SWIN flux datasets available during the eruption are ISCCP [36] and ERBS [37]. They are depicted in Fig. 6. Both datasets are unstable and spiky. The SWIN flux anomaly can also be estimated using the apparent transmission (AT) signal or optical depth measurements. In this case the AT signal of Mauna Loa has been used. The  $\Delta\text{SWIN}$  flux anomaly has been assumed to follow exactly the trend of the AT-signal. The time of the minimum value of the AT-signal has been used to be also the time of the minimum value of the SWIN flux value of  $-6 \text{ Wm}^{-2}$ . This estimate of  $\Delta\text{SWIN}$  flux is depicted in Fig. 5 and it can be noticed that this flux is very stable and its trend follows very well the average form of ISCCP and ERBS fluxes. The smoothed  $\Delta\text{ERBS}$  SWIN flux signal follows the estimated AT transformed  $\Delta\text{SWIN}$  flux signal so well that they could be used between each other.

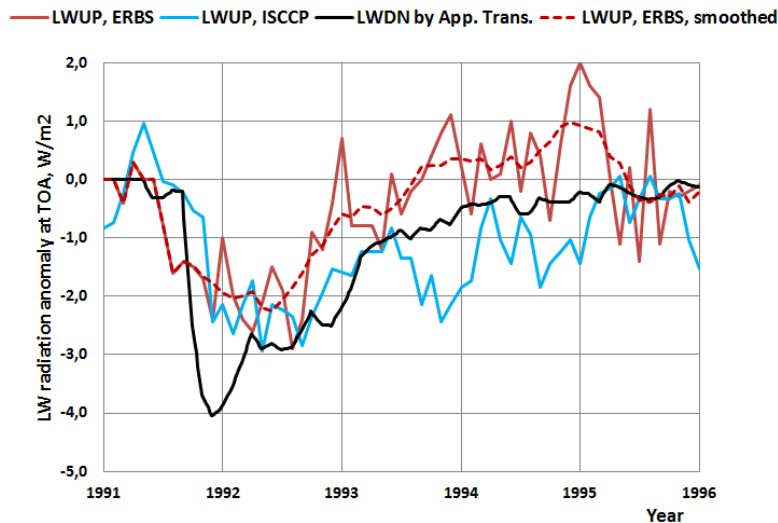


**Fig. 5. SW downward radiation flux anomalies at TOA.**

The two LWUP flux datasets available are ISCCP [36] and ERBS [37]. They are depicted in Fig. 6. Both fluxes are very spiky and the flux levels have the difference of about  $1 \text{ Wm}^{-2}$  after the year 1993.

Because there are no direct measurements of LWDN flux, it has been estimated. As realized before, the LWDN flux anomaly should follow the amount of large aerosol particle amounts in the atmosphere. Russell et al. has a Fig. 6 in their paper [1] containing information about the different particle size trends measured at Mauna Loa during the eruption.

It has been assumed that the smaller particle sizes from 0.382 to 0.500  $\mu\text{m}$  are related to the  $\Delta\text{SWIN}$  flux anomaly. The largest particle size is 1.020  $\mu\text{m}$  and this graph has been used to estimate the  $\Delta\text{LWDN}$  flux peak value. The peak values relationship between the 1.020  $\mu\text{m}$  and 0.382/0.500  $\mu\text{m}$  is 0.675. Using this relationship the peak value of estimated  $\Delta\text{LWDN}$  flux anomaly would be  $0.675 * (-6 \text{ Wm}^{-2}) = -4.05 \text{ Wm}^{-2}$ . The  $\Delta\text{LWDN}$  is been estimated to follow AT signal of Mauna Loa.



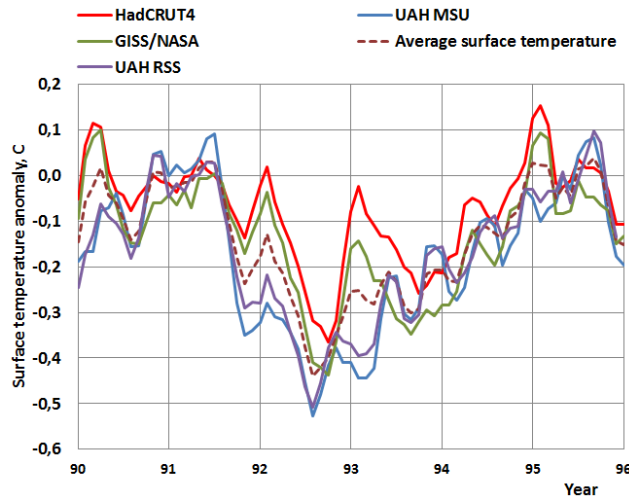
**Fig. 6. LW radiation flux anomalies at TOA.**

Another way to estimate the peak value of LWDN anomaly is to assume that the  $\Delta\text{LWUP}$  flux at TOA is reflected in the same way as the total sun irradiation is reflected back to the space because of the eruption aerosols. The percentage of the  $\Delta\text{SWIN}$  anomaly is  $-6 \text{ Wm}^{-2} / 342 \text{ Wm}^{-2} = -1.75 \%$ . Using this same percentage the LWDN anomaly would be  $-0.0175 * 239 \text{ Wm}^{-2} = -4.2 \text{ Wm}^{-2}$ . This value is close to the estimated value above. The estimated  $\Delta\text{LWDN}$  flux is depicted in Fig. 7.

In Fig. 7 it can be noticed that its peak value is much larger than the  $\Delta\text{LWUP}$  values measured at TOA by ISCCP and by ERBS. One explanation is that  $\Delta\text{LWUP}$  fluxes depend mainly on the surface temperature and therefore there is a dynamic delay in comparison to the  $\Delta\text{LWDN}$  flux. The full effect of this delay is about one year. In the dynamic situations like this Pinatubo eruption anomaly, the maximum temperature anomaly is about from 80 to 90 % from the full effect. This difference is analyzed more deeply in the simulation section.

In the simulations the measured surface temperature anomaly  $\Delta T$  is a reference. There are five dataset commonly available and four of them are depicted in Fig. 7. [5], [38]-[40]. There are small differences in the trends. The UAH MSU trend has the largest minimum value during the eruption. Because of this situation, two surface temperature trends have been used as references namely Tmsu (UAH MSU dataset) and Tav (average of four datasets).

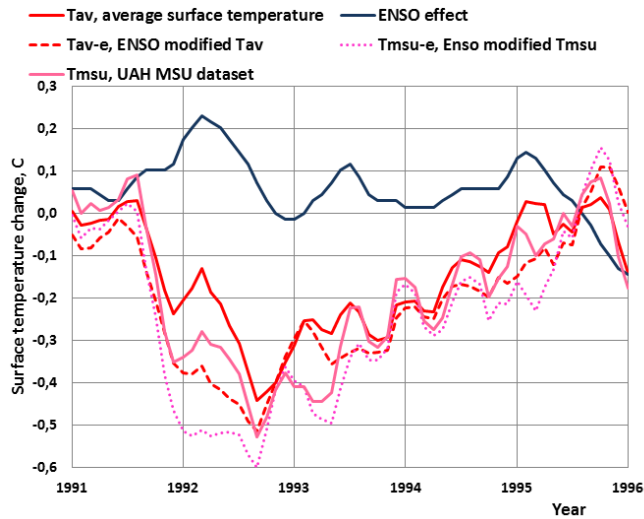




**Fig. 7. Surface temperature anomalies according to four datasets.**

Hansen et al. [22] and Soden et al. [23] have taken into account that the ENSO (El Niño Southern Oscillation) phenomenon had the maximum warming index in January 1992, when the Pinatubo eruption had the strongest cooling effects. So the researchers eliminated the ENSO effect by calculating a modified surface temperature of MSU UAH dataset. According to the graphs of these two papers, the ENSO corrected minimum peak of  $\Delta T$  has been from  $-0.7^{\circ}\text{C}$  to  $-0.75^{\circ}\text{C}$ . They refer to the study of Santer et al. [41]. The author reads this same paper that the maximum mean volcanically induced cooling  $\Delta T_{\text{max}}$  at the surface is from  $-0.35^{\circ}\text{C}$  to  $-0.45^{\circ}\text{C}$  and it is about double in the troposphere. ENSO certainly has a warming effect from 1991 to the end of 1992, and therefore this result is not logical, because the temperatures without ENSO corrections are about the same. There is a graph [41], where the temperature anomaly is about  $-0.75^{\circ}\text{C}$  but it is for the troposphere and not for the surface. Another study of Thompson et al. [42] shows the maximum warming effect of ENSO only  $0.14^{\circ}\text{C}$ .

Because the effects of ENSO are so controversial, this study has used the results of the own analyses. The elimination of ENSO is based on the analysis of ONI values (Oceanic Niño Index) [43] and the global  $\Delta T$  values. The ENSO effect creates fluctuations, which can be identified as almost identical fluctuations of  $\Delta T$  values after 1-12 months delay. The four most regular El Niño / La Niña cases were selected. The relationship from peak to peak between these fluctuations show that  $\Delta T = 0.144 \cdot \Delta \text{ONI}$  in average. These two relationships have been used in modifying the measured  $\Delta T$  values. In Fig. 8 is depicted the ENSO effect as a temperature anomaly and its effect on the two global  $\Delta T$  trends. This approach gives the maximum ENSO effect of about  $0.2^{\circ}\text{C}$ . The ENSO during the Pinatubo eruption has a special feature not having the negative La Niña temperature peak at all.

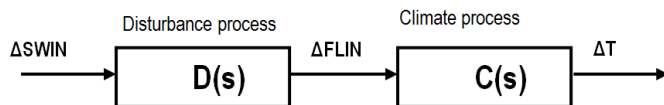


**Fig. 8. The ENSO signal removed from the surface temperature measurement.**

The ENSO effect explains quite well, why there is a peak upward, when the surface temperature should be in minimum because of forcing by  $\Delta\text{SWIN}/\Delta\text{LWDN}$  anomaly. After 1993 the ENSO effect is very small but it caused an upward tick at the end of 1995, when the Pinatubo event was practically over. The ENSO modified surface temperatures Tav-e and Tmsu-e have been used as references in this study.

### 3. DYNAMIC MODEL SIMULATIONS

The Pinatubo eruption happened in such a way that the forcing factors in the form of  $\Delta\text{SWIN}$  and  $\Delta\text{LWDN}$  flux anomalies changed all the time, and therefore the applied model must be dynamical. A dynamical model is capable of simulating time dependent variables and their impacts. In this case a simple one dimensional model 1DDM has been applied as described in Fig. 9. The 1DDM has been written in Laplace domain, because it is the most common and easiest way to describe dynamic processes.



**Fig. 9. The dynamic simulation model of the climate system.**

Three different simulation cases have been described and carried out: 1)  $\Delta\text{SWIN}$  and  $\Delta\text{LWIN}$  fluxes are from ERBS datasets, 2)  $\Delta\text{SWIN}$  and  $\Delta\text{LWIN}$  are estimated as described above based on the AT measurements, 3) Feedback process experiment. The ISCCP dataset turned out to be too swaying and unreliable and therefore it has not been used. In cases 1) and 2) the simulations have been carried out by  $\lambda$  values of  $0.27 \text{ K}/(\text{Wm}^{-2})$  and  $0.5 \text{ K}/(\text{Wm}^{-2})$ .

The input variable  $\Delta\text{SWIN}$  is a flux anomaly signal varying according to the time. The output  $\Delta\text{FLIN}$  of the disturbance process  $D(s)$  are  $\Delta\text{SWIN}$  and  $\Delta\text{LWDN}$  fluxes delayed by 1.6 months. In the case of ERBS, the  $\Delta\text{LWDN}$  is replaced by  $\Delta\text{LWUP}$  anomaly flux. The  $\Delta\text{SWIN}$  and  $\Delta\text{LWDN}$  fluxes are summarized and multiplied by the  $\lambda$ , which transforms the radiative flux forcing at TOA into the temperature change  $\Delta T$  at the surface. The flux  $\Delta\text{FLIN}$  is the

product of this operation. Therefore the  $C(s)$  contains only the time delays of the climate system.

The climate process  $C(s)$  is a combination of two parallel processes, which are the dynamic processes of land and ocean:

$$C(s) = K_{\text{sea}}/(1+T_{\text{sea}}s) + K_{\text{land}}/(1+T_{\text{land}}s), \quad (2)$$

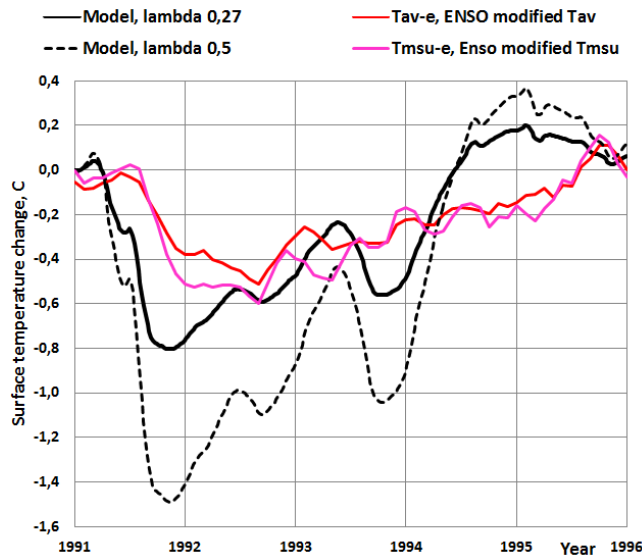
where  $K_{\text{sea}}$  is 0.7,  $K_{\text{land}}$  is 0.3,  $T_{\text{sea}}$  is a time constant of 2.74 months and  $T_{\text{land}}$  is a time constant of 1.04 months. These values are based on the earlier studies [11], [44]-[45]. The values of the  $K$  parameters are the area portions of land and ocean of the Earth.

The dynamic processes according to eq. (2) are first-order dynamic models, which can be simulated in the discrete form enabling continuously changing input variables:

$$\text{Out}(n) = (\Delta t/(T+\Delta t))((T/\Delta t)*(\text{Out}(n-1)+\text{In}(n)), \quad (3)$$

where  $\text{Out}(n)$  is the output of the process in step  $n$ ,  $\text{In}(n)$  is the input of the process of step  $n$ ,  $T$  is the time constant,  $\Delta t$  is the simulation step interval ( $=0.2$  months), and  $n-1$  is the previous step value.

The results of using ERBS flux values are depicted in Fig. 10.



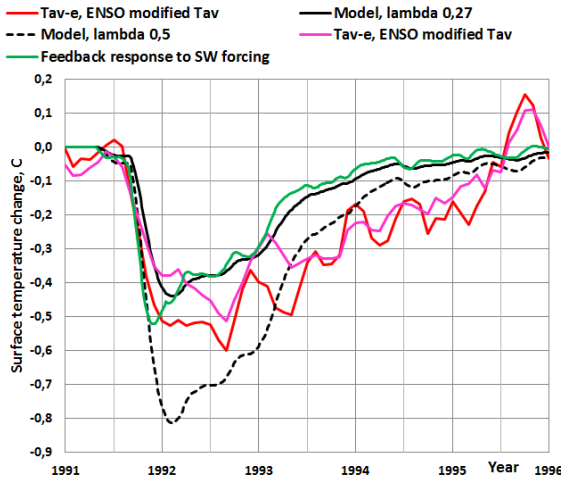
**Fig. 10. The simulated surface temperature according to the dynamic 1DDM using ERBS dataset  $\Delta\text{SWIN}$  and  $\Delta\text{LWUP}$  fluxes.**

It can be noticed that the simulated temperature values vary a lot because the fluxes  $\Delta\text{SWIN}$  and  $\Delta\text{LWIN}$  vary too much. Especially the  $\lambda$  value of  $0.5 \text{ K}/(\text{Wm}^{-2})$  gives  $\Delta T_m$  peak values, which are almost double as large as the  $\Delta T_m$  values using the  $\lambda$  value of  $0.27 \text{ K}/(\text{Wm}^{-2})$ . A possible reason for this is that the  $\text{LWUP}$  flux anomaly is not an accurate enough estimate of the real  $\Delta\text{LWDN}$  flux anomaly and the flux measurements are too inaccurate.

The GCM simulations of Soden et al. [23] gave rather different results. The reasons are that 1) the  $\Delta\text{LWDN}$  was on a much smaller change ( $-4 \text{ Wm}^{-2}$  versus  $-5.5 \text{ Wm}^{-2}$  of this study), and 2) the large fluctuations of  $\Delta\text{LWDN}$  flux after January 1993 were smoothed out and the

$\Delta$ LWDN flux was forced to the zero level around March 1993. Researchers did not explain these choices. If the same choices would have been made in this study, the minimum  $\Delta T_m$  would be about  $-0.6^\circ\text{C}$  and the 1DDM-predicted  $\Delta T_m$  after 1993 would be very close to the observed values with the  $\lambda$ -value of  $0.27\text{ K}/(\text{Wm}^{-2})$ .

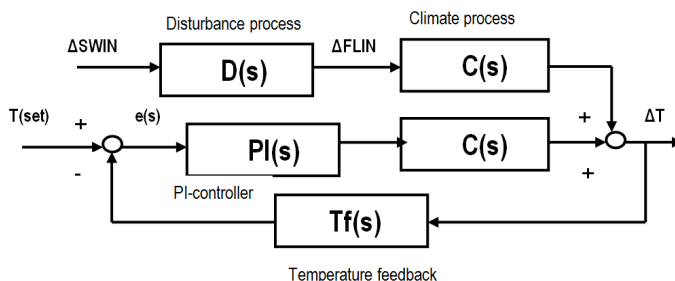
In Fig. 11 the same graphs are depicted, when the  $\Delta$ SWIN and  $\Delta$ LWDN are estimated according to AT measurements. The simulated  $\Delta T_m$  signal is stable and the dynamic changes follow very well the real temperature changes  $\Delta T$ . Also in this case the  $\lambda$  value of  $0.5\text{ K}/(\text{Wm}^{-2})$  gives results, which do not follow the real changes of the surface temperature changes but gives too great  $\Delta T_m$  during the first 1.5 years of the eruption..



**Fig. 11. The simulated surface temperature according to the dynamic 1D model using estimated SWIN and LWDN fluxes.**

The question of feedback has created the two schools of thoughts. Some researchers think that the climate system is like the other processes of the nature, which are built on negative feedbacks. A positive feedback system is dangerous, because it drives any system out of balance sooner or later. IPCC and some other researchers think that the climate system for example includes the positive water feedback as well as positive albedo and cloud feedbacks [28]. It should be noticed that the positive water feedback is included into the climate feedback parameter  $\lambda$ , when its value is  $0.5\text{ K}/(\text{Wm}^{-2})$  [26]. The  $\lambda$ -value of  $0.27\text{ K}/(\text{Wm}^{-2})$  means a constant water content of the atmosphere.

A theoretical feedback process is simulated using the process model depicted in Fig. 12.



**Fig. 12. A theoretical feedback process in the case of Pinatubo eruption.**

The theoretical feedback process can be constructed based on the assumption that the  $\Delta$ SWIN flux anomaly is the only disturbance in a very stable climate system, which tries to eliminate this disturbance. The elimination process is a theoretical PI-controller, which detects a change in the surface temperature and creates an eliminating phenomenon, which tries to minimize the disturbance. In this case the eliminating flux is the  $\Delta$ LWDN flux. The climate process  $C(s)$  has as an input only the  $\Delta$ SWIN anomaly. The PI-controller imitates the counter effect of  $\Delta$ LWDN flux but  $\Delta$ LWDN flux values are not needed to use in this simulation.

The mathematical form of the PI-controller in Laplace domain is

$$\text{Out}(s) = K_p(1+1/(T_i s))e(s) \quad (4)$$

Where  $K_p$  is the gain of the controller,  $T_i$  is the integral time and  $e(s)$  is the error signal between the set point and the measurement. The equation (4) simulated in a discrete form in the time domain is

$$\text{Out}(t) = K_p * \Delta e(t) + (K_p/T_i)\Sigma e(t)\Delta t \quad (5)$$

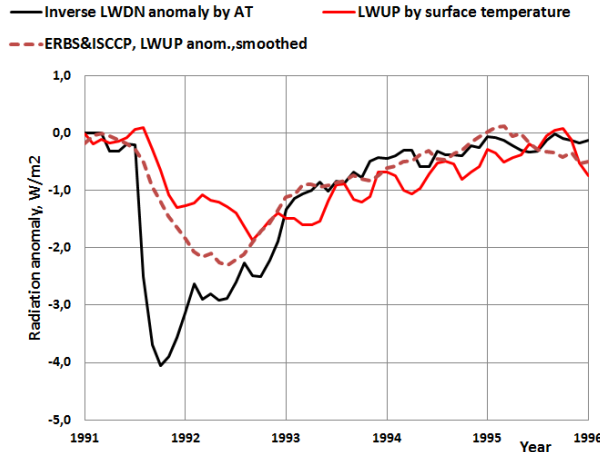
The PI-controller was tuned by trial and error giving  $K_p = 2$  and  $T_i = 500$  months. The results of the negative feedback process simulation are depicted in Fig. 11. The 1DDM-predicted  $\Delta T_m$  follows surprisingly closely the  $\Delta T_m$  values of simulation as well the measured and ENSO corrected  $\Delta T$  values using the  $\lambda$  values of  $0.27 \text{ K}/(\text{Wm}^{-2})$ .

One big difference between this study and the three referred studies [20], [22], and [23] is the use of estimated  $\Delta$ LWDN instead of measured  $\Delta$ LWUP fluxes. The basic reason is that these two fluxes have different values. The measured  $\Delta$ LWUP fluxes are not stable making the results very unstable, too. This problem can be eliminated to a certain degree by heavy smoothing or even by removing parts of a flux signal [23].

The actual  $\Delta$ LWUP flux depends on the surface temperature changes  $\Delta T$  which is caused by the RF change. The RF is the sum of  $\Delta$ SWIN+ $\Delta$ LWDN flux changes. The  $\Delta$ LWUP flux can be calculated using the measured  $\Delta T$  changes. The author has used two calculation methods. The first is MODTRAN radiation code available through Internet [46]. By applying the average global atmosphere profile, MODTRAN can calculate the LWUP flux change at TOA. The main parameters selected for these calculations were:  $\text{CO}_2$  357 ppm, fixed water vapor pressure, cloudy sky with cumulus cloud base of 0.66 km and top of 2.7 km. The  $1^\circ \text{C}$  change in the surface temperature gives  $\Delta$ LWUP change of  $3.39 \text{ Wm}^{-2}$  for the clear sky and  $3.08 \text{ Wm}^{-2}$  for the cloudy sky at TOA. By combining the two sky conditions, the all-sky value of 3.18 can be calculated [10]. Ollila [10] has calculated the same relationship using another commercial spectral analysis tool Spectral Calculator for the clear sky conditions. The cloudy sky fluxes are estimated to be 25 % less than the clear sky fluxes [28]. This calculation method gives the  $\Delta$ LWUP change of  $3.05 \text{ Wm}^{-2}$  for the  $1^\circ \text{C}$  change. The results of MODTRAN calculation have been used, which gives a linear relationship

$$\Delta \text{LWUP} = 3.18 * \Delta T. \quad (6)$$

This linear relationship is applicable inside the small temperature change of  $1^\circ \text{C}$ .



**Fig. 13. The LW fluxes during the Pinatubo eruption.**

The surface temperature calculated  $\Delta LWUP$  is depicted in Fig. 13. It can be compared to the measured  $\Delta LWUP$  flux, which is in this case the average of ISCCP and ERBS datasets. The observed flux has a minimum, which is about three months earlier than the 1DDM-predicted minimum. Anyway this is a very good result showing that  $\Delta LWUP$  depends on  $\Delta SWIN + \Delta LWDN$  fluxes and their dynamic effects on the  $\Delta T$  at the Earth's surface. Therefore  $\Delta LWUP$  is not really the right choice in calculating the surface temperature changes caused by downward radiation flux anomalies of  $SWIN$  and  $LWDN$ .

#### 4. CONCLUSION

The results show that a simple one dimensional dynamic model 1DDM gives results that are close to the real surface temperature changes  $\Delta T$  after the Mount Pinatubo eruption using the climate sensitivity parameter value of  $0.27 \text{ K}/(\text{Wm}^2)$ . Timewise the changes follow very well the real changes. It means that the applied time constants for land (1.04 months) and for ocean (2.74 months) are accurate and can be used in any dynamic simulations. Especially the quick and large  $\Delta T$  during the early phase of the eruption shows that the applied 1DDM follows very accurately the real change rate.

The maximum temperature decrease differs  $+0.07^\circ$  from lowest dataset value (HadCRUT4) and  $-0.09^\circ\text{C}$  from the highest dataset value (UAH MSU) being actually in the middle of the dataset changes. This is a very good accuracy taking into account that the difference between the different temperature datasets is in its maximum  $0.16^\circ\text{C}$  during the minimum peak of the eruption.

The climate sensitivity parameter value of  $0.5 \text{ K}/(\text{Wm}^2)$  gives the minimum peak value of  $-0.82^\circ\text{C}$ , which is almost double in comparison to  $\lambda$  value of  $0.27 \text{ K}/(\text{Wm}^2)$ . This means that the climate models are very sensitive to the value of the climate sensitivity parameter. The mean  $\lambda$ -value of  $1.0 \text{ K}/(\text{Wm}^2)$  commonly used in GCMs would give 200 % too high values.

In this study  $\Delta SWIN$  and  $\Delta LWDN$  fluxes have also been estimated utilizing the apparent transmission measurements. The simulation using these fluxes gives the best and consistent results. The theoretical feedback simulation gives values which are close to the 1DDM model values applying the  $\Delta LWDN$  flux values.

The theoretical simulation of negative feedback of the climate system gives  $\Delta T_m$  results, which follow well both the 1DDM results and the real  $\Delta T$  measurements.



## 5. DISCUSSION

These results can be compared to the results calculated by Hansen et al. [22] and Soden et al. [23] who have used complicated GCMs in their analyses. In these models the temperature effects are based on the eruption aerosol amounts and properties. When comparing the dynamic behavior, the calculated  $\Delta T_m$  of GCMs follows very accurately the real temperature change as does the 1DDM. The conclusion is that the dynamical time delays in their GCMs must come very close to the time constants applied in this study.

The peak values of  $\Delta T_m$  of the GCM studies are  $-0.6^\circ\text{C}$  [22] and  $-0.7^\circ\text{C}$  [23] and according to their graphs, the model-predicted values are practically same as the observed values. The observed values of the GCM studies are almost twice as large as used in this study ( $\Delta T_m = -0.44^\circ\text{C}$ ). One explanation is that in GCM studies a modified UAH MSU dataset has been used, which seems to have a greater ENSO effect correction than is this study.

In the GCM calculations the researchers have used ERBS flux values. In both cases the maximum value of SW anomaly  $\Delta SWIN$  has been about  $-4\text{ Wm}^{-2}$ , which differs 33 % from the value of  $-6\text{ Wm}^{-2}$  used in the majority of the other GCM studies and also in this study. The maximum LW anomaly  $\Delta LWUP$  used in the GCM studies has been about  $-2.5\text{ Wm}^{-2}$ . Using eq. (1) for steady-state conditions, the calculated peak  $\Delta T$  would be  $0.5 * (-4 + 2.5) = -0.75^\circ\text{C}$ . This value is very close to the model-predicted value of Soden et al. [23]. On the other hand, if the commonly used value of  $-6\text{ Wm}^{-2}$  were to be used, the calculated peak  $\Delta T$  would be  $0.5 * (-6 + 2.5) = -1.75^\circ\text{C}$ . Because the average  $\lambda$ -value of GCMs is  $1.0\text{ K}/(\text{Wm}^{-2})$  the  $\Delta T$  would be even larger.

This simple analysis shows that the model-predicted  $\Delta T_m$  values are completely depending on the selected forcing fluxes and even on the selected observed  $\Delta T$  value. It looks that in GCM simulations [22]-[23] the selected  $\Delta SWIN$  flux cannot be regarded as the justifiable choice. Actually the greatest uncertainty is about the right  $\Delta LWDN$  flux values, because there are no direct measurements available. The commonly used  $\Delta LWUP$  flux as a part of radiative forcing at TOA, is not the same flux as  $\Delta LWDN$ .  $\Delta LWUP$  is mainly depending on the real RF fluxes and on the surface temperature. Therefore it contains for example the dynamic delays of the land and ocean and finally the warming effects of the forcing radiation fluxes. In the dynamic simulations this is a source of error. The real measured  $\Delta LWDN$  fluxes are very spiky – especially ISCCP fluxes.

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