

# **Discussion of Foster & Brown's time and tide: analysis of sea level time series**

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## **ABSTRACT**

The recognition of the non-accelerating, periodic pattern of sea levels as described by the tide gauges measurements does not require any special mathematical tool. Providing enough data of sufficient quality have been recorded, If the classical linear fitting is used to compute the rate of rise at any time, then the acceleration is simply the time rate of change of this velocity. By using this technique, the lack of any acceleration over the last few decades is evident in the naturally oscillating, slow rising, tide gauges of appropriate quality and length. Contrary to what is claimed in the commented paper, the accuracy in the computation of the periodicities of the natural oscillations does not impact at all on this result. As the measured sea level oscillations are not perfectly sinusoidal, clearly different assumptions about the shape of the periodic functions, their number and the definition of the algorithm used to compute the parameters of the selected periodic functions all affect the determination of the periodicities. This has however very little influence on the present sea level debate questioning the presence or the absence of acceleration at the tide gauges.

*Keywords: Sea level rise, sea level acceleration, sea level oscillations, computations, experiments*

## **1. INTRODUCTION**

Analyses of the sea levels recorded by the tide gauges have shown that contrary to the IPCC claim, there has been no sign of carbon dioxide driven acceleration since the 1950. The sea levels are mostly oscillating, on average slow rising with a rate close to the subsidence rate of the tide gauge, and absolutely not accelerating over the last few decades (Parker, 2013; Parker, 2014; Carter et al, 2014).

According to Foster & Brown (2014), the papers that have examined sea level data to estimate the pattern of acceleration and deceleration proposing cyclic or quasi-periodic

variations “*contain technical problems which call their results into question*”. In this way, the authors try to make unclear what is otherwise very evident, defocusing the debate from the striding differences from the pattern predicted by the Intergovernmental Panel on Climate Change (IPCC) climate models and the actual measurements at the tide gauges.

The existence of natural, multi-decadal oscillations up to a quasi-60 years is a very well-known feature of sea levels. As evidenced by Carter et al (2014), all the climate-related phenomena, including the sea-level, change through time in a non-stationary way and exhibit repetitive (though not exactly regular) patterns of behavior decadal and multi-decadal periods. Changes in the rate of global sea-level are, for example, known to be influenced by a 50-60 year rhythm related to oceanic internal variability e.g., Pacific Decadal Oscillation, PDO; Atlantic Meridional Oscillation, AMO (e.g. Holgate, 2007; Chambers et al, 2012; Marcos, Tsimplis & Calafat, 2012; Soon & Legates, 2013; Parker et al, 2013). Long period tidal constituents (the 18.6 lunar nodal cycle, for example) also exert an influence on sea-level height (e.g. Pugh, 2004; Yndestad et al, 2008). Morner (2013) discussed the influence of the Helios sphere and the Earth magnetosphere on the climate on Earth. The solar-planetary beat has a 60-years cycle. The Earth’s rate of rotation has a 60-years Length of Day (the standard method to measure the Earth’s rate of rotation) cycle. The Global temperature has a 60 years cycle. The North Atlantic circulation has a 60 years cycle. The 60-years cycle recorded in solar activity and earth rotation affects the oceanic circulation, the temperatures and the sea levels.

While the existence of multi-decadal oscillations is very difficult to be negated, the autocorrelation issue raised by Foster & Brown (2014) did not put in question the existence of the natural fluctuations but at the most the accuracy of the computation of the amplitudes, phases and periodicities of the oscillations. As a matter of fact, the most part of the work on the multi-decadal periodicities claim the existence of quasi-20 or quasi-60 year’s periodicities, and not certainly of perfectly sinusoidal oscillations of time periods computed within an accuracy of the nanoseconds. It is shown with a simple methodology as the sea levels are not accelerating and the issues raised by Foster & Brown (2014) are irrelevant.

## 2. METHODOLOGY

Many tide gauges are recording the relative sea levels since the 1800s and the early 1900s in coastal locations worldwide and the linear analysis of the monthly average values has been historically the method of determining the relative rate of rise (Parker et al, 2013). Because of the quasi-60 years oscillations, Carter et al (2014) concluded that sea-level records longer than 60 years, and even better longer than 120 years, are required to identify any long-term trends that might, or might not, occur in the data. Considering not too many tide gauges are measuring sea levels since more than 120 years ago without any quality issues, Parker et al (2013) and Parker (2014) suggested using tide gauge signals continuously covering more than 60 years without many gaps and without any perturbing event as the relocation or substitution of the tide gauge.

The assessment of the presence (or absence) in the tide gauge records of enough length and quality of any acceleration induced by the anthropogenic carbon dioxide emission claimed by the climate model is then very simple. The simple mathematics has been proposed in Parker et al (2013), Parker (2014) and other papers and it is reproduced below.

The relative rate of rise SLR is computed through the linear fitting applied to the distribution of measured points  $\{x_i, y_i\}$   $i=1, \dots, n$  where  $y_i$  is the monthly average relative mean sea level at the time  $x_i$ . The relative rate  $SLR_{j,k}$  is computed over the time window  $(x_k-x_j)$  by linearly fitting the data  $\{x_i, y_i\}$   $i=j, \dots, k$  through the formula:

$$SLR_{j,k} = \frac{\sum_{i=j}^k (x_i - \bar{x}) \cdot (y_i - \bar{y})}{\sum_{i=j}^k (x_i - \bar{x})^2} \quad (1)$$

where  $\bar{x}$  and  $\bar{y}$  are the sample means.

If  $j=1$  (the oldest record) and  $k=n$  (the latest record), then  $SLR_{1,n}$  is the latest estimation of the relative rate of rise at the time  $x_n$ .

If  $j$  is variable and  $k=n$ , then  $SLR_{i,n}$  is the present velocity for different time windows  $x_n - x_i$ , simulating the effect of the tide gauge recording started at different times  $x_i$  rather than  $x_1$  (Parker et al, 2013; Parker, 2014).

If  $j=1$  (the oldest record) and  $k$  is variable, then  $SLR_{1,k}$  is the estimation of the relative rate of rise at the time  $x_k$ .

From Equation (1) with  $j=1$  and  $k$  variable it is possible to compute the acceleration:

$$SLA_k = \frac{SLR_{1,k} - SLR_{1,k-1}}{x_k - x_{k-1}} \quad (2)$$

To help understanding the effect of the multi-decadal oscillation, the measured data may be replaced with a fitting with a line and multiple sines (Parker, Saad Saleem & Lawson 2013; Parker 2014). This fitting with a line and sines has the expression:

$$y^*(x) = (A^* + SLR^* \cdot x) + \sum_{i=1}^n \left[ A_i \cdot \sin \left( \pi \cdot \frac{x - x_{c,i}}{w_i} \right) \right] \quad (3)$$

where  $y^*$  is the fitted relative sea level and the time  $x$ ,  $SLR^*$  is the relative rate of rise and  $A^*$  is the intercept, while  $A_i$ ,  $x_{c,i}$ ,  $w_i$  are the amplitudes, phases and periods of the oscillations permits to study the effect of the natural oscillations. It is worth to mention that equation (3) may also provide a tool to fill the gaps eventually available in a time series.

### 3. RESULTS

Application of equation (1) and equation (2) to a proper data set is enough to confute all the sea level accelerating claims without any need of hypothetically more sophisticated measurement and analysis tools only contributing to make more confused a worldwide sea level pattern that is otherwise very clear.

The surveys of relative sea level rates of rise global or local by many organizations as Permanent Service for Mean Sea Level (PSMSL) or National Oceanic and Atmospheric Administration (NOAA) may be used to evaluate the acceleration by using the relative sea level rates of rise computed for the same tide gauge at two different times.

As also reported elsewhere, the latest PSMSL "Table of Relative Mean Sea Level Secular Trends derived from PSMSL RLR Data" update 14-Feb-2014 ([www.psmsl.org](http://www.psmsl.org))

proposes the relative rates of rise computed for 560 tide gauges of variable record length (maximum 183, minimum 21, average 56.5 years) with the more recent, shortest tide gauges collected mostly in areas of subsidence and a strongly non-uniform geographical coverage.

The use in different times of different populations of tide gauges of different length, different rates of subsidence or uplift, and different parameters of the oscillations is what permits the false claim the sea level have been accelerating over the last decades by cherry picking when actually all the long term tide gauges of the world have been on average acceleration free.

The average relative rate of rise of the 560 tide gauges is  $1.04 \pm 0.45$  mm/year, but this number has very little significance. By only using the 170 tide gauges of PSMSL having length more than 60 years at the present time, the average relative rate of rise is  $0.25 \pm 0.19$  mm/year. If we want to study the changes in the rate of rise of sea levels over the satellite altimeter era, we do not have to consider the 100 tide gauges of PSMSL having length more than 80 years at the present time are 100, i.e. more than 60 years of length 20 years ago, and the average rate of rise for them is  $0.24 \pm 0.15$  mm/year. For these tide gauges, the rate of rise has been moving up and down over the last 20 years without any sign of globally positive or negative accelerations.

In additions of being acceleration free, these tide gauges are on average more subjected to subsidence than uplift, as suggested by the nearby GPS dome velocities by the Système d'Observation du Niveau des Eaux Littorales (SONEL) ([www.sonel.org](http://www.sonel.org)). Therefore the worldwide tide gauge signals suggest slow rising seas without any acceleration and with a significant component of subsidence.

The result of this synthetic analysis may be complemented by the analysis through equations (1) and (2) of the long term sea level time series. All the long term tide gauges exhibit pretty much the same pattern. Therefore, we select here the Sydney and San Diego tide gauges, on the west and east shores of the Pacific, in the southern and northern hemisphere.

Figures 1 and 2 present the mean sea level measured in Sydney and San Diego, plus the results obtained by replacing the measured data with a fitting with a line and multiple sines. Equations (1) and (2) are applied to both time series to show what natural oscillation is and what is noise. The figures also present the vertical position and the subsidence rate of inland GPS domes nearby the tide gauges. Application of equations (1) and (2) to the perfectly oscillating zero acceleration time series may return positive or negative accelerations depending on the time window.

In Figure **a**) is the classic trend computation (from [tidesandcurrents.noaa.gov/sltrends/](http://tidesandcurrents.noaa.gov/sltrends/)). The standard error or the 95% confidence interval is only a measure of the linear fitting error. The “true” relative rate of rise is not the computed value  $\pm$  the standard error or the 95% confidence interval. With short and incomplete records the computed value may be very far from the legitimate value. Other measurement issues, including variable subsidence at the tide gauge or relocation of the tide gauge or inaccurate levelling, may also bias the result.

In Figure **b**) is the measured monthly averaged mean sea levels and the fitted values from equation (3). The 36 months moving averaged are superimposed. The perfectly not accelerating model reproduces quite well the experimental evidence even if the experimental evidence is much more complex and the noise of the measurement is significant.

177 In Figure **c)** is the same monthly averaged mean sea levels of figure **b)** but de-trended,  
178 i.e. the monthly values minus their linear trend values.  
179

180 In Figure **d)** is the SLR computed from the measured and the fitted data over the last 20  
181 years. Over the time window 1993 to present, the measured SLR of Sydney is slightly  
182 increasing since 1999, while the measured SLR of San Diego is slightly decreasing since  
183 same year. Before that time, the trend was inverted, as a result of oscillations that are not in  
184 phase. Same pattern is shown by the fully periodical fitting. This is the only result of interest  
185 to assess the effect of global warming, and clearly having a more or less accurate model (3)  
186 has no impact on the conclusion.  
187

188 In Figure **e)** is the present SLR computed from the measured and the fitted data by using  
189 different record length. Unfortunately, the long tide gauges records having more than 100  
190 years of data are not too many, and in many cases SLR are computed by using short record  
191 lengths. With short record lengths the computed SLR differ considerably from the legitimate  
192 long term SLR. The measured 20 years SLR for Sydney is more than 5 times the correct  
193 value, while the measured 20 years SLR of San Diego is more than 10 times smaller.  
194

195 Even if many papers have wrongly claimed the hot spot of positive but never the cold  
196 spot of negative acceleration, this conclusion is only the result of cherry picking the  
197 information between a valley and a peak of an oscillation rather than between a peak and a  
198 valley. The pattern proposed in Figure **e)** is only the result of the periodicities, amplitudes,  
199 phases of the oscillations and the time window. Same pattern is shown by the not  
200 accelerating fitting.  
201

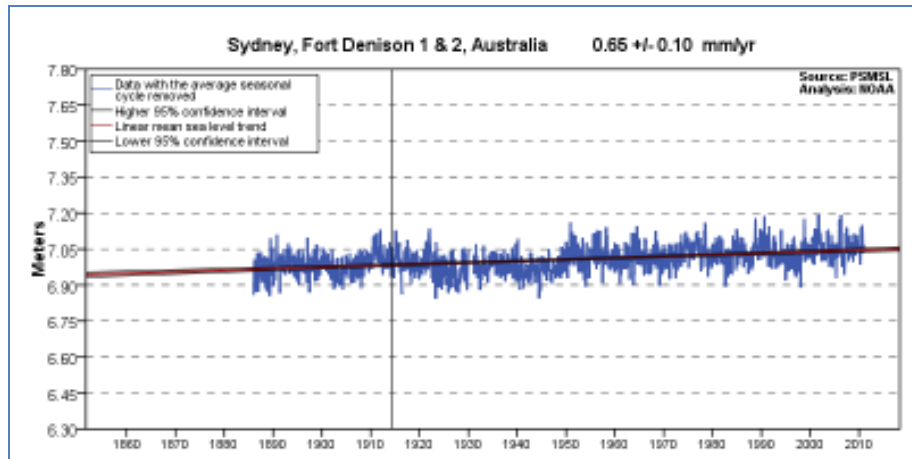
202 In Figure **f)** is the subsidence trend of GPS domes nearby the tide gauges (from  
203 [www.sonel.org](http://www.sonel.org)). This unfortunately not very accurate result suggests a subsidence rate very  
204 close to the relative rate of rise of sea levels for both Sydney and San Diego for a close to  
205 zero absolute rate of rise in both locations. The vertical velocity of the Sydney SYDN GPS  
206 dome is  $-0.89 \pm 0.65$  mm/year. Subsidence velocity of GPS domes nearby the San Diego tide  
207 gauge are  $-1.65 \pm 0.41$  mm/year (Point Loma 3, PLO3) and  $-3.23 \pm 0.17$  mm/year (Point Loma  
208 5, PLO5).

209 Figures 3 and 4 are the periodogram of the measured and fitted sea level patterns in  
210 Sydney and San Diego. Images **a)** and **b)** and data of **c)** are obtained by Wessa P. (2012).

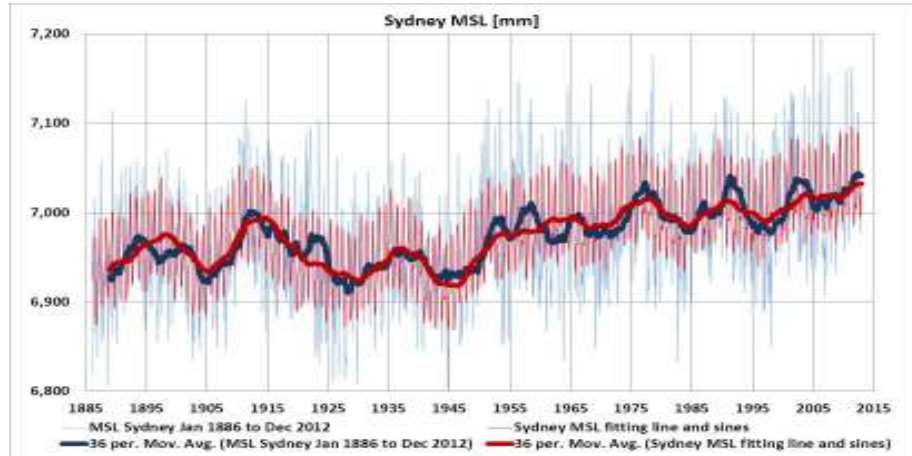
211 In Figure **a)** is the periodogram spectrum vs. frequency (in  $\text{months}^{-1}$ ) of the measured  
212 monthly average mean sea levels while in Figure **b)** is the periodogram spectrum vs.  
213 frequency (in  $\text{months}^{-1}$ ) of the monthly average mean sea levels from the fitting with a line  
214 and sines. The measured values have a very different signature, with the fitted values  
215 obviously evidencing the simulated periodicities.

216 In figure **c)** is the periodogram spectrum vs. period (in months) of the measured and fitted  
217 monthly averages. In case of San Diego, the record length is smaller, and the longer  
218 periodicity is consequently less well evidenced than in Sydney. To properly compute a  
219 periodicity, the record length must be many times the period length and this is unfortunately  
220 never the case.

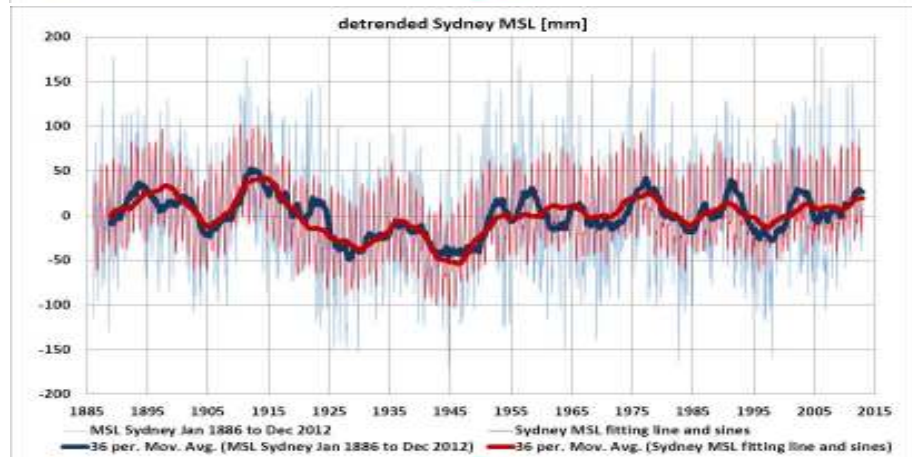
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a



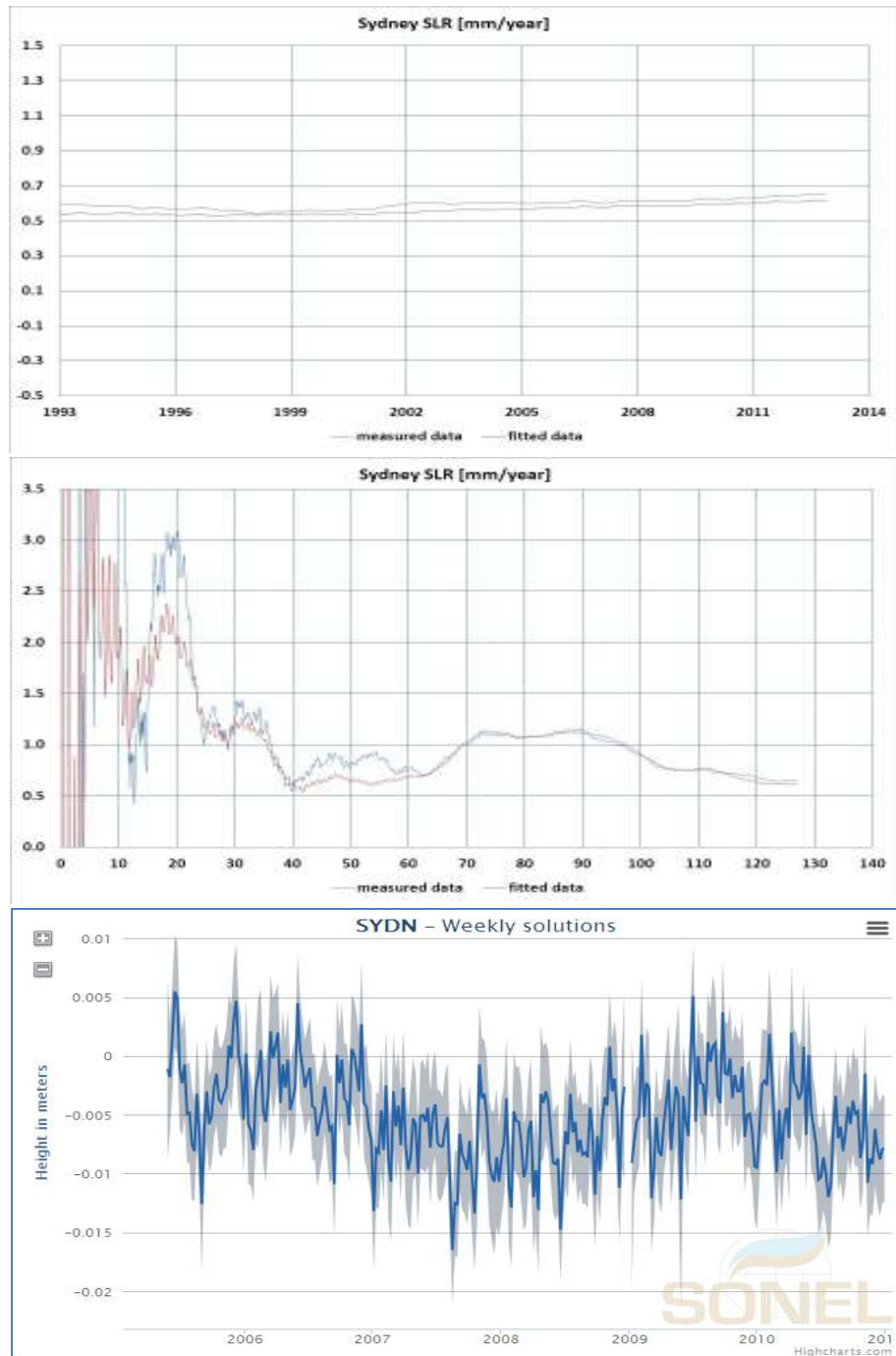
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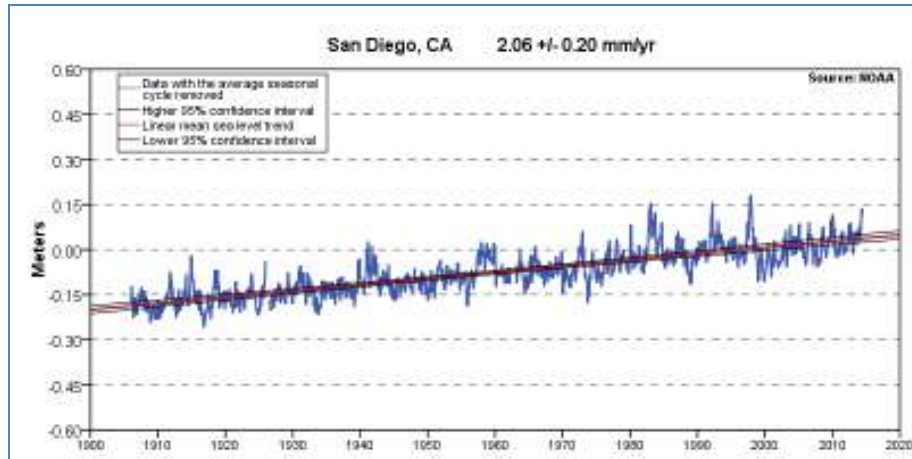
**Fig. 1 – continues - Measured and fitted sea level patterns in Sydney.**

a) classic trend computation (from [tidesandcurrents.noaa.gov/sltrends/](http://tidesandcurrents.noaa.gov/sltrends/) ). Relative sea level velocity is  $+0.65 \pm 0.10$  mm/year; b) measured and fitted (equation (3)) monthly average mean sea levels; c) detrended monthly average mean sea levels; d) SLR over the last 20 years.

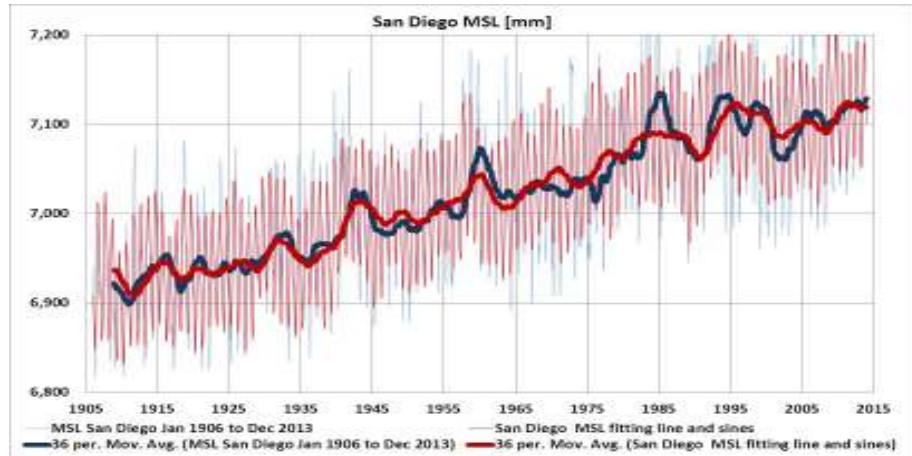


**Fig. 1 – continued - Measured and fitted sea level patterns in Sydney.**

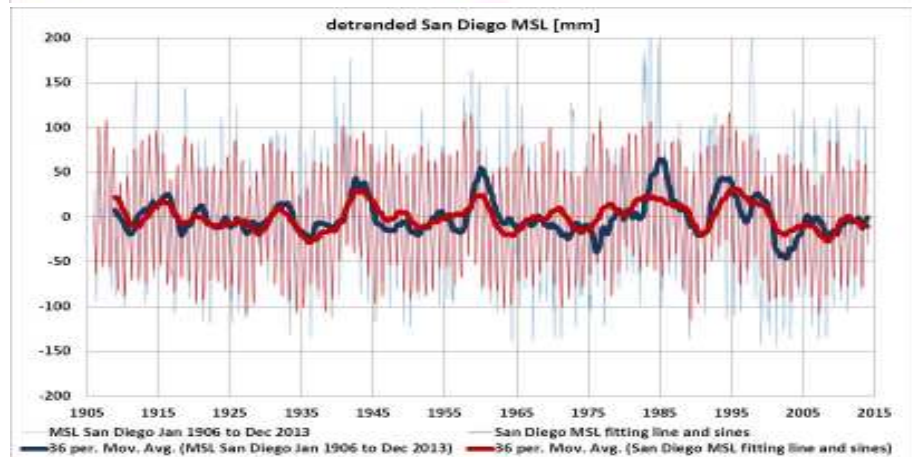
e) present SLR by using different record lengths; f) GPS velocity nearby the tide gauge (from [www.sonel.org](http://www.sonel.org)). Subsidence velocity is  $-0.89 \pm 0.65$  mm/year.



a



b

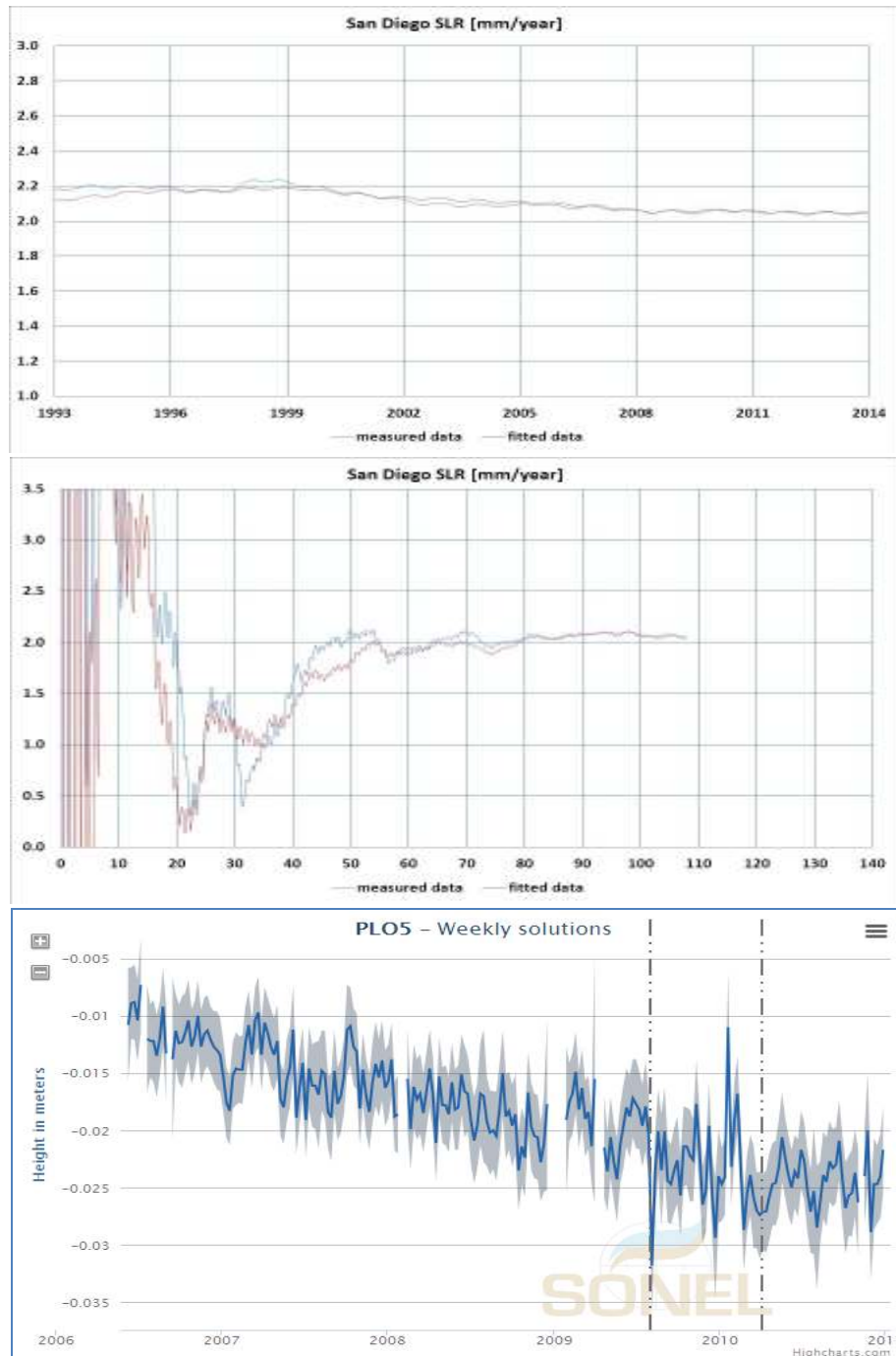


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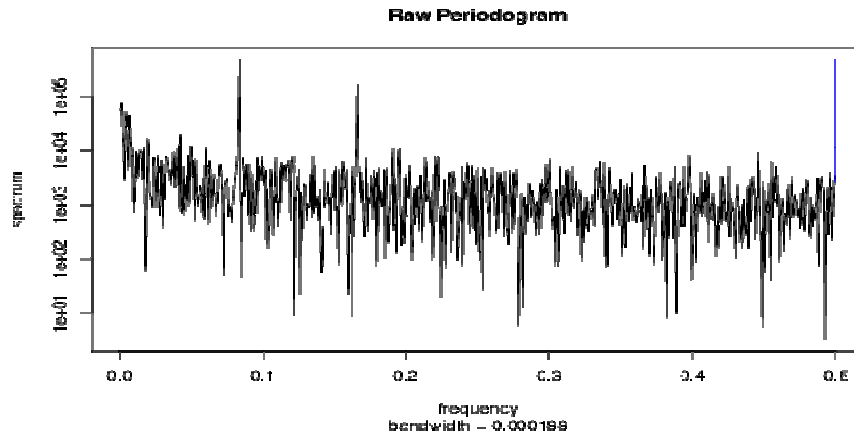
**Fig. 2 – Continues - Measured and fitted sea level patterns in San Diego.**

a) classic trend computation (from [tidesandcurrents.noaa.gov/sltrends/](http://tidesandcurrents.noaa.gov/sltrends/) ). Relative sea level velocity is  $+2.06 \pm 0.23$  mm/year; b) measured and fitted (equation (3)) monthly average mean sea levels; c) detrended monthly average mean sea levels; d) SLR over the last 20 years.

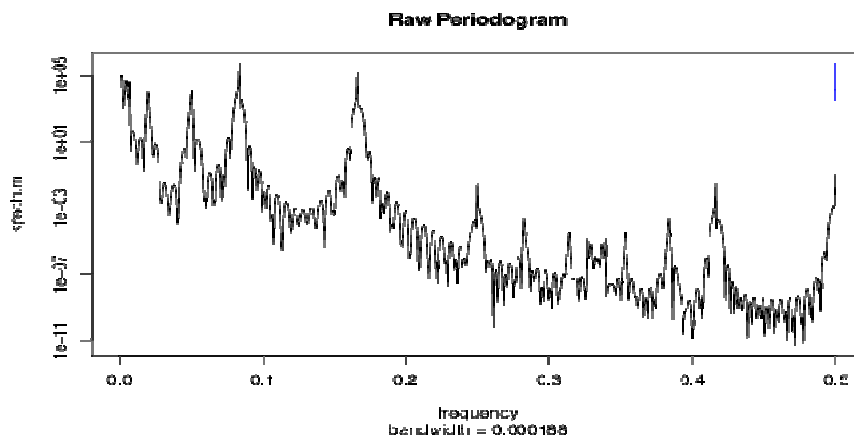




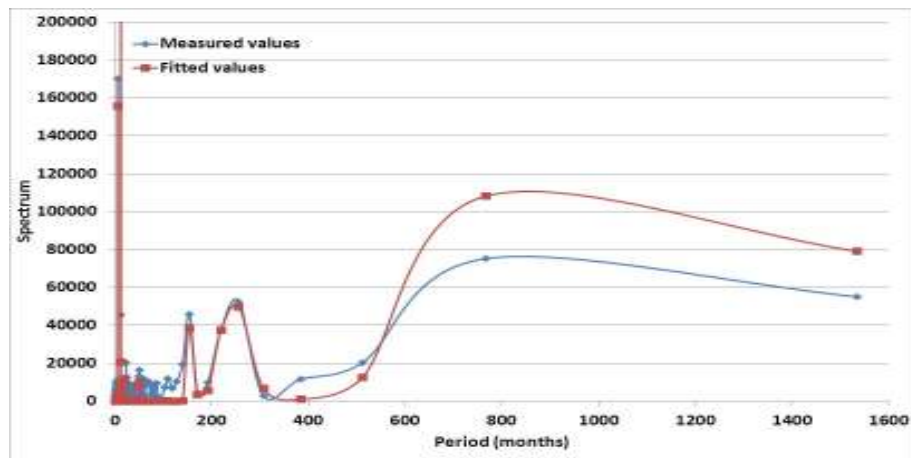
**Fig. 2 – Continued - Measured and fitted sea level patterns in San Diego.**  
 e) present SLR by using different record lengths; f) GPS velocity nearby the tide gauge (from [www.sonel.org](http://www.sonel.org)). Subsidence velocities of nearby domes are  $-1.65 \pm 0.41$  mm/year (Point Loma 3, PLO3) and  $-3.23 \pm 0.17$  mm/year (Point Loma 5, PLO5).



a

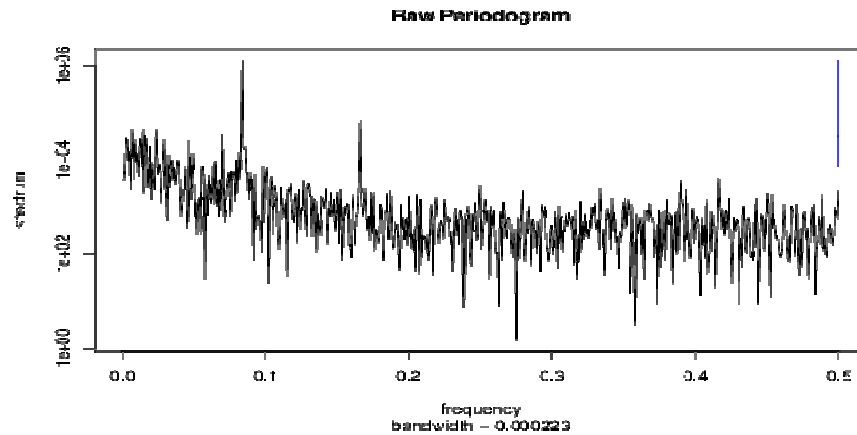


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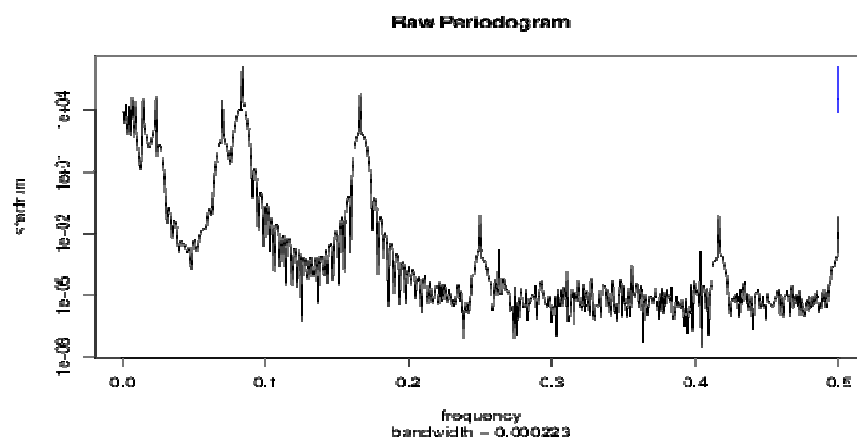


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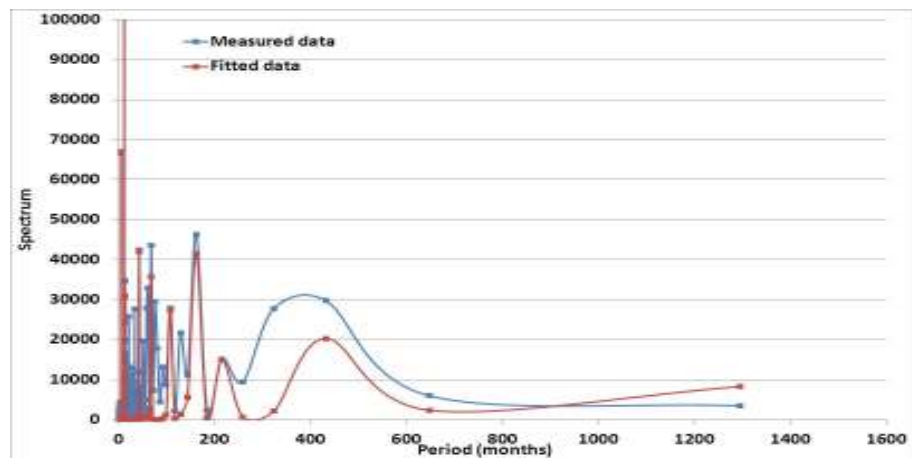
**Fig. 3 – periodogram of the measured and fitted sea level patterns in Sydney.**  
a) periodogram spectrum vs. frequency (in months<sup>-1</sup>) of the measured monthly average mean sea levels; b) periodogram spectrum vs. frequency (in months<sup>-1</sup>) of the monthly average mean sea levels from the fitting with a line and sines; c) periodogram spectrum vs. period (in months) of the measured and fitted monthly averages. Images a) and b) and data of c) are obtained by Wessa P. (2012).



a



b



c

**Fig. 4 – periodogram of the measured and fitted sea level patterns in San Diego.**  
a) periodogram spectrum vs. frequency (in months<sup>-1</sup>) of the measured monthly average mean sea levels; b) periodogram spectrum vs. frequency (in months<sup>-1</sup>) of the monthly average mean sea levels from the fitting with a line and sines; c) periodogram spectrum vs. period (in months) of the measured and fitted monthly averages. Images a) and b) and data of c) are obtained by Wessa P. (2012).

#### 4. DISCUSSION

The issue raised by Foster & Brown (2014) does not have any effect on the above conclusions. The oscillations of sea levels are not certainly perfectly sinusoidal and the sea level forcings are certainly many. Clearly, by using different periodic functions that are not exactly sinusoidal and by increasing the number of functions adopted for a fitting like (3), the determination of the periodicities of the oscillations may certainly provide slightly different results. However, this is irrelevant in the optic of the debate on the presence or absence of acceleration in the sea levels.

The linear and sinusoidal models, equation (1) and equation (3) respectively, can be fit by using least squares routines. To obtain a good fit for the sinusoidal (nonlinear) model, least squares routines may require good starting values for the constant, the amplitude, and the periodicity and different approaches may provide slightly different results. This has however not appreciable influence on the results of sea level rise. As with any statistical model, the fit is subjected to graphical and quantitative techniques of model validation up to satisfactory accuracy.

The measured sea level time series suffer of significant inaccuracies difficult or impossible to quantify. This is why the standard practice is to linearly fit the available monthly average mean sea level data mentioning the length and percentage of gaps in the record and the existence of levelling information about a datum. This gives a rate of rise of sea levels and the uncertainty in that value. If the levelling is accurate and the time span of data exceed the 60 years with minimal gaps, then the estimation of the rate of rise is reliable.

In sea levels there are many oscillations, with periodicities from hours to decades very well evidenced in the tide gauge records. The “*traditional*” analysis of sea levels (see the surveys by PSMSL, NOAA and other major players) is based on the linear fitting of the monthly average mean sea levels. The linear fitting of yearly average mean sea levels is less common but should not return average rates of rise that far. What is important is to linearly fit a time series having length much larger than the periodicity of the longest oscillation detected. Short tide gauge records should not be used to infer any trend.

The uncertainties of the estimation are generally significant and very difficult to be estimated. In the best cases, the tide gauge is periodically levelled versus a datum and every change of the instrument or relocation is carefully monitored to avoid biases. Unfortunately, the absolute tide gauge position is only known since very few years and only in very few locations with accuracy still far from the acceptable. However, at present there is no better measure of sea levels than the tide gauges. When everything has been done properly to avoid biases, there may still be the issue of missing data (gaps). Clearly, the reliability of a sea level rise estimation reduces the more are the gaps. Somebody as PSMSL and NOAA only use the measured data with gaps. We use either same approach or we do use a fitting with a line and multiple sines to fill the gaps iteratively. As a non-linear fitting depends on the first guesses of the parameters involved, uncertainties are either way substantial. The total length of the record and the percentage of gaps are two parameters that should be stated close to the rate of rise estimation to give an idea of the reliability of the estimation.

#### 5. CONCLUSION

In view of the only +0.25 mm/year of the present relative rate of rise at the acceleration free worldwide average tide gauge by classic, simple methods, with an overwhelming

contribution by subsidence, there is no reason to question how accurate may be the estimation of the multi-decadal periodicities to void the assessment of the velocity and acceleration of sea levels very far from the climate model predictions.

If the sea levels have to rise of 1 meter by 2100 and not of only 21.5 millimeters at the worldwide average tide gauge, there is a problem of orders of magnitude difference in the sea levels computed (by climate models) and measured (by tide gauges).

The best data we do have for sea levels is the one included in the Permanent Service on Mean Sea Level (2014) data base that is everything but perfect. The analysis of these data are however much better than any philosophical assumption even if popular these days (a theory not validated by experiments is philosophy and not science).

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376 **COMPETING INTERESTS**

377

378 The author has no financial and personal relationships with other people or organizations  
379 that could inappropriately influence (bias) their work.

380

381 **AUTHOR'S CONTRIBUTION**

382

383 All work, thoughts, interpretations and illustrations are done by the author.