# Modeling and Optimization of Operational Costs of Nissan Urvan Vehicles of a Fleet Operator 

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## Case Study


#### Abstract

This study focused on Modeling and Optimization of the operational costs of Nissan Urvan Vehicles of a fleet operator in Anambra State Nigeria. The special design used to fit a second order model needed to optimize the operational costs of Nissan Urvan Vehicles was Box - Behnken design while response surface method (RSM) was used to model and optimize performance characteristics of the vehicles. The response function of the second order model is best characterized by multivariate power equation. Ten (10) years operation data were collected from two sources, namely primary and secondary sources. The primary source of data was from the workshop manager and the statistical office of the company, and from Metrological Institute of Nigeria. The secondary source of data was from Books consulted at different Libraries. The outcome of the analysis of variance (ANOVA) for RSM optimization of operational costs of Nissan Urvan vehicles showed that all the control factors are significant except factors (B, C, D) of replacement costs.From the result of the


[^0]income generated at optimum condition and the sum of the maintenance \& replacement costs compared, by the year 2013 the income generated is less than the sum of maintenance \& replacement costs. It was observed that the operation of the transportation system is economical for a period of 8 years (from 2005 - 2012), where the income generated is more than the maintenance \& replacement costs.It is hereby recommended that response surface model should be deployed for the operation analysis of the case study company vehicles to enhance efficient utilization and profitability.

Keywords: Nissan Urvan vehicles; operational costs; response surface model; numerical optimization.

## 1. INTRODUCTION

The design life of most vehicles requires periodic maintenance. Failure to perform maintenance activities intended by the equipment's designer shortens the operating life of the equipment (Abdul, 2011). Vehicles and equipment are subject to deterioration due to their use and exposure to environmental conditions as a result of wear and tear of parts in relative motion and improper lubrication of the sliding parts. Maintenance is necessary to enhance utilization of vehicles with minimum cost of stoppage and repair. If deterioration and breakdown are not checked they may render the vehicles unserviceable, therefore, it is necessary to attend to them from time to time, repair and recondition them so as to enhance their life economically and protect them from failure (Goldberg et al, 2004). This has brought the role of maintenance and replacement as an important activity in the transportation industries (Latham, 2008). Maintenance is defined as the combination of activities to restore the component or equipment to a state in which it can perform its designated functions (Duffuaa et al, 2001). Every vehicle requires maintenance even if it is best designed; the maintenance must be done at such a period when it will have least disruptions of service, therefore, vehicles, machines undergo maintenance when not in use or their use may be postponed without affecting service and operation (Clarotti et al, 2004). However, in reality most of the equipment failures are influenced not only by the internal factor (agetime usage) but also by the external factor. The external factors would be the effects of the environment (dust, humidity, precipitation, temperature and heat), human skills, product types and maintenance activities. The timely maintenance of vehicles in the fleet is one of the fundamental programs that serve as a backbone of a successful transport system (Gertsbalch, 1997). Vehicle maintenance expenses usually increase as the age of a vehicle advances thereby triggering replacement. The vehicles are
subject to breakdowns and deterioration therefore, maintenance policy can be beneficial in order to prevent failures during operation (Steven, 2009).Besides, vehicle maintenance is an important service function of an efficient operational/productive system. It helps in maintaining and increasing the operational efficiency of the transport facilities and thus contributes to increase in revenue by reducing the operating costs and increasing the effectiveness of production (Zeqing and Price, 2006).Conversely, poorly maintained vehicles may lead to more frequent parts failures, poor utilization and delayed operation schedules. Also, poor maintenance may mean more frequent vehicle replacement because of shorter life. For many asset-intensive industries the maintenance costs are a significant portion of the operational costs, the maintenance expenditure accounts for $20-50 \%$ of the service cost for the industry depending on the level (age) of the equipment (Parida, 2007).

Prior to this study, the case company was challenged with high cost of maintaining company's vehicles which reduces and generally affect the total net profit of the company. However, this research work is geared towards optimization of the operational costs of Nissan Urvan vehicles of the case company by the application of response surface method which is best characterized by multivariate power law model (Chapra and Canale, 2006). This would help in making an optimal replacement policy so that a particular vehicle is replaced when it has reached its optimum service.It would also help the company to prevent losses by making the proper decisions based on relevant information.

Although, many approaches and models have been used in the past to analyze the operational costs of transportation industries, but they could not be used widely to fit second order model to the response surface and were not able to display the extent of the significance of the control factors on the yield (Amponsah,
2006). With these proposed model an optimal replacement policy can be made so that a particular vehicle is replaced when it has reached its optimum service. The accomplishment of the response surface method for automobile replacement policy stated would assist the case study company and other transport service providers nationwide to better access and manage their vehicles that need particularly maintenance and replacement. The creation of a more effective equipment replacement system would be of tremendous benefit both in potential labor and vehicle maintenance Naira savings. Finally, the study would be used as a guide for organizations to improve or promote their maintenance strategies and also benefit future researchers in this field on how to adopt maintenance measures. The objective of this study is to optimize the operational costs of Nissan Urvan vehicles of a fleet operator using response surface method.

## 2. MATERIALS AND METHODS

### 2.1 Data Collection

In this study, data on the type and number of vehicles, maintenance costs, replacement costs and income generated from 2005 to 2014 were collected from the maintenance workshop of the company, while data on environmental factors were obtained from the Metrological Institute of

Nigeria. The data obtained were presented in Table 1.

### 2.2 Fitting a Second Order Model to the Data Collected

In this study the data obtained from the statistical office of the fleet operator is linearized on the assumption that the sample results follow a power law model of the form:
$Y=a_{0} A^{a 1} B^{a 2} C^{a 3} \ldots N^{a n} \quad$ (Chapra and Canale, 2006).
and that the response surface is optimized by a second order polynomial equation stated as:
$Y=\beta_{0}+\sum_{i=1}^{q} \beta_{i} x_{i}+\sum_{i=1}^{q} \beta_{i i} x_{i}^{2}+\sum_{i=1}^{q-1} \sum_{j=2}^{q} \beta_{i j}+\varepsilon$
Where, $Y$ is the predicted response (dependent variable),
q is the number of factors (independent variables),
$X_{i}$ is the input factors ( $\mathrm{i}=1,2$ etc),
$\beta_{0}$ is the constant coefficient, and
$\beta_{\mathrm{i}}, \beta_{\mathrm{ij}}$ and $\beta_{\mathrm{ii}}$ are the coefficients of linear, interaction and quadratic terms respectively.

Table 1. Environmental factors and data collected from Nissan Urvan fleet operator's office Please insert all table data in standard MS word table format bellow

| Year | Factor A <br> Dist. $($ Km $)$ | Factor B <br> Pr eci. $($ Cubic $)$ | Factor C <br> Temp. $\left({ }^{\circ}\right.$ C) | Factor D <br> Re lative <br> humidity | Ma int. <br> Cost <br> $(\# x 1000)$ | Re place. <br> Cost <br> $(\# x 1000)$ | Income <br> generated <br> $(\# x 1000)$ |
| :--- | :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| 2005 | 101616 | 1620 | 29.2 | 148 | 1969 | 1992 | 9807.30 |
| 2006 | 102784 | 1500 | 28.5 | 156.9 | 2250 | 2240 | 9782.40 |
| 2007 | 105120 | 1650.3 | 28.96 | 176.98 | 2520 | 2400 | 9660.00 |
| 2008 | 113296 | 1507 | 28.15 | 159.56 | 2815 | 2500 | 9515.00 |
| 2009 | 116800 | 1579.1 | 28.3 | 126.2 | 3030 | 2568 | 9020.00 |
| 2010 | 117384 | 1506.6 | 27.8 | 122.65 | 3240 | 2681 | 8850.00 |
| 2011 | 117968 | 1695.4 | 28.85 | 129.7 | 3360 | 2705 | 8610.00 |
| 2012 | 118552 | 1662 | 27.9 | 148 | 3590 | 2805 | 8489.70 |
| 2013 | 119720 | 2294.7 | 28.3 | 122.65 | 3995 | 2856 | 8340.00 |
| 2014 | 120304 | 1695 | 24.4 | 129.68 | 4005 | 2943 | 8300.00 |

Km=kilometer, ${ }^{\circ} \mathrm{C}=$ degree Celsius, Dist.$=$ Distance, Temp. $=$ Temperature

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For four factors, three level design equation (1) reduces to:

$$
\begin{equation*}
Y=a_{0} A^{a 1} B^{a 2} C^{a 3} D^{a 4} \tag{3}
\end{equation*}
$$

And equation (2) expanded to:

$$
\begin{align*}
& Y=\beta_{0}+\beta_{1} x_{1}+\beta_{2} x_{2}+\beta_{3} x_{3}+\beta_{4} x_{4}+\beta_{11} x_{1}{ }^{2}+ \\
& \beta_{22} x_{2}{ }^{2}+\beta_{33} x_{3}{ }^{2}+\beta_{44} x_{4}{ }^{2}+\beta_{12} x_{1} x_{2}+\beta_{13} x_{1} x_{3} \\
& +\beta_{14} x_{1} x_{4}+\beta_{23} x_{2} x_{3}+\beta_{24} x_{2} x_{4}+\beta_{34} x_{3} x_{4} \tag{4}
\end{align*}
$$

The coefficient parameters were estimated by linearizing the data of maintenance cost, replacement cost and income generated of Table 1 and using regression as analysis tool for evaluating transformed log data of input
parameters presented in Table 2, 3 and 4, and expressed them as power law models of the form of equation (3).
$\mathrm{Y}_{\mathrm{m} \text { mosto }}=2.805336072 \mathrm{D}^{0.274461545}(5) \mathrm{E}-14 \mathrm{~A}^{3.183453789} \mathrm{~B}^{0.4665364202} \mathrm{C}^{-}$ ${ }^{0.80574072} D^{0.274461545}(5)$
$Y_{\text {rcost }}=6.418851538 \mathrm{E}-07 \mathrm{~A}^{1.813623751} \mathrm{~B}^{0.139777175} \mathrm{C}^{-}$
${ }^{0.378185139} \mathrm{D}^{0.247298984}(6)$
$\mathrm{Y}_{\text {income }}$ gen. $=22976659.8 \mathrm{~A}^{-0.668996929} \mathrm{~B}^{-0.147041359} \mathrm{C}$ ${ }^{0.240003793} \mathrm{D}^{0.046911726}(7)$

Where, factors $A, B, C$ and $D$ are the distance covered, precipitation, temperature and relative humidity respectively.

Table 2. Log transformed data for maintenance cost
Please insert all table data in standard MS word table format bellow

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| Factor | Factor | Factor | Factor | Response | Log A | Log B | Log C | LogD | LogY |
| A | $B$ | $C$ | $D$ | $Y$ |  |  |  |  |  |
| 101616 | 1620 | 29.2 | 148 | 1969 | 5.007 | 3.2095 | 1.4654 | 2.1703 | 3.2942 |
| 102784 | 1500 | 28.5 | 156.9 | 2250 | 5.012 | 3.1761 | 1.4548 | 2.1956 | 3.3522 |
| 105120 | 1650.3 | 28.96 | 176.98 | 2520 | 5.0217 | 3.2176 | 1.4618 | 2.2479 | 3.4014 |
| 113296 | 1507 | 28.15 | 159.56 | 2815 | 5.0542 | 3.1781 | 1.4495 | 2.2029 | 3.4495 |
| 116800 | 1579.1 | 28.3 | 126.2 | 3030 | 5.0674 | 3.1984 | 1.4518 | 2.1011 | 3.4814 |
| 117384 | 1506.6 | 27.8 | 122.65 | 3240 | 5.0696 | 3.1780 | 1.4440 | 2.089 | 3.5105 |
| 117968 | 1695.4 | 28.85 | 129.7 | 3360 | 5.0718 | 3.2293 | 1.4601 | 2.1129 | 3.5263 |
| 118552 | 1662 | 27.9 | 148 | 3590 | 5.0739 | 3.2206 | 1.4456 | 2.1703 | 3.5551 |
| 119720 | 2294.7 | 28.3 | 122.65 | 3995 | 5.0782 | 3.3607 | 1.4518 | 2.0887 | 3.6015 |
| 120304 | 1695 | 24.4 | 129.68 | 4005 | 5.0803 | 3.2292 | 1.3874 | 2.1129 | 3.6026 |

Table 3. Log transformed data for replacement cost
Please insert all table data in standard MS word table format bellow

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| Factor | Factor | Factor | Factor | Re sponse | $\log A$ | $\log B$ | $\log C$ | $\log D$ | $\log Y$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| A | $B$ | $C$ | $D$ | $Y$ |  |  |  |  |  |
| 101616 | 1620 | 29.2 | 148 | 1992 | 5.007 | 3.2095 | 1.4654 | 2.1703 | 3.2993 |
| 102784 | 1500 | 28.5 | 156.9 | 2240 | 5.012 | 3.1761 | 1.4548 | 2.1956 | 3.3502 |
| 105120 | 1650.3 | 28.96 | 176.98 | 2400 | 5.0217 | 3.2176 | 1.4618 | 2.2479 | 3.3802 |
| 113296 | 1507 | 28.15 | 159.56 | 2500 | 5.0542 | 3.1781 | 1.4495 | 2.2029 | 3.3979 |
| 116800 | 1579.1 | 28.3 | 126.2 | 2568 | 5.0674 | 3.1984 | 1.4518 | 2.1011 | 3.4096 |
| 117384 | 1506.6 | 27.8 | 122.65 | 2681 | 5.0696 | 3.1780 | 1.4440 | 2.089 | 3.4283 |
| 117968 | 1695.4 | 28.85 | 129.7 | 2705 | 5.0718 | 3.2293 | 1.4601 | 2.1129 | 3.4322 |
| 118552 | 1662 | 27.9 | 148 | 2805 | 5.0739 | 3.2206 | 1.4456 | 2.1703 | 3.4479 |
| 119720 | 2294.7 | 28.3 | 122.65 | 2856 | 5.0782 | 3.3607 | 1.4518 | 2.0887 | 3.4558 |
| 120304 | 1695 | 24.4 | 129.68 | 2943 | 5.0803 | 3.2292 | 1.3874 | 2.1129 | 3.4688 |

Table 4. Log transformed data for income generated
Please insert all table data in standard MS word table format bellow

| Factor | Factor | Factor | Factor | Re sponse | $\log A$ | $\log B$ | $\log C$ | $\log D$ | $\log Y$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $A$ | $B$ | $C$ | $D$ | $Y$ |  |  |  |  |  |
| 101616 | 1620 | 29.2 | 148 | 1992 | 5.007 | 3.2095 | 1.4654 | 2.1703 | 3.9915 |
| 102784 | 1500 | 28.5 | 156.9 | 2240 | 5.012 | 3.1761 | 1.4548 | 2.1956 | 3.9904 |
| 105120 | 1650.3 | 28.96 | 176.98 | 2400 | 5.0217 | 3.2176 | 1.4618 | 2.2479 | 3.9850 |
| 113296 | 1507 | 28.15 | 159.56 | 2500 | 5.0542 | 3.1781 | 1.4495 | 2.2029 | 3.9784 |
| 116800 | 1579.1 | 28.3 | 126.2 | 2568 | 5.0674 | 3.1984 | 1.4518 | 2.1011 | 3.9552 |
| 117384 | 1506.6 | 27.8 | 122.65 | 2681 | 5.0696 | 3.1780 | 1.4440 | 2.089 | 3.9469 |
| 117968 | 1695.4 | 28.85 | 129.7 | 2705 | 5.0718 | 3.2293 | 1.4601 | 2.1129 | 3.9350 |
| 118552 | 1662 | 27.9 | 148 | 2805 | 5.0739 | 3.2206 | 1.4456 | 2.1703 | 3.9289 |
| 119720 | 2294.7 | 28.3 | 122.65 | 2856 | 5.0782 | 3.3607 | 1.4518 | 2.0887 | 3.9212 |
| 120304 | 1695 | 24.4 | 129.68 | 2943 | 5.0803 | 3.2292 | 1.3874 | 2.1129 | 3.9191 |


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Table 5. Design matrix of Box-Behnken design for optimization of maintenance costs Please insert all table data in standard MS word table format bellow

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| Std. <br> order | Run <br> order | Distance | Precipitation | Temp. | Relative <br> humidity | Response <br> maintenance cost |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 23 | 1 | 110960 | 1500.00 | 26.8 | 176.980 | 2970.01 |
| 14 | 2 | 110960 | 2294.70 | 24.4 | 149.815 | 3729.47 |
| 3 | 3 | 101616 | 2294.70 | 26.8 | 149.815 | 2613.34 |
| 2 | 4 | 120304 | 1500.00 | 26.8 | 149.815 | 3670.10 |
| 8 | 5 | 110960 | 1897.35 | 29.2 | 176.980 | 3092.00 |
| 18 | 6 | 120304 | 1897.35 | 24.4 | 149.815 | 4415.72 |
| 26 | 7 | 110960 | 1897.35 | 26.8 | 149.815 | 3165.11 |
| 22 | 8 | 110960 | 2294.70 | 26.8 | 122.650 | 3273.18 |
| 11 | 9 | 101616 | 1897.35 | 26.8 | 176.980 | 2503.97 |
| 13 | 10 | 110960 | 1500.00 | 24.4 | 149.815 | 3060.03 |
| 27 | 11 | 110960 | 1897.35 | 26.8 | 149.815 | 3165.11 |
| 15 | 12 | 110960 | 1500.00 | 29.2 | 149.815 | 2647.79 |
| 10 | 13 | 120304 | 1897.35 | 26.8 | 122.650 | 3875.47 |
| 1 | 14 | 101616 | 1500.00 | 26.8 | 149.815 | 2144.24 |
| 21 | 15 | 110960 | 1500.00 | 26.8 | 122.650 | 2685.64 |
| 16 | 16 | 110960 | 2294.70 | 29.2 | 149.815 | 3227.05 |
| 25 | 17 | 110960 | 1897.35 | 26.8 | 149.815 | 3165.11 |
| 5 | 18 | 110960 | 1897.35 | 24.4 | 122.650 | 3231.25 |
| 9 | 19 | 101616 | 1897.35 | 26.8 | 122.650 | 2264.22 |
| 24 | 20 | 110960 | 2294.70 | 26.8 | 176.980 | 3619.76 |
| 19 | 21 | 101616 | 1897.35 | 29.2 | 149.815 | 2232.31 |
| 12 | 22 | 120304 | 1897.35 | 26.8 | 176.980 | 4285.82 |
| 20 | 23 | 120304 | 1897.35 | 29.2 | 149.815 | 3820.84 |
| 6 | 24 | 110960 | 1897.35 | 29.2 | 122.650 | 2795.95 |
| 17 | 25 | 101616 | 1897.35 | 24.4 | 149.815 | 2579.86 |
| 7 | 26 | 110960 | 1897.35 | 24.4 | 176.980 | 3573.39 |
| 4 | 27 | 120304 | 2294.70 | 26.8 | 149.815 | 4473.01 |

The power law models of Eqs. (5) - (7) were used to evaluate the design matrix of Box Behnken design and presented in Tables 5, 6 and 7 for maintenance, replacement and income generated respectively.

The regression model resulting from the evaluation of the design matrix of Box-Behnken design for maintenance cost is presented as equation (8) for uncoded factors. Also the test for statistical significance of the response model is presented as Table 8.

Table 6. Design matrix of Box-Behnken design for optimization of replacement cost
Please insert all table data in standard MS word table format bellow

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| Std. <br> order | Run <br> order | Distance | Precipitation | Temp. | Relative <br> humidity | Response <br> maintenance cost |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 23 | 1 | 110960 | 1500.00 | 26.8 | 176.980 | 2613.64 |
| 14 | 2 | 110960 | 2294.70 | 24.4 | 149.815 | 2757.82 |
| 3 | 3 | 101616 | 2294.70 | 26.8 | 149.815 | 2269.18 |
| 2 | 4 | 120304 | 1500.00 | 26.8 | 149.815 | 2904.24 |
| 8 | 5 | 110960 | 1897.35 | 29.2 | 176.980 | 2614.72 |
| 18 | 6 | 120304 | 1897.35 | 24.4 | 149.815 | 3109.61 |
| 26 | 7 | 110960 | 1897.35 | 26.8 | 149.815 | 2591.88 |
| 22 | 8 | 110960 | 2294.70 | 26.8 | 122.650 | 2533.20 |
| 11 | 9 | 101616 | 1897.35 | 26.8 | 176.980 | 2302.62 |
| 13 | 10 | 110960 | 1500.00 | 24.4 | 149.815 | 2598.71 |
| 27 | 11 | 110960 | 1897.35 | 26.8 | 149.815 | 2591.88 |
| 15 | 12 | 110960 | 1500.00 | 29.2 | 149.815 | 2428.08 |
| 10 | 13 | 120304 | 1897.35 | 26.8 | 122.650 | 2856.34 |
| 1 | 14 | 101616 | 1500.00 | 26.8 | 149.815 | 2138.26 |
| 21 | 15 | 110960 | 1500.00 | 26.8 | 122.650 | 2387.05 |
| 16 | 16 | 110960 | 2294.70 | 29.2 | 149.815 | 2576.74 |
| 25 | 17 | 110960 | 1897.35 | 26.8 | 149.815 | 2591.88 |
| 5 | 18 | 110960 | 1897.35 | 24.4 | 122.650 | 2555.86 |
| 9 | 19 | 101616 | 1897.35 | 26.8 | 122.650 | 2103.00 |
| 24 | 20 | 110960 | 2294.70 | 26.8 | 176.980 | 2773.66 |
| 19 | 21 | 101616 | 1897.35 | 29.2 | 149.815 | 2139.14 |
| 12 | 22 | 120304 | 1897.35 | 26.8 | 176.980 | 3127.48 |
| 20 | 23 | 120304 | 1897.35 | 29.2 | 149.815 | 2905.43 |
| 6 | 24 | 110960 | 1897.35 | 29.2 | 122.650 | 2388.03 |
| 17 | 25 | 101616 | 1897.35 | 24.4 | 149.815 | 2289.47 |
| 7 | 26 | 110960 | 1897.35 | 24.4 | 176.980 | 2798.47 |
| 4 | 27 | 120304 | 2294.70 | 26.8 | 149.815 | 3082.05 |

The regression model resulting from the evaluation of the design matrix of Box-Behnken design for replacement cost is stated as equations (9)for uncoded factors.Also the test for statistical significance of the response model is presented as Table 9.

The regression model equation for uncoded factors is presented in equation (10). Also, the test for statistical significance of the response model is presented as Table 10.

### 2.3 Optimization Plots

Optimization plot is a graphical representation of the dependent and independent variables at their optimal value settings. The optimization plots are presented in Figs. 1, 2 and 3. The optimal values of the factors were indicated in the plots in squared parentheses. The optimization plots showed the maximum predicted values of \#1,916,643.30 for maintenance cost, 1,971 , 390.00 for replacement cost and $\# 10,040,000.00$ for income generated. The optimized plot was obtained with the response surface optimizer of Minitab 16 software.
2.4 Model Validation

[^1]The fitted models were checked to ensure that they provide adequate approximations to the real systems. Unless the models show adequate fits, proceeding with the optimization of the fitted response surfaces is likely to give misleading results. The graphical optimization method (optimization plot) was used as a primary tool for optimization. The graphical techniques were validated using a numerical method. There are three optimization parameters namely maximum, minimum and target that define each desirability index, $\mathrm{d}_{\mathrm{i}}$. The desirability function $\mathrm{d}_{\mathrm{i}}$ is defined differently based on the objective of the response according to Relia Wiki (2013), and is expressed as:
(i) If the response is to be maximized, $\mathrm{d}_{\mathrm{i}}$ is defined as:

Where, T represents the target value of the $\mathrm{i}^{\text {th }}$ response ( the highest value) and

L represents the acceptable lower limit value for the response.
(ii) If the response is to be minimized, di is defined as:
$d_{i}= \begin{cases}\left(\frac{U^{1}-Y_{i}}{U-T}\right) & \begin{array}{l}Y_{i}<T \\ T \leq Y_{i} \leq U \\ Y_{i}>U\end{array}\end{cases}$
Where, U represents the acceptable upper limit of the response and $T$ is the smallest value.
(iii) For a specific target response value, $d_{i}$ is defined as:
$d_{i}= \begin{cases}\left(\begin{array}{l}\frac{Y_{i}^{0}-L}{T-L} \\ \frac{Y_{i}<L}{U-Y_{i}} \\ U-T\end{array}\right) & \begin{array}{l}T \leq Y_{i} \leq T \\ Y_{i}>U\end{array} \\ \end{cases}$

Table 7. Design matrix of Box-Behnken design for optimization of income generated

| Std. <br> order | Run <br> order | Distance | Precipitation | Temp. | Relative <br> humidity | Response income <br> generated |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 27 | 1 | 110960 | 1897.35 | 26.8 | 149.815 | 8889.55 |
| 4 | 2 | 120304 | 2294.70 | 26.8 | 149.815 | 8189.29 |
| 19 | 3 | 101616 | 1897.35 | 29.2 | 149.815 | 9624.49 |
| 15 | 4 | 110960 | 1500.00 | 29.2 | 149.815 | 9393.46 |
| 24 | 5 | 110960 | 2294.70 | 26.8 | 176.980 | 8712.29 |
| 11 | 6 | 101616 | 1897.35 | 26.8 | 176.980 | 9502.40 |
| 21 | 7 | 110960 | 1500.00 | 26.8 | 122.650 | 9116.12 |
| 1 | 8 | 101616 | 1500.00 | 26.8 | 149.815 | 9759.88 |
| 16 | 9 | 110960 | 2294.70 | 29.2 | 149.815 | 8824.23 |
| 13 | 10 | 110960 | 1500.00 | 24.4 | 149.815 | 8997.20 |
| 22 | 11 | 110960 | 2294.70 | 26.8 | 122.650 | 8563.69 |
| 6 | 12 | 110960 | 1897.35 | 29.2 | 122.650 | 8989.66 |
| 14 | 13 | 110960 | 2294.70 | 24.4 | 149.815 | 8451.97 |
| 7 | 14 | 110960 | 1897.35 | 24.4 | 176.980 | 8759.83 |
| 2 | 15 | 120304 | 1500.00 | 26.8 | 149.815 | 8717.56 |
| 8 | 16 | 110960 | 1897.35 | 29.2 | 176.980 | 9145.64 |
| 25 | 17 | 110960 | 1897.35 | 26.8 | 149.815 | 8889.55 |
| 23 | 18 | 110960 | 1500.00 | 26.8 | 176.980 | 9274.30 |
| 20 | 19 | 120304 | 1897.35 | 29.2 | 149.815 | 8596.63 |
| 26 | 20 | 110960 | 1897.35 | 26.8 | 149.815 | 8889.55 |
| 3 | 21 | 101616 | 2294.70 | 26.8 | 149.815 | 9168.45 |
| 9 | 22 | 101616 | 1897.35 | 26.8 | 122.650 | 9340.33 |
| 5 | 23 | 110960 | 1897.35 | 24.4 | 122.650 | 8610.43 |
| 10 | 24 | 120304 | 1897.35 | 26.8 | 122.650 | 8342.82 |
| 18 | 25 | 120304 | 1897.35 | 24.4 | 149.815 | 8233.98 |


| 12 | 26 | 120304 | 1897.35 | 26.8 | 176.980 | 8487.58 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| 17 | 27 | 101616 | 1897.35 | 24.4 | 149.815 | 9218.48 |
| The maintenance and replacement cost | maximum and minimum values of maintenance |  |  |  |  |  |
| responses were evaluated by minimisation | cost response in Table 5 for $Y_{i}>U$. |  |  |  |  |  |
| method while the generated income response |  |  |  |  |  |  |
| was evaluated by maximization method. | $1=\left(\frac{4,473.01-Y_{i}}{4,473.01-2,144.24}\right)$ |  |  |  |  |  |

By the evaluation of equation (12) for minimization at a desirability index of 1, with the Which gives $Y_{i}<2,144.24$


Fig. 1. Optimization plot for maintenance cost


Fig. 2. Optimization plot for replacement cost


Fig. 3. Optimization plot for income generated

From the optimization plot of Fig. 1, $Y_{i}=$ \#1,916.64. The result of the validation of the model is an adequate approximation of the result obtained from the optimization plot.

Similarly, the replacement cost response was evaluated with equation (12) for minimization at a desirability index of 1 , with the maximum and minimum values of replacement cost response in Table 6 for $Y_{i}>U$.

$$
1=\frac{3,127.48-Y_{i}}{3,127.48-2,103.00}
$$

Which gives $Y_{i}<2,103.00$
From the optimization plot of Fig. 2, $Y_{i}=$ \#1,971.39. The result of the validation of the model is an adequate approximation of the result obtained from the optimization plot.

By the evaluation of equation (11) for maximization at a desirability index of 1 , with the maximum and minimum values of income generated a response in Table 7 for $Y_{i}>T$.
$1=\frac{Y_{i}-8,189.29}{9,759.88-8,189.29}$
Which gives $Y_{i}>9,759.88$

From the optimization plot of Fig. 3, $Y_{i}=$ $\# 10,040.00$. The result of the validation of the model is an adequate approximation of the result obtained from the optimization plot.

## 3. RESULTS AND DISCUSSIONS

### 3.1 Response Surface Models Obtained from the Evaluation and Optimization of Maintenance, Replacement Costs and Income Generated

The response surface models are second order regression models with $\{(n+1)(n+2) / 2\}$ numbers of regression parameters, with $n$ being the number of factors. The regression parameters include the coefficients for main effects $A, B, C$ and $D$, coefficients for quadratic main effects $A^{2}, B^{2}, C^{2}$ and $D^{2}$ and the coefficients for two factors interaction effects $A B$, $A C, A D, B C, B D$ and $C D$ and a constant value.

For uncoded factors, the regression models for income are presented thus: maintenance, replacement and generated

$$
\begin{align*}
Y_{\text {most }}= & 3708.23-0.101076 A-0.862676 B+106.003 C-6.46065 D+8.92869 E-07 A^{2} \\
& -1.12127 E-04 B^{2}+3.26418 C^{2}-0.0143282 D^{2}+2.24767 E-05 A B-0.00275723 A C  \tag{8}\\
& +0.000168026 A D-0.0236410 B C+0.00144085 B D-0.176736 C D .
\end{align*}
$$

$$
\begin{equation*}
Y_{r \text { cost }}=-187.693+0.007 A+0.036 B-6.526 C+0.796 D+0.000 A^{2}-0.000 B^{2}+0.947 C^{2} \tag{9}
\end{equation*}
$$

$$
-0.011 D^{2}+0.000 A B-0.001 A C+0.000 A D-0.003 B C+0.000 B D-0.061 C D
$$

$$
\begin{align*}
Y_{\text {income gen. }} & =17296.9-0.1 A-1.8 B+203.2 C+7.0 D+0.0 A^{2}-0.0 B^{2}-1.2 C^{2} \\
& -0.0 D^{2}+0.0 A B-0.0 A C-0.0 A D-0.0 B C-0.0 B D+0.0 C D . \tag{10}
\end{align*}
$$

### 3.2 Test for Statistical Significance

The summary of the Analysis of variance (ANOVA) for RSM optimization for maintenance costs of Nissan Urvan vehicles is displayed in Table 8. The significance of each term in the model is represented by the $p$-value associated with the term. A term is not significant if $p$-value is greater than 0.05 . The value 0.05 indicates the significance level of the observed effects. The significance level is the probability of the observed significant effect being due to pure error.

The summary of the Analysis of variance (ANOVA) for RSM optimization for replacement costs of Nissan Urvan vehicles is illustrated in Table 9. The outcome of the analysis indicated that some control variables are significant while others are not.

The outcome of the Analysis of variance (ANOVA) for RSM optimization for Income Generation of Nissan Urvan vehicles is shown in Table 10. From the result obtained it could be observed that all the control factors, that is linear factors, square factors, interaction factors and
lack of fit are all highly significant. The degree of freedom in the regression model is fourteen. However, the analysis shows that the degree of freedom in linear factors is four, while the degree of freedom in square factors is also four. Finally, the degree of freedom in interaction factors is six. The ANOVA shows an excellent analysis of the data collected and what the data portrays.

Table 11 presented the income generated at optimum condition and the sum of the maintenance \& replacement costs. It was observed that by the year 2013 the income generated was less than the sum of maintenance \& replacement costs. Fig. 4 showed the chart of the combined plot of optimized income, and the non-optimized sum of maintenance and replacement costs against the operational period.

From the chart presented, it can be seen that by the year 2013 the income generated is less than the sum of maintenance \& replacement costs. This shows that the operation of the transportation system is economical for a period of 8 years (from 2005 - 2012), where the income generated is more than the maintenance \& replacement costs.

Table 8. Analysis of variance (ANOVA) for RSM optimization for Maintenance costs of Nissan Urvan vehicles
Please insert all table data in standard MS word table format bellow

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Table 9. Analysis of variance (ANOVA) for RSM optimization for replacement costs of Nissan Urvan vehicles
Please insert all table data in standard MS word table format bellow

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Table 10. Analysis of variance (ANOVA) for RSM optimization for income generation of Nissan Urvan vehicles
Please insert all table data in standard MS word table format bellow

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|  |  |  |  |  |  |  |
| Source | DF | Seq SS | Adj. SS | Adj. MS | $F$ | $P$ |
| Re grssion | 14 | 4510855 | 4510855 | 322204 | 184137.62 | 0.000 |
| Linear | 4 | 4493294 | 26388 | 6597 | 3770.20 | 0.000 |
| A | 1 | 3046344 | 10862 | 10862 | 6207.74 | 0.000 |
| B | 1 | 934424 | 5518 | 5518 | 3153.46 | 0.000 |
| C | 1 | 442454 | 1673 | 1673 | 956.05 | 0.000 |
| D | 1 | 70072 | 383 | 383 | 218.63 | 0.000 |
| Square | 4 | 15833 | 15833 | 3958 | 2262.14 | 0.000 |
| A* $A$ | 1 | 6598 | 6727 | 6727 | 3844.56 | 0.000 |
| $B * B$ | 1 | 8867 | 6105 | 6105 | 3489.15 | 0.000 |
| $C * C$ | 1 | 118 | 241 | 241 | 137.68 | 0.000 |
| $D^{*} D$ | 1 | 249 | 249 | 249 | 142.37 | 0.000 |
| Interaction | 6 | 1728 | 1728 | 288 | 164.55 | 0.000 |
| A*B | 1 | 997 | 997 | 997 | 569.95 | 0.000 |
| $A^{*} C$ | 1 | 470 | 470 | 470 | 268.61 | 0.000 |
| $A^{*} D$ | 1 | 75 | 75 | 75 | 42.79 | 0.000 |
| $B * C$ | 1 | 144 | 144 | 144 | 82.33 | 0.000 |
| $B * D$ | 1 | 23 | 23 | 23 | 13.11 | 0.004 |
| $C * D$ | 1 | 18 | 18 | 18 | 10.52 | 0.007 |
| Re sidual error | 12 | 21 | 21 | 21 |  |  |
| Lack of fit | 10 | 21 | 21 | 21 | 475431.43 | 0.000 |
| Pure error | 2 | 0.0000 | 0.0000 | 0.0000 |  |  |
| Total | 26 | 4510876 |  |  |  |  |

Table 11. Optimized income generated compared with the sum of Non-optimized maintenance and replacement costs

| Year | Optimized income $\mathbf{\ddagger}(\mathbf{x 1 0 0 0 )}$ | Non-Optimized sum of Maint \& Replac costs $\mathbf{\#} \mathbf{( x 1 0 0 0 )}$ |
| :--- | :--- | :--- |
| 2005 | 10165.57 | 3961.00 |
| 2006 | 10033.30 | 4490,00 |
| 2007 | 9931.47 | 4920.00 |
| 2008 | 9540.79 | 5315.00 |
| 2009 | 9150.10 | 5598.00 |
| 2010 | 8926.72 | 5921.00 |
| 2011 | 8639.81 | 6065.00 |
| 2012 | 8569.29 | 6605.00 |
| 2013 | 6842.48 | 6851.00 |


| $2014 \quad 6762.03$ | 6948.00 |
| :--- | :--- |



Fig. 4. Plot of Optimized income, and Non-optimized sum of maintenance and replacement costs of Nissan Urvan vehicles against the operational period

## 4. CONCLUSION

The work has demonstrated the application of Numerical optimization in validating the optimized operationof Nissan Urvan vehicle(s). From the study carried out, the following conclusions were drawn:

1. The results of statistical analysis (ANOVA) show that all the control and interaction factors have significant effects on the maintenance and income generated, while the control factors $\mathrm{B}, \mathrm{C}$, and D of replacement cost have no significant effect on replacement cost.
2. The response models of Nissan Urvan Vehicle(s) operations are representable with a nonlinear power law (equations 5 7) and second order polynomial equations (equations $8-10$ ).
3. The income and costs values of the vehicle(s) operation obtained from the validation of the models are in the ranges of those estimated using the models. It implied that numerical optimization approach was appropriate for validating the optimized performance characteristics of Nissan Urvan Vehicle(s).
4. From Table 11 and Fig. 4, comparing the income generated at optimum condition
and the sum of the maintenance \& replacement costs by the year 2013 the income generated is less than the expenditures. This shows that the operation of the transportation system was economical for a period of 8 years from 2005 - 2012. It is hereby recommended that response surface model should be deployed for the operational analysis of the case study company to enhance efficient utilization and profitability.

## COMPETING INTERESTS

Authors have declared that no competing interests exist.

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