

# Deep Recurrent Q-learning Method for Area Traffic Coordination Control

## ABSTRACT

In order to improve the performance of Deep Q-learning when dealing with the area traffic control which is Partially Observable Markov. We introduce Deep Recurrent Q-learning by changing the fully connected network layer to LSTM layer. On the other hand, we use transfer learning to handle the coordination of multiple intersections in the area. By the simulation, we compare the average delay of our algorithm and the Deep Q-learning algorithm for three different saturation flows, respectively. We also compare our algorithm with another two popular traffic signal control algorithms, i.e., Q-learning and fixed time control algorithm. The experiment results show that the performance of our improved Deep Recurrent Q-learning algorithm is better than the other three algorithms.

*Keywords: Area Traffic Coordination Control; Deep Recurrent Network; Deep Q-learning; Deep Recurrent Q-learning*

## 1. INTRODUCTION

The problem of traffic congestion has been very serious, causing economic losses and environmental pollution. There are mainly two techniques to solve the problem of traffic congestion. One is the construction of infrastructure, but the construction cost of this method is relatively expensive, and it cannot solve the problem fundamentally. The other is to develop intelligent transportation system, and to increase the effective control of urban traffic signals by using knowledge in the field of artificial intelligence without increasing existing infrastructure. The second method can save costs and effectively alleviate urban congestion. Surveys and statistics found that most of the traffic jams occurred at intersections, so it is particularly critical to adopt more intelligent control strategies for urban intersections. This article coordinated the control of the area composed of multiple intersections and improved the signal control performance of the intersections.

The use of Deep Q-learning(DQN) methods for optimal control of intersections has achieved good results. DQN does not need to extract human-crafted features and solves the problem of dimensional explosion[1]. Richter S et al. proved that the state of the intersection is Partially Observable Markov(POMDP)[2], DQN's performance deteriorates due to inaccurate observation status. Some efforts have been made in the state representation to reduce the impact of POMDP. The literature [3] and [4] represent Q-values with deep convolution neural network. The location and speed of vehicles at the intersection are represented by matrix. In addition to using the location and speed matrix of vehicles, Van der Pol E also adds the acceleration matrix of vehicle as the state of intersection[5]. The work[6] directly input the first four frames of intersection, and use deep neural network to deal with these high-dimensional state representations.

This paper introduces Deep Recurrent Q-learning(DRQN) to further reduce the effect of the POMDP. For area traffic coordination control, which is a multi-agent Q-learning problem, transfer learning is used to reduce the training time for DRQN. The rest of this paper is organized as follows. In Section 2, we define reinforcement learning components for a single intersection, we also introduce the structure of DRQN. In Section 3, we apply DRQN to multi-agents, using transfer learning and max-plus for area traffic coordination control. In Section 4, we verify our algorithm by simulations and compare its performance to popular traffic signal control algorithms. In Section 5, we conclude the whole paper.

## 2. Q-LEARNING FOR SINGLE INTERSECTION

Q-learning is described by the following process: during each iteration, the agent observes its current environment, from which it infers the environment's state  $S$ , then executes an action selected from the action space  $A$ . Then the agent transfers to the next state and gets the reward  $R$ . The Q-values from  $S$  to  $A$  is denoted by  $Q(S, A)$ .

Assume that the state of the agent at time  $t$  is  $s_t$ , the action taken by the agent is  $a_t$ , the state transitions to the next  $t+1$  moment is  $s_{t+1}$  and the agent gets the reward  $r_t$ . After that, the agent updates  $Q(S, A)$  according to all records  $(s_t, a_t, r_t, s_{t+1})$  to find the best strategy. In this section, we formulate traffic signal control problem as a Q-learning problem.

### 2.1 State Space

Consider the four-phase single intersection shown in Fig. 1. Taking the position, velocity and acceleration matrix of the vehicles in the current intersection as input.

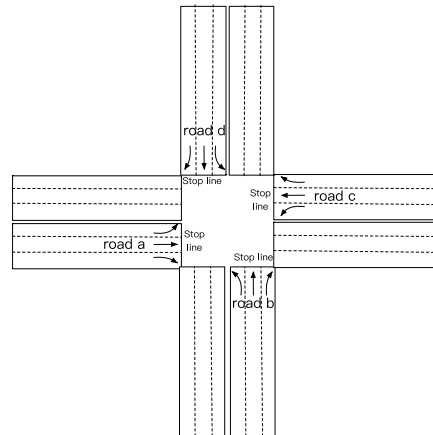


Fig. 1. Four-phase intersection schematic

Take road a in Fig. 1. as an example, suppose the current intersection vehicle is shown in Fig. 2. Consider a section of distance  $L$  from the stop line, divide the road into multiple small sections called Cell, and the length of each Cell is  $C$ . Then, the position matrix of the current intersection are shown in Table 1. When there is a vehicle in the divided Cell, the corresponding position of the matrix is 1, and vice versa is 0. When a vehicle crosses two Cells, the Cell that has a large proportion of occupancy is selected. The velocity matrix and the acceleration matrix are the same as the position matrix, the matrix values are normalized by the upper limits of velocity and acceleration in the simulation software.

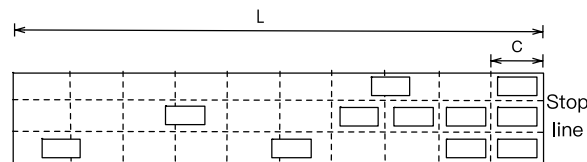


Fig. 2. Vehicle location of road a

Table 1. Position matrix of entrance road a

|   |   |   |   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|---|---|---|
| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 1 |
| 0 | 0 | 0 | 1 | 0 | 0 | 1 | 1 | 1 | 1 |
| 1 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 1 | 1 |

## 2.2 Action Space

In this research, the agent's possible actions are the traffic signal phase configurations. Suppose the vehicle is always allowed to turn right, we choose North-South Green, East-West Green, North-South Left Green, East-West Left Green as possible actions. The duration of each phase is 10s.

## 2.3 Reward

Q-learning will be iteratively trained according to the reward function. The average delay can indicate the congestion of the current intersection. Therefore, the average delay is used as the evaluation measure for the reward.

## 2.4 $\epsilon$ -greedy

Q-learning will select the action with the largest Q-values as the current action to be performed. To avoid the algorithm falling into a local optimum, it is necessary to choose between exploring new actions and adopting the current optimal action. We implement  $\epsilon$ -greedy exploration policy, which selects a random action with a probability  $\epsilon$  and selects the action with the highest value with a probability  $1 - \epsilon$ . The value of  $\epsilon$  decreases as training epochs progress according to (2.1).

$$\epsilon = \max\left(0.01, 1 - \frac{n}{N}\right) \quad (2.1)$$

Where  $n$  is the current training epoch and  $N$  is the total number of training epochs.

## 2.5 DNN STRUCTURE

Deep Q-learning uses a deep neural network structure to represent the value of  $Q(s|a|\theta)$ , where  $\theta$  represents the weights of the neural network. This section will introduce the specific network structure. In the above, we mentioned that the state of the intersection is POMDP. Define the observation state in POMDP as  $O$ , then  $O$  and real state  $S$  are different, that is,  $Q(s|a|\theta) \neq Q(o|a|\theta)$ .

This article introduces the DRQN, DRQN has been proven to handle POMDP problems very well [7]. DRQN is a combination of a Long Short Term Memory (LSTM) and a Deep Q-Network. LSTM can remember timeline information, by remembering the input states of the previous moments, not just the current moment, the input state of the current intersection can be represented as completely as possible, and the gap between  $Q(s|a|\theta)$  and  $Q(o|a|\theta)$  can be narrowed.

Next, we will introduce the network structure of DRQN. The state matrix is fed to a convolutional neural network with two convolutional layers and the activation function uses ReLU, next is the LSTM layer, the activation function also applies ReLU. The number of layers and the number of neurons in the LSTM layer need to be determined by experiment. The final output layer is a fully connected layer, which is used to output the Q-values of all the actions. The network structure is shown in Fig. 3.

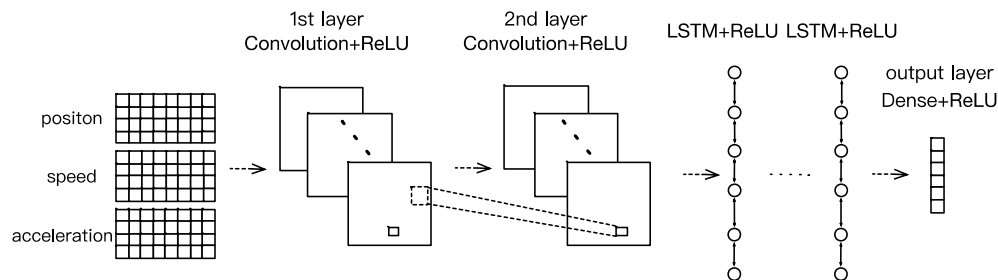


Fig. 3. DRQN network structure

As mentioned above, Q-learning generates many group records  $(s_t, a_t, r_t, s_{t+1})$  in the process of state transition. According to these records, training samples of the deep neural network are constructed. The neural network input is  $s_t$  and the output is the target Q value:

$$y_t = r_t + \gamma \max_{a_{t+1}} Q(s_{t+1}, a_{t+1} | \theta) \quad (2.2)$$

Where  $\gamma$  is the discount factor.

The agent learns weights  $\theta$  by training the DNN network to minimize the following mean squared error (MSE):

$$L(\theta) = E[(r_t + \gamma \max_{a_{t+1}} Q(s_{t+1}, a_{t+1} | \theta) - Q(s_t, a_t | \theta))^2] \quad (2.3)$$

We adopt the stochastic gradient descent algorithm *Adam* to train the network.

To improve algorithm stability, we adopt two methods proposed in [8]: experience replay and target network.

Experience replay sets a replay memory  $M$  to store all records. The replay memory is of finite capacity and when it is full, the oldest data will be discarded. When the agent trains the DNN network, it randomly draws a *batch* ( $batch < M$ ) size samples from the replay memory  $M$  to form input data and target pairs, and then uses these input data and targets to update DNN parameters  $\theta$  by *Adam* algorithm.

The structure of the target network is the same as that of the DRQN. It is used to generate the target value of equation (2.2).

Assume that the original network parameter is  $\theta$ , the target network parameter is  $\theta'$ ,  $\theta$  is updated every step, and  $\theta'$  is updated to the value of  $\theta$  after a certain number of steps.

The algorithm is described as follows:

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**Algorithm 1** Deep reinforcement learning algorithm with experience replay and target network for single intersection

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1: Initialize the DRQN network structure with weights  $\theta$ . Initialize target network with
   weights  $\theta' = \theta$ 
2: Initialize  $\varepsilon, \gamma, N$ 
3: for episode 1 to N do
4:   Initialize intersection state  $s_0$  and action  $a_0$ 
5:   for 1 to T do
6:     Select  $a_t = \arg \max_a Q(s_t, a | \theta)$  with the probability of  $1 - \varepsilon$ , and randomly
       select an action with the probability of  $\varepsilon$ 
7:     Perform selected action  $a_t$ , get reward  $r_t$  and next state  $s_{t+1}$ .
8:     Store observed experience  $(s_t, a_t, r_t, s_{t+1})$  into replay memory  $M$ .
9:     if the number of samples in the replay memory  $> batch$  then
10:      Randomly draw a batch size samples from memory  $M$ , for each
        record,  $y = r_t + \gamma \max_{a_{t+1}} Q(s_{t+1}, a_{t+1} | \theta')$ 
11:      Update  $\theta$  by applying Adam algorithm to training data.
12:      Update  $\theta'$  after reaching a certain number of steps.
13:    end if
14:     $s_{t+1} = s_t$ 
15:  end for
16: end for

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### 3. AREA TRAFFIC COORDINATION CONTROL

As discussed above, when dealing with single-intersection problems, we can train the deep Q network so that the agent can choose the best action. When dealing with the area traffic coordination control, which is a multi-agent Q-learning problem, our goal is also to select the joint action that allows multiple intersections to achieve optimal results. A simple idea is that we can choose the optimal actions for each intersection separately, and then combine these actions into a joint action. However, the behavior of the agent  $i$  can be regarded as the environment in which the agent  $j$  is located. That is to say, the agent  $i$  must consider the action of the agent  $j$  when selecting the optimal action. Therefore, the optimal action of a multi-agent must be considered together.

Coordination algorithm can be used to obtain multi-agent optimal joint action, commonly used coordination algorithms include variable elimination and Max-plus[9] algorithms. By maximizing over one factor at a time, variable elimination is much faster than optimizing over the entire joint action space. However, it is computationally expensive, as the execution time is exponential as the number of agents increases. In such cases, the Max-plus algorithm is a better choice.

#### 3.1 Max-plus

Suppose that we have a coordination graph  $\mathcal{G} = (\mathcal{V}, \mathcal{E})$ , each agent  $i$  repeatedly sends a message  $\mu_j$  to its neighbors  $j$ . The message  $\mu_j$  is defined as:

$$\mu_j(a_j) = \max_{a_i} \left\{ f_{ij}(a_i, a_j) + \sum_{k \in \Gamma(i) \setminus j} \mu_{ki}(a_i) \right\} \quad (3.1)$$

where  $\Gamma(i) \setminus j$  represents all neighbors of agent  $i$  except agent  $j$ .

The meaning of this formula is,  $i$  sends a message to  $j$  that consists of a maximization over  $i$  and  $j$ 's factor and the messages  $i$  has received from its neighbours that are not  $j$ . An agent  $i$  only has to sum over the received messages from its neighbors which are defined over individual actions, instead of enumerating over all possible action combinations of its neighbors. Messages are exchanged until they converge to a fixed point, or until some external signal is received. When the iteration of the max-plus algorithm is terminated, each agent  $i$  can get the optimal action according to the following equation:

$$a_i^* = \arg \max_{a_i} \sum_{j \in \Gamma(i)} \mu_{ji}(a_i) \quad (3.2)$$

The max-plus algorithm is shown in Algorithm 2.

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#### Algorithm 2 Max-plus algorithm

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- 1: Initialize  $\mu_j = \mu_{ji} = 0$  for all vertices  $(i, j)$ .
  - 2: Initialize fixed point = false, number of iterations  $n = 0$ , maximum number of iterations is  $N_{\max}$ , threshold  $\Delta$
  - 3: **while** fixed point = false and  $n < N_{\max}$  **do**
  - 4:   fixed point = True,  $n = n + 1$ .
  - 5:   **for every** agent  $i$  **do**
  - 6:     **for all** neighbors  $j \in \Gamma(i)$  **do**
  - 7:        $i$  send message  $\mu_{ji}(a_j)$  to  $j$  according to equation(3.1)
  - 8:       **if**  $\mu_{ji}(a_j)$  differs from previous message by  $\Delta$  **then**
  - 9:          fixed point = False
  - 10:       **end if**
  - 11:    **end for**
  - 12: **end for**
  - 13: **end while**
  - 14: Get the best action  $a_i^*$  according to equation (3.2).
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### 3.2 Transfer Learning

When dealing with area coordination control problems, it will take a long time if Q-learning is performed for every intersections. According to the literature [10], intersections of same traffic flow are divided into one area, so we can think that the Q functions of all intersections are relatively close. Therefore, we can use transfer learning [11]. Although the approximation of the Q-values is less accurate, the advantage of using transfer learning instead of multi-agent reinforcement learning is that less time has to be spent on training.

### 3.3 Area Coordination Control

In this section, we will combine the max-plus algorithm and transfer planning and apply it to area coordination control. In area coordination control, we define  $f_{ij}(a_i, a_j)$  as:

$$f_{ij}(a_i, a_j) = Q_i(s_i, a_i | q) + Q_j(s_j, a_j | q) \quad (3.3)$$

Where  $Q_i(s_i, a_i | q)$  and  $Q_j(s_j, a_j | q)$  are the Q functions for i and j, respectively.

For the pseudocode of the entire algorithm, see Algorithm 3.

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#### Algorithm 3 Area Coordination Control

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1: Initialize  $Q(s, a | q)$  for a single intersection using Algorithm 1.
2: Initialize  $s \leftarrow s_0$ 
3: for time step t do
4:   Get the best action  $a^*$  from s according to Algorithm 2.
5:   for every agent i do
6:     take action  $a_i^*$ 
7:   end for
8:   Transfer to a new state  $s'$ ,  $s \leftarrow s'$ 
9: end for

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## 4. SIMULATION RESULTS AND ANALYSIS

### 4.1 Simulation Settings

In order to validate the performance of DRQN in this paper, microscopic traffic simulation software (USTCMTS2.1) is used, which is developed by laboratory of the data fusion & intelligent traffic system, University of Science and Technology of China. The DNN network shown in Fig. 3. is implemented using Keras Python libraries. USTCMTS2.1 uses C# as programming language, C# and Python communicate using the IronPython library. Detailed simulation settings are as follows.

**Parameter settings:** The agent is trained for  $N = 200$  episodes. Each episode lasts  $T = 0.1$  hours. Set discount factor  $\gamma = 0.95$ , capacity of replay memory  $M = 2000$  and  $batch = 32$ . Set  $N_{max} = 30$ , threshold  $\Delta \leq 10^{-9}$ .

**DNN Structure:** The first convolution layer has 32 convolution kernels and the convolution kernel is  $3 \times 3$ . The second convolution layer has 64 convolution kernels and the convolution kernel is also  $3 \times 3$ . Learning rate of DNN is 0.001.

**Intersection:** As shown in Fig. 4, a typical area consisting of the four intersections is selected. Set road segment L to be 224 meters, cell length C to be 7 meters.

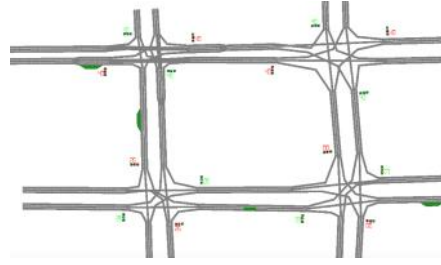


**Fig. 4. An area of four intersections**

**Intersection traffic flow settings:** Select three typical traffic flows, low saturation, near saturation, and supersaturation, each intersection has the same flow, flow values are shown in Table 2.

**Table 2. Traffic Flow**

|                               | road a | road b | road c | road d |
|-------------------------------|--------|--------|--------|--------|
| <b>Low saturation(veh/h)</b>  | 96     | 228    | 80     | 236    |
| <b>Near saturation(veh/h)</b> | 592    | 672    | 352    | 736    |
| <b>Supersaturation(veh/h)</b> | 664    | 1600   | 696    | 1632   |

## 4.2 Simulation Results

First, we determine the number of LSTM layers and the number of neurons for the above three typical flows, respectively. According to the experience of parameter setting in deep learning, we choose the number of layers of the network from 1 to 3, and the number of neurons is {64, 128, 256, 512}. Using grid search, the average delays of the three types of traffic under different network parameters are shown in Table 3:

**Table 3. Average delay under different network parameters(low saturation/near saturation/supersaturation)**

|          | 64                | 128                       | 256                        | 512                |
|----------|-------------------|---------------------------|----------------------------|--------------------|
| <b>1</b> | 45.16/66.3/93.12  | 47.33/59.87/96.1          | 47.02/61.23/95.33          | 49.91/65.29/97.72  |
| <b>2</b> | 48.67/75.54/89.57 | <b>43.39</b> /65.38/99.49 | 50.41/57.81/103.5          | 53.4/63.74/101.69  |
| <b>3</b> | 54.87/62.47/94.78 | 44.57/64.93/ <b>87.94</b> | 46.14/ <b>56.12</b> /91.38 | 45.66/65.18/106.96 |

As can be seen from the table, the optimal network structure for the three saturations are 2/3/3 LSTM layer with 128/256/128 neurons per layer, respectively.

Then, taking the near saturation flow as an example, we analyze the performance of the DRQN proposed in this paper. The network structure adopts the optimal network structure shown in Table 3, we records the intersection delay every 180 simulation seconds. The average delay for the original DQN is 60.22s and the average delay for the DRQN is 56.12s. The average DRQN delay is found to be 6.8% lower than the original DQN. Fig. 5. shows the comparison between DRQN and traditional Q-learning and fixed time control. The average delays for Q-learning and fixed time control are 65.08s and 69.24s. Compared with these two algorithms, DRQN reduces the average delay by 13.8% and 18.9%, respectively. These results show that the historical information recorded by the recurrent neural network does make the observed state more in line with the real intersection state.

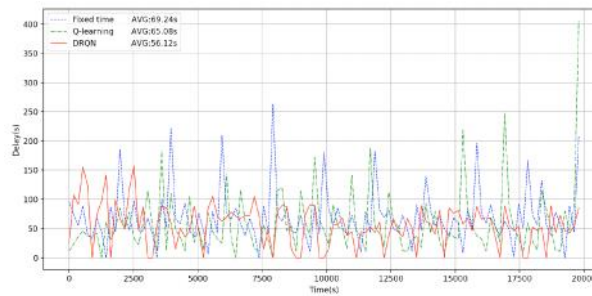


Fig. 5. The average delay comparison of the three algorithms

Experiments are also conducted on the other two saturation flows. The average delays are shown in Table 4:

Table 4. Low saturation and supersaturation average delay comparison results

|                 | Fixed time(s) | Q-learning(s) | DQN(s) | DRQN(s) |
|-----------------|---------------|---------------|--------|---------|
| low saturation  | 49.7          | 46.67         | 44.92  | 43.39   |
| supersaturation | 109.59        | 102.25        | 95.98  | 87.94   |

It is found that when two another saturations are taken, the result is similar to that of near saturation. The average delay of the original DQN is smaller than the average delay of fixed time control and Q-learning. The average delay of the DRQN algorithm is also smaller than the original DQN.

## 5. CONCLUSION

In this paper, we use DRQN network to handle intersection signal control problems. At the same time, multi-agent coordination control is implemented using transfer learning and max-plus. Experiments show that the DRQN algorithm improves the performance of DQN algorithm at different saturation flow conditions, and is also superior to fixed time control and Q-learning algorithms. Although we have adopted transfer learning to reduce the training time for Q-learning, it is expected that there are more methods will be proposed to improve the speed of the algorithm while ensuring the accuracy.

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