

Original Research Article

Cryptanalysis and Improvement on an E-mail Protocol

Abstract

With the rapid development of Internet, e-mail has become an essential communication tool. But, the security of e-mail communications is an important issue. Recently, Chen et al. proposed a new protocol of wide use for e-mail. Chen et al. claimed that the proposed protocol is skillfully designed to achieve perfect forward secrecy and end to end security as well as to satisfy the requirements of confidentiality, origin, integrity and easy key management. But, in this paper, we show that Chen et al.'s protocol suffers from the e-mail server impersonation attack, mail content confidentiality attack and replay attack. Moreover, we give an improvement on Chen et al.'s protocol. We also discuss the security of the improved protocol. The improved protocol provides the perfect forward secrecy and resists replay attack, impersonation attack, and mail content confidentiality attack.

Keywords: Cryptography; Secure protocol; E-mail protocol; Security

1. Introduction

With the rapid development of Internet, e-mail has become an essential communication tool. Unfortunately the basic e-mail protocol does not provide the confidentiality and integrity service. So, the security of e-mail communications is an important issue. Bacard [1] introduced some security requirements in e-mail systems. Since then, several security protocols such as, PGP [2], PEM [3] and S/MIME [4] have been designed to provide confidentiality and authentication of e-mail system. However, these protocols cannot provide perfect forward secrecy [5] because once the secret key of the receiver is disclosed, all previous used short-term keys will also be opened and hence previous e-mail will be learned.

In order to provide perfect forward secrecy, Sun et al. [5] proposed two new e-mail protocols. However, in 2006, Dent [6] pointed out Sun et al.'s protocols do not provide perfect forward secrecy as claimed. Later, Kim et al. [7] proposed an improved version of Sun et al.'s protocols to overcome this weakness. But, in 2010, Chang et al. [8] showed that Kim et al.'s protocols suffer from the well-known man-the-middle attack and consequently do not achieve perfect forward secrecy.

In 2007, Kwon et al. [9] proposed a password-based e-mail protocol for mobile devices. However too many modular exponentiation operations in their protocol might cause mobile devices consume battery power expeditiously [8].

Recently, Chen et al. [10] took into account the scenario that the e-mail sender and the recipient register at different servers and proposed a new protocol of wide use

for e-mail. Chen et al. claimed that the proposed protocol is skillfully designed to achieve perfect forward secrecy and end to end security as well as to satisfy the requirements of confidentiality, origin, integrity and easy key management. But, in this paper, we show that Chen et al.'s protocol suffers from the e-mail server impersonation attack, mail content confidentiality attack and replay attack. Moreover, we give an improvement on Chen et al.'s protocol. We also discuss the security of the improved protocol. The improved protocol provides the perfect forward secrecy and resists replay attack, impersonation attack, and mail content confidentiality attack.

This article is organized as follows. We review Chen et al.'s protocol in Section 2 and point out its flaws in Section 3. In Section 4, we give an improvement on Chen et al.'s protocol. The security analysis of the improved protocol is discussed in Section 5. Finally, conclusions are given in Section 6.

2. Review of Chen et al.'s e-mail protocol

In this section, we review Chen et al.'s e-mail protocol [10]. Chen et al.'s protocol consists of three phase: registration, sending, and receiving.

2.1 Registration

Either e-mail the sender or the recipient has to register at an individual e-mail server at the beginning. For example, when a participant A (resp. B) registers at e-mail server S_A (resp. S_B), it implies that A shares password Q_1 with S_A . A submits ID_A and $g^{aQ_1} \bmod n$ to S_A where n is a big prime number, g is a generator with order $n-1$ over $GF(n)$, and a is a random number. S_A computes the registration information $(g^a \bmod n)$ with Q_1^{-1} and stores $(g^a \bmod n)$. Likewise, the participant B shares Q_2 with e-mail server S_B . S_B stores $(g^b \bmod n)$ for B . The e-mail server S_A and S_B also share a password K , MAC denotes a message authentication code. $[\cdot]_K$ denotes the symmetric encryption with the key K . For simplicity, 'mod n ' is omitted hereafter.

2.2 Sending phase

When sender A intends to send an e-mail to recipient B , the operation goes as follows:

71 Step 1: $A \rightarrow S_A$: Request.

72 If A wants to deliver an e-mail to B , he should send the request to S_A firstly.

73 Step 2: $S_A \rightarrow S_B$: Request.

74 S_A forwards the request to S_B to ask for the registration information of B

75 Step 3: $S_B \rightarrow S_A$: $ID_B, g^b, MAC_K(ID_B, g^b)$

76 S_B finds the registration information g^b of B . Then S_B computes the
77 MAC value of ID_B, g^b with K , and sends $ID_B, g^b, MAC_K(ID_B, g^b)$ to S_A .

78 Step 4: $S_A \rightarrow A$: $ID_B, g^b, MAC_{Q_1}(ID_B, g^b)$

79 In order to check the validation of the received message, S_A computes
80 $MAC_K(ID_B, g^b)$ and checks if the computed MAC value is equal to the received
81 MAC value. If it holds, S_A computes the MAC value of ID_B, g^b with Q_1 and
82 sends $ID_B, g^b, MAC_{Q_1}(ID_B, g^b)$ to A .

83 Step 5: $A \rightarrow S_A$: $ID_A, ID_B, [M]_{g^{xb}}, g^x, MAC_{Q_1}(ID_A, ID_B, [M]_{g^{xb}}, g^x)$.

84 Upon receiving the message, A computes $MAC_{Q_1}(ID_B, g^b)$ and checks if the
85 computed MAC value is equal to the received MAC value. If it holds,
86 A computes g^x with a random number x and g^{xb} by computing $(g^b)^x$. A
87 encrypts mail content M with g^{xb} . Then A computes the MAC value of
88 $ID_A, ID_B, [M]_{(g^{xb})}, g^x$ with Q_1 and sends
89 $ID_A, ID_B, [M]_{(g^{xb})}, g^x, MAC_{(Q_1)}(ID_A, ID_B, [M]_{(g^{xb})}, g^x)$
90 to S_A .

91 Step 6: $S_A \rightarrow S_B$: $ID_A, ID_B, [M]_{(g^{xb})}, g^x, MAC_K(ID_A, ID_B, [M]_{(g^{xb})}, g^x)$.

92 S_A checks the validation of the received message. he computes
93 $MAC_{Q_1}(ID_A, ID_B, [M]_{g^{xb}}, g^x)$ and checks if the computed MAC value is equal to

94 the received MAC value. If it holds, S_A computes the MAC value of
 95 $ID_A, ID_B, [M]_{(g^{xb})}, g^x$ with K and sends
 96 $ID_A, ID_B, [M]_{(g^{xb})}, g^x, MAC_K(ID_A, ID_B, [M]_{(g^{xb})}, g^x)$
 97 to S_B . After receiving the message, S_B stores the e-mail message for B .

98 **2.3 Receiving phase**

99 Step 7: $B \rightarrow S_B: ID_B, g^{b'}, MAC_{Q_2}(ID_B, g^{b'}, g^b)$.

100 When B is on-line and intends to check e-mails, he will compute $g^{b'}$ with a
 101 new random number b' and $MAC_{Q_2}(ID_B, g^{b'}, g^b)$. Then B sends

102 $ID_B, g^{b'Q_2}, MAC_{Q_2}(ID_B, g^{b'}, g^b)$

103 to S_B

104 Step 8: $S_B \rightarrow B: ID_A, ID_B, [M]_{g^{xb}}, g^x, MAC_{Q_2}(ID_A, ID_B, [M]_{g^{xb}}, g^x, g^{b'})$

105 Upon S_B receiving the message, S_B verifies $MAC_{Q_2}(ID_B, g^{b'}, g^b)$. If the
 106 verification fails, S_B will reject the request from B . Otherwise, S_B update g^b
 107 with $g^{b'}$. Lastly, S_B computes the MAC value of $ID_A, ID_B, [M]_{g^{xb}}, g^x, g^{b'}$ with
 108 Q_2 and sends

109 $ID_A, ID_B, [M]_{g^{xb}}, g^x, MAC_{Q_2}(ID_A, ID_B, [M]_{g^{xb}}, g^x, g^{b'})$

110 to B .

111 When B receives the message from S_B , he computes

112 $MAC_{Q_2}(ID_A, ID_B, [M]_{g^{xb}}, g^x, g^{b'})$.

113 **B** checks if the computed MAC value. If it holds, he computes g^{xb} by computing
 114 $(g^x)^b$ to decrypt $[M]_{g^{xb}}$.
 115

116 **3. The Cryptanalysis of Chen et al.'s protocol**

117 In this section, we show that Chen et al.'s protocol suffers from the e-mail server

118 impersonation attack, mail content confidentiality attack and replay attack.

119 **3.1 The e-mail server impersonation attack**

120 In Chen et al.'s protocol, the e-mail server S_B can impersonate the e-mail
121 sender A to send message to B .

122 In fact, when S_B receives $g^{b'}$ in step 7, S_B can pick a random number x'
123 and computes $g^{x'}$. Then S_B computes

$$124 \quad [M']_{g^{x'b}}, MAC_{Q_2}(ID_A, ID_B, [M']_{g^{x'b}}, g^{b'}, g^b).$$

125 Where M' is the mail content that S_B wants to impersonate the e-mail sender A
126 to send to B . Then S_B sends

$$127 \quad ID_A, ID_B, [M']_{g^{x'b}}, g^{x'}, MAC_{Q_2}(ID_A, ID_B, [M']_{g^{x'b}}, g^{b'}, g^b)$$

128 to B . Receiving the message, B cannot find any problem by checking the MAC
129 value and believe M' is the mail content which the sender A want to send him. So,
130 the e-mail server S_B successfully impersonate the sender A to send message to the
131 receiver B .

132 **3.2 Replay attack**

133 In Chen et al.'s protocol, when an attacker intercepts the message
134 $ID_A, ID_B, [M]_{g^{xb}}, g^x, MAC_{Q_1}(ID_A, ID_B, [M]_{g^{xb}}, g^x)$ in step 5, he can use it in future to
135 implement replay attack. In next procedure of A sending e-mail to B , the attacker
136 can send the intercepted message

$$137 \quad ID_A, ID_B, [M]_{g^{xb}}, g^x, MAC_{Q_1}(ID_A, ID_B, [M]_{g^{xb}}, g^x)$$

138 to S_A in step 5. S_A cannot find any problem. Then S_A sends

$$139 \quad ID_A, ID_B, [M]_{g^{xb}}, g^x, MAC_K(ID_A, ID_B, [M]_{g^{xb}}, g^x)$$

140 to S_B . In step 6, S_B also cannot find any problem. Then S_B sends

$$141 \quad ID_A, ID_B, [M]_{g^{xb}}, g^x, MAC_{Q_2}(ID_A, ID_B, [M]_{g^{xb}}, g^{b'}, g^b)$$

142 to B . In step 8, the message also satisfies the verification. So, the attacker
143 successfully implement replay attack. Of course, at the end of the replay attack, the
144 mail content got by the receiver B may not be M , because the personal
145 information g^b might have replaced by $g^{b'}$.

146 3.3 Mail content confidentiality attack

147 In step 4 of Chen et al.'s protocol, the mail server S_A can pick a random
 148 number c and send $ID_B, g^c, MAC_{Q_1}(ID_B, g^c)$ to the e-mail sender A . Then in step
 149 5 when S_A receives the message $[M]_{g^{xc}}, g^x$, S_A can compute $g^{xc} = (g^x)^c$ and
 150 obtain the mail content by decrypting $[M]_{g^{xc}}$. Then S_A can continue performing
 151 step 6. At the end of the protocol, the receiver B may get a false mail content since
 152 $g^c \neq g^b$.

154 4. The improved protocol

155 4.1. Registration

156 The registration phase of the improved protocol is essentially identical to that of
 157 Chen et al.'s protocol. The mail sender A shares a password Q_1 with his mail
 158 server S_A . The mail receiver B shares a password Q_2 with his mail server S_B .
 159 S_A and S_B also share a password K , MAC denotes a message authentication
 160 code. $[\cdot]_K$ denotes the symmetric encryption with the key K . But, the personal
 161 information of the e-mail sender A is g^a and $Sig_{SK_A}(g^a)$. Where SK_A is the
 162 private key of A , $Sig_{SK_A}(g^a)$ is the signature generated by A . Likewise, the
 163 personal information of the e-mail receiver B is g^b and $Sig_{SK_B}(g^b)$.

164 4.2. Sending phase

165 When sender A intends to send an e-mail to the recipient B , the operation goes as
 166 follows:

167 Step 1: $A \rightarrow S_A$: Request.

168 If A wants to deliver an e-mail to B , he first sends the request to his mail

169 server S_A .

170 Step 2: $S_A \rightarrow S_B$: Request.

171 S_A forwards the request to S_B , the recipient B 's server, to ask for the
172 registration information of B

173 Step 3: $S_B \rightarrow S_A$: $ID_B, g^b, Sig_{Sk_B}(g^b), MAC_K(ID_B, g^b, Sig_{Sk_B}(g^b))$

174 S_B finds $ID_B, g^b, Sig_{Sk_B}(g^b)$ of B . Then S_B computes the MAC value of
175 $ID_B, g^b, Sig_{Sk_B}(g^b)$ with K , and sends

176 $ID_B, g^b, Sig_{Sk_B}(g^b), MAC_K(ID_B, g^b, Sig_{Sk_B}(g^b))$

177 to S_A .

178 Step 4: $S_A \rightarrow A$: $ID_B, g^b, Sig_{Sk_B}(g^b), MAC_{Q_1}(ID_B, g^b, Sig_{Sk_B}(g^b))$

179 S_A computes $MAC_K(ID_B, g^b, Sig_{Sk_B}(g^b))$ and checks if the computed MAC
180 value is equal to the received MAC value. If it holds, S_A computes the MAC
181 value of $MAC_{Q_1}(ID_B, g^b, Sig_{Sk_B}(g^b))$ and sends

182 $ID_B, g^b, Sig_{Sk_B}(g^b), MAC_{Q_1}(ID_B, g^b, Sig_{Sk_B}(g^b))$

183 to A .

184 Step 5: $A \rightarrow S_A$:

185 $ID_A, ID_B, [M]_{g^{xb}}, g^x, Sig_{SK_A}(g^x), T, MAC_{Q_1}(ID_A, ID_B, [M]_{g^{xb}}, g^x, Sig_{SK_A}(g^x), T)$

186 Upon receiving the message, A first verifies the signature $Sig_{SK_B}(g^b)$. Then

187 A computes

188 $MAC_{Q_1}(ID_B, g^b, Sig_{Sk_B}(g^b))$

189 and checks if the computed MAC value is equal to the received MAC value. If the

190 verifications hold, A computes g^x with a random number x and g^{xb} by

191 computing $(g^b)^x$. A encrypts M with g^{xb} , where M is the content of the

192 e-mail. Then A computes the MAC value of $ID_A, ID_B, [M]_{g^{xb}}, g^x, Sig_{SK_A}(g^x), T$

193 with Q_1 and sends

$$194 \quad ID_A, ID_B, [M]_{g^{xb}}, g^x, Sig_{SK_A}(g^x), T, MAC_{Q_1}(ID_A, ID_B, [M]_{g^{xb}}, g^x, Sig_{SK_A}(g^x), T)$$

195 to S_A . Where T is time stamp.

196 Step 6: $S_A \rightarrow S_B$:

$$197 \quad ID_A, ID_B, [M]_{g^{xb}}, g^x, Sig_{SK_A}(g^x), T, MAC_K(ID_A, ID_B, [M]_{g^{xb}}, g^x, Sig_{SK_A}(g^x), T).$$

198 S_A computes $MAC_{Q_1}(ID_A, ID_B, [M]_{g^{xb}}, g^x, Sig_{SK_A}(g^x), T)$ and checks if the

199 computed MAC value is equal to the received MAC value. If it holds, S_A

200 computes the MAC value of $ID_A, ID_B, [M]_{g^{xb}}, g^x, Sig_{SK_A}(g^x), T$ with K and sends

$$201 \quad ID_A, ID_B, [M]_{g^{xb}}, g^x, Sig_{SK_A}(g^x), T, MAC_K(ID_A, ID_B, [M]_{g^{xb}}, g^x, Sig_{SK_A}(g^x), T)$$

202 to S_B . After receiving the message, S_B stores the e-mail message for B .

203 4.3. Receiving phase

$$204 \quad \text{Step 7: } B \rightarrow S_B: ID_B, g^{b'}, Sig_{SK_B}(g^{b'}), MAC_{Q_2}(ID_B, g^{b'}, Sig_{SK_B}(g^{b'}), g^b).$$

205 When B checks e-mails, he will compute $g^{b'}$ with a new random number b'

206 and $MAC_{Q_2}(ID_B, g^{b'}, Sig_{SK_B}(g^{b'}), g^b)$. Then B sends

$$207 \quad ID_B, g^{b'Q_2}, MAC_{Q_2}(ID_B, g^{b'}, Sig_{SK_B}(g^{b'}), g^b)$$

208 to S_B

209 Step 8: $S_B \rightarrow B$:

$$210 \quad ID_A, ID_B, [M]_{g^{xb}}, g^x, Sig_{SK_A}(g^x), T, MAC_{Q_2}(ID_A, ID_B, [M]_{g^{xb}}, g^x, Sig_{SK_A}(g^x), g^{b'}, g^b, T)$$

211 Upon S_B receiving the message, S_B first verifies the signature $Sig_{SK_B}(g^{b'})$.

212 Then he verifies

$$213 \quad MAC_{Q_2}(ID_B, g^{b'}, Sig_{SK_B}(g^{b'}), g^b).$$

214 If the verifications fail, S_B will reject the request from B . Otherwise, S_B update

215 g^b with $g^{b'}$. Lastly, S_B computes the MAC value of

216 $ID_A, ID_B, [M]_{g^{xb}}, g^x, Sig_{SK_A}(g^x), T$ with Q_2

217 and sends

218 $ID_A, ID_B, [M]_{g^{xb}}, g^x, Sig_{SK_A}(g^x), T, MAC_{Q_2}(ID_A, ID_B, [M]_{g^{xb}}, g^x, Sig_{SK_A}(g^x), g^{b'}, g^b, T)$

219 to B .

220 When B receives the message from S_B , he computes

221 $MAC_{Q_2}(ID_A, ID_B, [M]_{g^{xb}}, g^x, Sig_{SK_A}(g^x), g^{b'}, g^b, T)$.

222 B checks if the computed MAC value is equal to the received MAC value. If it

223 holds, he computes g^{xb} by computing $(g^x)^b$ to decrypt $[M]_{g^{xb}}$.

224

225 **5. Security analysis of the improved protocol**

226 **5.1 Perfect forward secrecy**

227 In a protocol, if compromise of long-term keys does not compromise session
228 keys, it's said that the protocol satisfies the perfect forward secrecy. In improved
229 protocol, the session key g^{xb} is determined by the randomly selected secret numbers

230 x and b . So, the session key g^{xb} has no relationship with the long-term SK_A or

231 SK_B . Even if the attacker gets g^x and g^b by compromise of long-term keys SK_A

232 and SK_B , the attacker also cannot get g^{xb} thanks to the difficulty of computing

233 discrete logarithm. Therefore, the improved protocol satisfies the perfect forward
234 secrecy.

235 **5.2. Replay attack**

236 An attacker may intercept message in step 3, step 4, step 5, step 6, step 7 and

237 step 8. But in improved protocol the information g^b of receiver B is renewed

238 when each receiving e-mail is finished. Secondly, time stamp T is involved in step 5,
239 step 6, step 7 and step 8 to guarantee the freshness of transmitted messages. So, the
240 intercepted messages are useless for the attacker to perform replay attacks.

241 **5.3. Sender impersonation attack**

242 If an attacker wants to impersonate e-mail sender A to send a message to
243 receiver B , he must know the password Q_1 or Q_2 and private key SK_A . Because

in step 5, step 6 and step 8 g^x is signed by SK_A . Before decrypting the mail content, the e-mail receiver B first verifies the signature $Sig_{SK_A}(g^x)$ generated by e-mail sender A . The attacker do not know SK_A , then he cannot generate signature $Sig_{SK_A}(g^x)$. So, the attacker cannot success to perform sender impersonation attack. Of course, the e-mail server S_B cannot perform sender impersonation attack.

5.4. Mail content confidentiality attack

Unlike Chen et al.'s protocol, the improved protocol can resist mail content confidentiality attack. Because in step 4 of improved protocol, the signature $Sig_{SK_B}(g^b)$ is needed. The mail server S_A cannot successfully change the information g^b of B . So, in step 5 of the improved protocol, S_A cannot decrypt $[M]_{g^{xb}}$. Of course, except the e-mail receiver B , no one can obtains the mail content.

6. Conclusion

In this paper, we show that Chen et al.'s e-mail protocol suffers from the e-mail server impersonation attack, mail content confidentiality attack and replay attack. Moreover, we give an improvement on Chen et al.'s e-mail protocol. We also discuss the security of the improved protocol. The improved protocol provides the perfect forward secrecy and resists replay attack, impersonation attack, and mail content confidentiality attack.

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