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2**3 Calculation of Measurement Uncertainty for Tensile Strength and Flexural Strength of  
4 Thermoplastic**

5 **Abstract:** In this study, a thermoplastic such as polycarbonate (PC) has been characterized  
6 to determine its tensile strength and flexural strength properties. The width and thickness of  
7 the PC samples have been measured, and then their average dimensions and standard  
8 deviation values were calculated. The samples have been characterized by using a universal  
9 testing machine. The tensile strength values of the dumbbell-shaped PC samples were  
10 determined according to ASTM D638-10, whereas ASTM D790-10 was applied to ascertain  
11 the flexural strength values of the rectangular-shaped PC samples. Based on the obtained  
12 results, the average tensile strength value is  $58.978 \pm 0.258$  MPa, whilst the average flexural  
13 strength value is  $97.437 \pm 0.240$  MPa. From the measurement uncertainty, the calculated  
14 expanded uncertainty for the tensile strength is 0.467 MPa at a confidence level of 95%. On  
15 the other hand, the calculated expanded uncertainty for the flexural strength is 0.806 MPa at  
16 a confidence level of 95% as well. In summary, the values of expanded uncertainty for the  
17 PC samples were particularly influenced by the standard uncertainty values of the tested  
18 samples and the expanded uncertainty values of the equipment used.

19 **Keywords:** measurement uncertainty; tensile strength; flexural strength; ASTM D638;  
20 ASTM D790

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**22 1. Introduction**

23 Measurement uncertainty is an array of feasible results in which the possibilities are  
24 designated to each result. All measurements are only finalised if they are followed by a  
25 statement of the accompanied uncertainty, which are dependent on measured values and their  
26 uncertainties. On the other hand, the performance of measurement affects the distribution of  
27 the measured values. The estimated true value obtained from their average value is highly  
28 trustworthy compared to a sole measured value. The calibration and measurement works have  
29 given the vital effects on the measurement uncertainty that are also influencing the  
30 consistency of the attained results. The quality of the laboratory usually indicated by the  
31 range of the expanded uncertainty from produced calibration reports, smaller the uncertainty  
32 values frequently resulted in greater the testing charges.

33 Tensile strength is the maximum tensile stress which a material can tolerate while being  
34 extended before fracturing. In other words, it is the limit of the material to withstand exerted  
35 force without causing faulty. Furthermore, the tensile strength can be calculated as force per  
36 unit area. On the other hand, flexural strength is the maximum flexure stress that a material  
37 can resist before failure. The material typically subjected to bending state, therefore it  
38 possesses stress and compressive properties. The three-point bending technique is the most  
39 commonly used in determination of the flexural strength. Moreover, the flexural strength can  
40 be computed as the coefficient of three over two times with the product of the load at the  
41 fracture point and the length of support span divide by the product of the width and the  
42 square of thickness.

43 Hitherto, the study regarding the calculation of measurement uncertainty for the tensile  
44 strength and flexural strength of thermoplastic specifically polycarbonate (PC) has not been  
45 reported yet. Hence, the aim of this study is to demonstrate on how to calculate the expanded

46 uncertainty for the results of tensile strength and flexural strength for the PC samples. On the  
47 other hand, the sources of uncertainty for both strengths have also been thoroughly identified,  
48 computed and separately tabulated based on their test methods. Additionally, the factors that  
49 are influenced the values of calculated expanded uncertainty were extensively described as  
50 well.

## 51 **2. Materials and Methods**

52 The thermoplastic samples used are polycarbonate (PC) that has been procured from GT  
53 Instruments Sdn. Bhd., Malaysia. For tensile test, the samples were dumbbell-shaped (Type  
54 I), whereas for flexural test, the samples were rectangular-shaped with nominal size of  $126 \times$   
55  $12 \times 3 \text{ mm}^3$ . All samples were characterized as purchased without any alterations.

56 The width and thickness of the dumbbell-shaped PC samples were measured by using a  
57 calibrated Mitutoyo digimatic micrometer, and at least three different places within the gauge  
58 length (grip separation) area were recorded. The samples were conditioned according to the  
59 ASTM D618-13 [1] at temperature of  $23 \pm 2^\circ\text{C}$  and relative humidity of  $50 \pm 10\%$  for not  
60 less than 40 hours prior to testing. The ASTM D638-10 [2] was applied to determine tensile  
61 strength at the same temperature and relative humidity as sample conditioning procedure. The  
62 test was conducted by using an Instron universal testing machine (model 5567) equipped with  
63 a 30 kN load cell. The crosshead speed was  $5 \text{ mm min}^{-1}$  [3-5] with a 125 mm gauge length.  
64 The average data value and the standard deviation value from five samples were calculated  
65 and recorded.

66 The rectangular-shaped PC samples were also measured for their width and thickness  
67 with the same micrometer for at least three different places within the support span area, and  
68 then the values were recorded and averaged. The similar conditioning procedure as  
69 mentioned earlier was carried out to condition the samples before testing as well. The flexural  
70 strength of the samples was measured according to the ASTM D790-10 [6] by using the same  
71 universal testing machine equipped with the unchanged load cell. The lengths of support span  
72 were obtained by multiplying the thickness of the samples with 16 [6]. The length of support  
73 span was then fixed by using a calibrated Mitutoyo digimatic caliper. The crosshead speed  
74 was calculated according to the equation which consisted of their length of support span and  
75 thickness of the samples. The average crosshead speed was used for flexural testing. Five  
76 samples were tested to obtain the average value and the standard deviation value.

## 77 **3. Results**

### 78 *3.1. Tensile strength*

79 Throughout the tensile test was conducted, there are some sources of uncertainty that can  
80 be detected which are from the tested PC samples and the measuring equipment used. For the  
81 PC samples, the sources of uncertainty are the measured width and thickness of the samples  
82 themselves. Meanwhile, the sources of uncertainty for the measuring equipment are measured  
83 force, calibrated micrometer and universal testing machine. The values of measured width  
84 and thickness for the dumbbell-shaped PC samples with their calculated averages are shown  
85 in Table 1. In addition, the values of obtained force and tensile strength for the PC samples  
86 with their computed averages are also presented in Table 1.

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**Table 1.** Width, thickness, force, tensile strength and their averages for the PC samples.

No. of sample	Width (mm)	Thickness (mm)	Force (N)	Tensile strength (MPa)
1	13.173	3.026	2349.215	58.934
2	13.238	3.005	2329.533	58.560
3	13.232	3.006	2349.223	59.062
4	13.262	3.009	2364.229	59.246
5	13.303	3.009	2365.122	59.086
<b>Average</b>	13.242	3.011	2351.464	58.978

91 The standard deviations were also calculated to determine the standard uncertainties  
 92 aside from been used to show the error range [7]. The standard deviations of width, thickness,  
 93 force and tensile strength of the samples have been computed according to Equation 1. The  
 94 standard deviation values for the width, thickness, force and tensile strength of five PC  
 95 samples measured are displayed in Table 2. On the other hand, the standard uncertainties of  
 96 width, thickness, force and tensile strength of the samples have been calculated based on  
 97 Equation 2. The standard uncertainty values of width, thickness, force and tensile strength for  
 98 the five PC samples measured are also displayed in Table 2. From the obtained results, it can  
 99 be observed that the smaller standard deviation values resulted in lower standard uncertainty  
 100 values. This is due to the fact that the standard uncertainty values are directly proportional to  
 101 the standard deviation values.

$$s = \sqrt{\frac{\sum_{i=1}^n (p - \bar{p})^2}{n-1}} \quad (1)$$

$$u(p) = \frac{s}{\sqrt{n}} \quad (2)$$

102 Where,

103  $s$  = Standard deviation of sample

104  $p$  = Parameter (width, thickness, force, or tensile strength) of sample

105  $\bar{p}$  = Average parameter

106  $n$  = Number of sample

107  $u(p)$  = Standard uncertainty of parameter

108 **Table 2.** Standard deviation and standard uncertainty values of width, thickness,  
 109 force and tensile strength for the PC samples.

Parameter	Standard deviation	Standard uncertainty
Width (mm)	0.047	0.021

Thickness (mm)	0.009	0.004
Force (N)	14.496	6.483
Tensile strength (MPa)	0.258	0.116

110 The expanded uncertainty of calibrated micrometer has been obtained from accredited  
 111 laboratory namely Calibration and Measurement Centre, Vitar-Segatec Sdn. Bhd., whereas  
 112 the expanded uncertainty for the universal testing machine has been procured from Instron  
 113 Calibration Laboratory, National Voluntary Laboratory Accreditation Program. The  
 114 expanded uncertainty values of calibrated micrometer and universal testing machine (tension  
 115 value) are indicated in Table 3. The standard uncertainties of equipment specifically  
 116 micrometer and universal testing machine have been calculated according to Equation 3. The  
 117 divisor values for each parameter are equal to 2 because of their confidence level is 95% and  
 118 their distribution type is normal [8] as shown in calibration certificate of equipment. The  
 119 standard uncertainty values of micrometer and universal testing machine are also  
 120 demonstrated in Table 3. From the acquired results, it is indicated that the standard  
 121 uncertainty values of equipment are thoroughly dependent on the expanded uncertainty  
 122 values of calibrated equipment.

$$u(e) = \frac{U(e)}{K} \quad (3)$$

123 Where,

124  $u(e)$  = Standard uncertainty of calibrated equipment (micrometer or universal testing  
 125 machine)

126  $U(e)$  = Expanded uncertainty of calibrated equipment

127  $K$  = Divisor of parameter

128 **Table 3.** Expanded uncertainty and standard uncertainty values of micrometer and  
 129 universal testing machine for the tensile test results.

Equipment	Expanded uncertainty	Standard uncertainty
Micrometer (mm)	0.002	0.001
Universal testing machine, tension (N)	$1.1 \times 10^{-3}$	$5.5 \times 10^{-4}$

130 The average tensile strength of tested samples is actually calculated by using Equation 4.  
 131 On the other hand, the partial derivative of the average tensile strength with respect to the  
 132 average parameter (width, thickness or force) yields the sensitivity coefficient [9] as showed  
 133 in Equation 5. The sensitivity coefficients of width, thickness and force can be directly  
 134 computed according to Equation 6, 7 and 8, respectively. The calculated sensitivity  
 135 coefficient values of width, thickness and force for the PC samples are demonstrated in Table  
 136 4. Besides that, the sensitivity coefficients of calibrated micrometer and universal testing  
 137 machine are calculated based on Equation 9. The computed sensitivity coefficient values of  
 138 calibrated micrometer and universal testing machine are also indicated in Table 4. The  
 139 degrees of freedom for the width, thickness and force are computed according to Equation 10,  
 140 while the degree of freedom values of calibrated micrometer and universal testing machine  
 141 are commonly regarded as much as  $10^{13}$ . The calculated degree of freedom values for the  
 142 width, thickness and force are demonstrated in Table 4 as well.

$$\bar{\sigma}_{TS} = \frac{\bar{F}}{A} = \frac{\bar{F}}{wt}, \quad (4)$$

143 Where,

144  $\bar{\sigma}_{TS}$  = Average tensile strength

145  $\bar{F}$  = Average force

146  $\bar{A}$  = Average area

147  $\bar{w}$  = Average width

148  $\bar{t}$  = Average thickness

$$c_p = \frac{\partial \bar{\sigma}_{TS}}{\partial p}, \quad (5)$$

149 Where,

150  $c_p$  = Sensitivity coefficient of parameter (width, thickness or force)

151  $\partial \bar{\sigma}_{TS}$  = Differentiation of average tensile strength

152  $\partial p$  = Differentiation of average parameter

$$c_w = \frac{\partial \bar{\sigma}_{TS}}{\partial w} = -\frac{\bar{F}}{w^2 t} = -\frac{\bar{\sigma}_{TS}}{w}, \quad (6)$$

$$c_t = \frac{\partial \bar{\sigma}_{TS}}{\partial t} = -\frac{\bar{F}}{wt^2} = -\frac{\bar{\sigma}_{TS}}{t}, \quad (7)$$

$$c_F = \frac{\partial \bar{\sigma}_{TS}}{\partial F} = \frac{1}{wt} = \frac{\bar{\sigma}_{TS}}{F}, \quad (8)$$

153 Where,

154  $c_w$  = Sensitivity coefficient of sample width

155  $c_t$  = Sensitivity coefficient of sample thickness

156  $c_F$  = Sensitivity coefficient of sample force

157  $\partial \bar{w}$  = Differentiation of average width

158  $\partial \bar{t}$  = Differentiation of average thickness

159  $\partial \bar{F}$  = Differentiation of average force

$$c_e = \frac{\partial y}{\partial x}, \quad (9)$$

160 Where,

161  $c_e$  = Sensitivity coefficient of calibrated equipment (micrometer or universal testing  
 162 machine)

163  $\partial y$  = Change in output of equipment

164  $\partial x$  = Change in input of standard

$$v_p = n - 1, \tag{10}$$

165 Where,

166  $v_p$  = Degree of freedom for parameter (width, thickness or force)

167  $n$  = Number of sample

168 **Table 4.** Sensitivity coefficient and degree of freedom values for width, thickness,  
 169 force, micrometer and universal testing machine of the tensile test results.

Sources of uncertainty	Sensitivity coefficient	Degree of freedom
Width	-4.454 (N mm <sup>-3</sup> )	4
Thickness	-19.587 (N mm <sup>-3</sup> )	4
Force	0.025 (mm <sup>-2</sup> )	4
Micrometer	1 (N mm <sup>-3</sup> )	10 <sup>13</sup>
Universal testing machine	1 (mm <sup>-2</sup> )	10 <sup>13</sup>

170 The uncertainty contributions of parameter and calibrated equipment have been  
 171 calculated using standard uncertainty and sensitivity coefficient in accordance with Equation  
 172 11, and the values of uncertainty contribution for the width, thickness, force, micrometer and  
 173 universal testing machine are tabulated in Table 5. On the other hand, the combined  
 174 uncertainties for parameter and equipment can be computed by squaring the uncertainty  
 175 contribution of width, thickness, force, micrometer and universal testing machine (Equation  
 176 12), and the values of calculated combined uncertainty for each parameter and equipment are  
 177 also indicated in Table 5. On top of that, the combined standard uncertainty and effective  
 178 degree of freedom for the tensile strength can be computed based on Equation 13 and 14,  
 179 respectively. Aside from that, the coverage factor for effective degree of freedom has been  
 180 determined through Student's T-distribution table at 95% confidence level. The values of  
 181 combined standard uncertainty, effective degree of freedom and coverage factor are displayed  
 182 in Table 6. From the computation, it can be seen that the values of combined standard  
 183 uncertainty and effective degree of freedom are certainly dependent on uncertainty  
 184 contribution of parameter or equipment. Finally, the expanded uncertainty of the tensile  
 185 strength can be calculated by multiplying the combined standard uncertainty with the  
 186 coverage factor (Equation 15). The value of calculated expanded uncertainty is also  
 187 demonstrated in Table 6. From the obtained value, the standard uncertainty values of the  
 188 tested PC samples and the expanded uncertainty values of the equipment used have clearly  
 189 influenced the expanded uncertainty value of the tensile strength.

$$u_{con} = uc, \tag{11}$$

$$u_{com} = u_{con}^2, \tag{12}$$

$$u_c = \sqrt{\sum u_{com}^2}, \quad (13)$$

$$v_{eff} = \frac{u_{con}^4}{\sum u_{com}^4 / v}, \quad (14)$$

$$U(TS) = u_c k, \quad (15)$$

190 Where,

191  $u_{con}$  = Uncertainty contribution of parameter or equipment

192  $u$  = Standard uncertainty of parameter or equipment

193  $c$  = Sensitivity coefficient of parameter or equipment

194  $u_{com}$  = Combined uncertainty of parameter or equipment

195  $u_c$  = Combined standard uncertainty of tensile strength

196  $v_{eff}$  = Effective degree of freedom for tensile strength

197  $v$  = Degree of freedom for parameter or equipment

198  $U(TS)$  = Expanded uncertainty of tensile strength

199  $k$  = Coverage factor for effective degree of freedom

200 **Table 5.** Uncertainty contribution and combined uncertainty values of width,  
201 thickness, force, micrometer and universal testing machine for the tensile test results.

Sources of uncertainty	Uncertainty contribution (N mm <sup>-2</sup> )	Combined uncertainty (N <sup>2</sup> mm <sup>-4</sup> )
Width	-0.094	0.009
Thickness	-0.075	0.006
Force	0.163	0.026
Micrometer	0.001	10 <sup>-6</sup>
Universal testing machine	5.5 x 10 <sup>-4</sup>	3.0 x 10 <sup>-7</sup>

202 **Table 6.** Combined standard uncertainty, effective degree of freedom, coverage  
203 factor and expanded uncertainty of the tensile strength.

Combined standard uncertainty (N mm <sup>-2</sup> )	Effective degree of freedom	Coverage factor	Expanded uncertainty (MPa)*
0.202	8.298	2.306	0.467

204 \*MPa = N mm<sup>-2</sup>

205 3.2. Flexural strength

206 For the flexural test, there are some additional sources of uncertainty that can be  
 207 identified which are also from the tested PC samples and the measuring equipment used. For  
 208 the PC samples, the additional source of uncertainty is the length of support span, whilst the  
 209 additional source of uncertainty for the measuring equipment is calibrated caliper. On the  
 210 other hand, the length of support span was obtained by multiplying the thickness of each  
 211 sample with 16 (Equation 16). Besides that, the crosshead speed was calculated according to  
 212 Equation 17. The measured width and thickness of the rectangular-shaped PC samples values  
 213 and the length of support span values with their calculated averages are displayed in Table 7.  
 214 In addition, the values of acquired force and flexural strength for the PC samples with their  
 215 computed averages are also exhibited in Table 7.

$$l = 16t, \tag{16}$$

$$s = \frac{0.01l^2}{6t}, \tag{17}$$

216 Where,

217  $l$  = Length of support span

218  $t$  = Thickness of sample

219  $s$  = Crosshead speed

220 **Table 7.** Width, thickness, length of support span, force, flexural strength and their  
 221 averages for the PC samples.

No. of sample	Width (mm)	Thickness (mm)	Length (mm)	Force (N)	Flexural strength (MPa)
1	12.469	3.162	50.600	160.008	97.415
2	12.476	3.160	50.560	160.487	97.699
3	12.472	3.184	50.940	161.364	97.515
4	12.463	3.158	50.530	159.899	97.508
5	12.463	3.171	50.740	159.796	97.050
<b>Average</b>	12.469	3.167	50.674	160.311	97.437

222 The standard deviations were calculated to determine the standard uncertainties as  
 223 mentioned earlier. The standard deviations and standard uncertainties of width, thickness,  
 224 length of support span, force and flexural strength of the PC samples have also been  
 225 computed based on Equation 1 and 2, respectively. The standard deviation and standard  
 226 uncertainty values for the width, thickness, length of support span, force and flexural strength  
 227 of five PC samples measured are presented in Table 8. From the attained results, it is  
 228 obviously implied that the standard uncertainty values are also directly proportional to the  
 229 standard deviation values, which is the same trend with the tensile strength results.

230 **Table 8.** Standard deviation and standard uncertainty values of width, thickness,  
 231 length of support span, force and flexural strength for the PC samples.

Parameter	Standard deviation	Standard uncertainty
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Width (mm)	0.006	0.003
Thickness (mm)	0.011	0.005
Length (mm)	0.169	0.076
Force (N)	0.645	0.289
Flexural strength (MPa)	0.240	0.107

232 The expanded uncertainties of calibrated micrometer, caliper and universal testing  
 233 machine have been procured from the same accredited laboratories that are mentioned above.  
 234 The expanded uncertainty values of calibrated micrometer, caliper and universal testing  
 235 machine (compression value) are demonstrated in Table 9. The standard uncertainties of  
 236 calibrated equipment specifically micrometer, caliper and universal testing machine have also  
 237 been calculated according to Equation 3. Moreover, the divisor values for each parameter are  
 238 equal to 2 due to their confidence level is 95% and their distribution type is normal as well.  
 239 The standard uncertainty values of micrometer, caliper and universal testing machine are also  
 240 displayed in Table 9. From the results, it is clearly showed that the standard uncertainties of  
 241 calibrated equipment are dependent on their expanded uncertainties as well.

242 **Table 9.** Expanded uncertainty and standard uncertainty values of micrometer,  
 243 caliper and universal testing machine for the flexural test results.

Equipment	Expanded uncertainty	Standard uncertainty
Micrometer (mm)	0.002	0.001
Caliper (mm)	0.010	0.005
Universal testing machine, compression (N)	$1.7 \times 10^{-3}$	$8.5 \times 10^{-4}$

244 The average flexural strength of tested PC samples is frequently computed according to  
 245 Equation 18. The sensitivity coefficients of width, thickness, length of support span and force  
 246 can be straightly calculated by using Equation 19, 20, 21 and 22, respectively. The computed  
 247 sensitivity coefficient values for the width, thickness, length of support span and force of the  
 248 PC samples are demonstrated in Table 10. The sensitivity coefficients of calibrated  
 249 micrometer, caliper and universal testing machine are also calculated based on Equation 9.  
 250 The computed sensitivity coefficient values of the calibrated equipment are indicated in Table  
 251 10 as well. The degrees of freedom for the width, thickness, length of support span and force  
 252 are also calculated according to Equation 10, whereas the degree of freedom values for the  
 253 calibrated micrometer, caliper and universal testing machine are regarded as much as  $10^{13}$  as  
 254 well. The computed degree of freedom values for the width, thickness, length of support span  
 255 and force are also demonstrated in Table 10.

$$\bar{\sigma}_{FS} = \frac{3\bar{F}\bar{l}}{2wt^2}, \tag{18}$$

256 Where,

257  $\bar{\sigma}_{FS}$  = Average flexural strength

258  $\bar{F}$  = Average force

259  $\bar{l}$  = Average length of support span

260  $\bar{w}$  = Average width

261  $\bar{t}$  = Average thickness

$$c_w = \frac{\partial \bar{\sigma}_{FS}}{\partial \bar{w}} = -\frac{3\bar{F}\bar{l}}{2\bar{w}^2\bar{t}^2} = -\frac{\bar{\sigma}_{FS}}{\bar{w}}, \quad (19)$$

$$c_t = \frac{\partial \bar{\sigma}_{FS}}{\partial \bar{t}} = -\frac{3\bar{F}\bar{l}}{\bar{w}^2\bar{t}^3} = -\frac{2\bar{\sigma}_{FS}}{\bar{t}}, \quad (20)$$

$$c_l = \frac{\partial \bar{\sigma}_{FS}}{\partial \bar{l}} = \frac{3\bar{F}}{2\bar{w}\bar{t}^2} = \frac{\bar{\sigma}_{FS}}{\bar{l}}, \quad (21)$$

$$c_F = \frac{\partial \bar{\sigma}_{FS}}{\partial \bar{F}} = \frac{3\bar{l}}{2\bar{w}\bar{t}^2} = \frac{\bar{\sigma}_{FS}}{\bar{F}}, \quad (22)$$

262 Where,

263  $c_w$  = Sensitivity coefficient of sample width

264  $c_t$  = Sensitivity coefficient of sample thickness

265  $c_l$  = Sensitivity coefficient of length of support span

266  $c_F$  = Sensitivity coefficient of sample force

267  $\partial \bar{w}$  = Differentiation of average width

268  $\partial \bar{t}$  = Differentiation of average thickness

269  $\partial \bar{l}$  = Differentiation of average length of support span

270  $\partial \bar{F}$  = Differentiation of average force

271 **Table 10.** Sensitivity coefficient and degree of freedom values for width, thickness,  
 272 length of support span, force, micrometer, caliper and universal testing machine of  
 273 the flexural test results.

Sources of uncertainty	Sensitivity coefficient	Degree of freedom
Width	-7.815 (N mm <sup>-3</sup> )	4
Thickness	-61.533 (N mm <sup>-3</sup> )	4
Length	1.923 (N mm <sup>-3</sup> )	4
Force	0.608 (mm <sup>-2</sup> )	4
Micrometer	1 (N mm <sup>-3</sup> )	10 <sup>13</sup>
Caliper	1 (N mm <sup>-3</sup> )	10 <sup>13</sup>
Universal testing machine	1 (mm <sup>-2</sup> )	10 <sup>13</sup>

274 The uncertainty contributions of parameter and calibrated equipment have also been  
 275 calculated by means of standard uncertainty and sensitivity coefficient in accordance with  
 276 Equation 11. The values of uncertainty contribution for the width, thickness, length of  
 277 support span, force, micrometer, caliper and universal testing machine are presented in Table  
 278 11. Besides that, the combined uncertainties of parameter and equipment can be computed by  
 279 squaring the uncertainty contribution of width, thickness, length of support span, force,  
 280 micrometer, caliper and universal testing machine (Equation 12). The values of calculated  
 281 combined uncertainty for each parameter and equipment are indicated in Table 11 as well.  
 282 The combined standard uncertainty and effective degree of freedom for the width, thickness,  
 283 length of support span, force, micrometer, caliper and universal testing machine can also be  
 284 computed based on Equation 13 and 14, respectively. The coverage factor for effective  
 285 degree of freedom has been determined through Student’s T-distribution table at 95%  
 286 confidence level. The values of combined standard uncertainty, effective degree of freedom  
 287 and coverage factor were displayed in Table 12. From the computation, it can be seen that the  
 288 values are also dependent on combined uncertainty of parameter or equipment. On the other  
 289 hand, the expanded uncertainty of the flexural strength can be computed by using Equation  
 290 15. The value of calculated expanded uncertainty is indicated in Table 12 as well. From the  
 291 attained value, it is clearly implied that the value of expanded uncertainty of the flexural  
 292 strength was also influenced by the standard uncertainty values of the tested PC samples and  
 293 the expanded uncertainty values of the equipment used.

294 **Table 11.** Uncertainty contribution and combined uncertainty values of width,  
 295 thickness, length of support span, force, micrometer, caliper and universal testing  
 296 machine for the flexural test results.

Sources of uncertainty	Uncertainty contribution (N mm <sup>-2</sup> )	Combined uncertainty (N <sup>2</sup> mm <sup>-4</sup> )
Width	-0.020	3.9 x 10 <sup>-4</sup>
Thickness	-0.295	0.087
Length	0.145	0.021
Force	0.175	0.031
Micrometer	0.001	10 <sup>6</sup>
Caliper	0.005	2.5 x 10 <sup>-5</sup>
Universal testing machine	8.5 x 10 <sup>-4</sup>	7.2 x 10 <sup>-7</sup>

297 **Table 12.** Combined standard uncertainty, effective degree of freedom, coverage  
 298 factor and expanded uncertainty of the flexural strength.

Combined standard uncertainty (N mm <sup>-2</sup> )	Effective degree of freedom	Coverage factor	Expanded uncertainty (MPa)*
0.330	5.876	2.447	0.806

299 \*MPa = N mm<sup>-2</sup>

300 **4. Conclusions**

301 From this study, it can be perceived that the dumbbell-shaped PC samples have the  
 302 average tensile strength value of 58.978 ± 0.258 MPa, whereas the average flexural strength  
 303 value for the rectangular-shaped PC samples is 97.437 ± 0.240 MPa. Based on the obtained

304 values, at a confidence level of 95%, the calculated expanded uncertainty of tensile strength  
305 is 0.467 MPa. On top of that, at the same confidence level (95%), the calculated expanded  
306 uncertainty of flexural strength is 0.806 MPa. In conclusion, the standard uncertainty values  
307 of the tested samples and the expanded uncertainty values of the equipment used have  
308 obviously influenced the expanded uncertainty values of the measured tensile strength and  
309 flexural strength of the PC samples.

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