Determination of Cross Section for Different Fusion Reactions in Terms of Lattice Effects in Solid State Internal Conversion for Different metallic Crystalline Environments

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Abstract

In present paper, the cross section for D(d,p)T, $D(d,\gamma)^4He,T(d,n)^4He$ and $D(p,\gamma)^3He$ fusion reactions in 6 7 terms of the lattice effect in solid state internal conversion for different structures and different metallic crystalline 8 environments in comparison with palladium environment has been determined. Elements that we used in this 9 article are Ni, Ru, Rh, Pt, Ta, Ti, Zr, which arecontained FCC, BCC and HCP lattice structures. Fusionable particles are solved as a sublattice in mentioned crystalline metals. Fusion reactions are 10 generated by flux of incoming fusionable particles. We took lattice effect part into our calculations with 11 regarding the Bloch function for the initial and final state of three body system. Three body system 12 involved the host lattice, sublattice and incident particles. The cross section for performing each fusion 13 14 reaction inside different metal is computed using the state of initial and final system. Then our resultsfor 15 cross section of different metal are compared with palladium metal. Finally, the solid state internal 16 conversion coefficient is obtained by considering the lattice effect.

17 *Key words*: internal conversion ,fusion ,lattice ,deuterium

18 **1. Introduction**

19 Nowadays using nuclear energy is very important as a clean source of energy. There are two

20 kinds of nuclear reactions, fusion and fission. Since fusion reaction has less radioactive radiation

and the fusion fuels required for these reactions are more sufficiently available in the nature,

22 therefore fusion reactions are important to study.

23 The ability of palladium to absorb hydrogen was recognized as early as the nineteenth century by Thomas Graham [1]. In the late 1920s, two Austrian born scientists, Friedrich Paneth and Kurt 24 25 Peters, originally reported the transformation of hydrogen into helium by spontaneous nuclear 26 catalysis when hydrogen was absorbed by finely divided palladium at room temperature [1,2].In 27 1927, Swedish scientist J. Tandberg stated that he had fused hydrogen into helium in an 28 electrolytic cell with palladium electrodes [1]. On the basis of his work, he applied for a Swedish 29 patent for "a method to produce helium and useful reaction energy". After deuterium was 30 discovered in 1932, Tandberg continued his experiments with heavy water [1]. The term "cold fusion" was used as early as 1956 in a New York Times article about Luis W. Alvarez's work on 31 muon-catalyzed fusion [4]. Jones had worked for some time on muon-catalyzed fusion, a known 32 method of inducing nuclear fusion without high temperatures, and had written an article on the 33 topic entitled "Cold nuclear fusion" that had been published in Scientific American in July 1987 34 35 [5]. In 1985, many years after Pons and Fleischmann separation, Fleischmann continued his researches and published many articles [5]. In 1988, Fleischmann and Pons applied to the United 36 States Department of Energy for funding towards a larger series of experiments. Up to this point 37

they had been funding their experiments using a small device built with \$100,000 out-of-pocket 38 [5]. In 1989, Fleischmann and Pons published the result of their experiments which showed the 39 approval of the cold fusion in several papers. [6] (Other scientists' works were also published 40 [7]). In 1989, observations of Stanley Pons and Martin Fleischmann about fusion in room 41 42 temperature gained a lot of attention [8]. After that the word "cold fusion" used for low-energy nuclear reactions (LENR)[9]. In September 1990 the National Cold Fusion Institute listed 92 43 groups of researchers from 10 different countries that had reported corroborating evidence of 44 excess heat [10]. From 1990 to 2008, special researches were done in this field in India [11]. In 45 1991, the failure of all the experiments and researches were declared [12]. In 1 January 1991, 46 Pons left his tenure, and both he and Fleischmann quietly left the United States [13,14]. In 1992 47 they resumed research with Toyota Motor Corporation's IMRA lab in France [13]. Fleischmann 48 left for England in 1995, and the contract with Pons was not renewed in 1998 after spending \$40 49 million with no tangible results. The IMRA laboratory was closed in 1998 after spending £12 50 51 million on cold fusion work. Pons has made no public declarations since, and only Fleischmann continues giving talks and publishing papers [15]. In 1995, many experimental works is done on 52 gaseous metals for determining screening effect [16]. From 1998 to 2001, these experiments 53 continued on metallic environments [17-19]. In 1999 the Japan C-F Research Society was 54 55 established to promote the independent research into cold fusion that continued in Japan [20]. The society holds annual meetings; the 12th meeting took place on December 17-18, 2011 at 56 Kobe University [21]. In 2000, the electron screening effect on cold fusion reaction was studied 57 for D + D in the metallic environment [9]. In 2002, they released a two-volume report, "Thermal 58 and nuclear aspects of the Pd/D₂O system," with a plea for funding [22]. In 2002, the 59 60 enhancement of cold fusion and solid state effect were studied in deuterated metal for D+D [23]. From 2002 to 2004, the screening effect on 50 metals and insulator is checked by series of 61 experiments [24-26]. In 2003, the enhancement of deuteron-fusion reactions in metals and 62 experimental implications were studied for electron screening effect [27]. In 2004, the subject of 63 solid state internal conversion came up [28]. And DOE review started again [29]. In 2005, many 64 efforts were done to make an apparatus according to the Fleischmann and pons' works, finally, 65 Cold fusion apparatus was made at San Diego Space and Naval Warfare Systems Center. They 66 used other names instead of cold fusion to reduce the effect of previous failures. Often they prefer 67 68 to name their field Low Energy Nuclear Reactions (LENR) or Chemically Assisted Nuclear 69 Reactions (CANR), also Lattice Assisted Nuclear Reactions (LANR), Condensed Matter Nuclear Science (CMNS) and Lattice Enabled Nuclear Reactions [30-33]. 70

In 2007, the Naval Research Laboratory published a literature review explaining why most researchers have usually been unable to replicate successful LENR experiments, saying that the loading ratio of gas to metal was the most crucial aspect, which can be affected by metal properties, cell configuration, and the experimental protocols [34]. In 2007, nuclear physicist and engineering professor Jean-Paul Biberian published an update surveying the previous 15 years of work, stating that nuclear reactions which are not predicted by current theories have been proven [35].

In 2002, Peter Kalman and Thomas Keszthelyi studied this problem on different metals. 78 They studied many different factors to explain the enhancement of cross section. For example, 79 the electron screening was checked for 29 deuterated metals and 5 deuterated 80 insulators/semiconductors from periodic tables. Among them, metals were most convenient. 81 82 Some of the other factors that they considered were: stopping power, thermal motion, channeling, diffusion, conductivity, and crystal structure and electron configuration. None of 83 them could explain the observed enhanced cross section [23, 25, 27, 36-38]. In 2004, they found 84 a reason to explain the enhancement of cross section that was called solid state internal 85 conversion [28]. In 2008, screening effect is studied for the first time on metals by considering 86 87 solid state; actually solid state of metals is expressed in experiments [39]. Finally, in 2009, they considered a metal with its lattice structure and entered the lattice shape of the solid in their 88 internal conversion calculations [40]. Their calculations were just for $D(p,\gamma)^3$ He reaction. 89

Here different metals are considered. We choose such metals that are shown the best results in term of screening effect and the density of deuterium [41]. In this article, for comparing internal conversion and lattice effect in solid state internal conversion, we calculate cross section for different seven particles in plus palladium for $D(p,\gamma)$ 3He , D(d,p)T , $D(d,\gamma)$ 4He , T(d,n)4He .

94 The aim of this work is determination of fusion cross section for different reactions in different metallic environments regarding the lattice effect in solid state internal conversion (LEISSIC). 95 For approaching to this aim we studied on the different steps that are followed by: in the first 96 step right after introduction, the aspects of IC, SSIC and LEISSIC are explained. In second step, 97 different special lattice such as FCC, BCC and HCP are introduced in details. In third step, 98 LEISSIC and other required quantities for determining FCS and LEISSIC coefficient for Pd 99 environment are computed. In fourth step, all calculations in the previous step are repeated for 100 Ni, Ru, Rh, Pt, Ta, Ti, Zr. In fifth step, microscopic FCS for all elements are determined in 101 different reaction for element host particle. Finally, in the sixth step, we can suggest the best kind 102 of lattice, fusion reaction and metallic environment which have high value LEISSIC when cold 103 fusion happening. 104

2. Internal Conversion (IC) and Solid State Internal Conversion (SSIC)

106 **Internal conversion** is a radioactive decay process where an excited nucleus interacts with an electron in one of the lower atomic orbitals, causing the electron to be emitted from the atom. 107 Thus, in an internal conversion process, a high-energy electron is emitted from the radioactive 108 atom, but without beta decay taking place. For this reason, the high-speed electrons from internal 109 conversion are not beta particles (β particles), since the latter come from beta decay. Since no 110 111 beta decay takes place in internal conversion, the element atomic number does not change, and 112 thus (as is the case with gamma decay) no transmutation of one element to another is seen. Also, no neutrino is emitted in internal conversion. 113

Internally converted electrons do not have the characteristic energetically-spread spectrum of β particles, which results from varying amounts of decay-energy being carried off by the neutrino (or antineutrino) in beta decay. Internally converted electrons, which carry a fixed fraction of the characteristic decay energy, have a well-specified discrete energy. The energy spectrum of a β particle is thus a broad hump, extending to a maximum decay energy value, while the spectrum of internally converted electrons is a sharp peak.



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Figure 1: Internal conversion

In the internal conversion process, the wave function of an inner shell electron penetrates the nucleus (i.e. there is a finite probability of the electron in an s-atomic orbital being found in the nucleus) and when this is the case, the electron may couple to the excited state and take the energy of the nuclear transition directly, without an intermediate gamma ray being produced first.

Most internal conversion electrons come from the K shell (1s state, see electron shell), as these two electrons have the highest probability of being found inside the nucleus. After the electron has been emitted, the atom is left with a vacancy in one of the inner electron shells. This hole will be filled with an electron from one of the higher shells and subsequently a characteristic x-ray or Auger electron will be emitted [9].

132 Scientists first examined different environments; among them, the deuterated metallic environments were the best to be a host environment for cold fusion. At first they studied the 133 gaseous metals, and then they considered the target as a solid. Comparing the results of these 134 experiments with the results obtained with gaseous targets extra fusion events were obtained. The 135 enhancement in the fusion rate is attributed to the presence of solid state material but up till now the 136 theoretical explanation of the phenomenon is still missing [42-44]. In what follows we suggest a possible 137 138 mechanism called solid state internal conversion process that should be considered when trying to 139 understand the extra fusion events. In "ordinary" nuclear physics the internal conversion process is a well140 known reaction in which a nuclear isomer loses its nuclear excitation energy by ejecting an electron of its

- 141 Surroundings (one of the atomic electrons) instead of by emitting radiation [45].
- 142 143

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[28].

Internal conversion process arises due to the electromagnetic interaction between the nucleon

and the electronic shell. A similar process can take place in a solid between fusionable nuclei and any charged particle in the crystal. The solid state internal conversion process counterparts of the $D(p,\gamma)^{3}$ He nuclear reaction -can be processes consisting of (a) a bound-free electron transition $p + d + (e) \rightarrow {}^{3}He +$ eand (b) a bound-free deuteron transition $p + d + (d) \rightarrow {}^{3}He + d$. Therefore, as internal conversion happened in solid environment in addition of electron channel we have deuterium channel too

We understood that in a solid (deuteroned pd) the interchange of light phonon results in an absorbent potential between semi-free fusionable particles(between semi-free deuterium). Absorption increases by relative increase of deuterium in the host material and may have eye catching effect on nuclear fusion rate in low temperature that is basically determined by strong colony repellence. It is shown that in a solid material, nuclear fusion reactions can happen in solid state internal conversion that creates transit for every charged particle by electromagnetic reaction [28].

3. Describing mentioned lattice in this article: FCC, BCC, HCP

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In this article, these elements are studied: Ni, Ru, Rh, Pt, Ta, Ti, Zr. Which, Ni, Pt, Rh have aFCC lattice such as Pd. Ru, Ti, Zr have a hexagonal lattice and the lattice of Ta is BCC.

After investigating prior experimental work, finally in 2008 solids are considered without 161 their lattice crystal [39]. Then, in 2009 calculations are continued for Pd and with regarding the 162 crystalline lattice [40]. Before study on solid state internal conversion the scientists examined 163 screening effect on metals to finding the reasons of the enhancement FCS of metals which was 164 observed[41].In this article chosen element are significant in screening effect or deuterium 165 density. For example, Ti and Zr showed the most screening potential in the experiments [27]. Ta 166 and Zr had the most solved deuterium density [41]. Whereas having a maximum deuterium 167 density in Ti depends on having high temperature [28]. 168

The most important quantities that change during calculations are unit cell volume and the number of atom that belongs to each kind of lattice. Those quantities are explained for each lattice that is following.

In each unit cell of FCC and BCC lattice, eight atoms stand on the corner of cubic that are collaborative between eight other closed cubic (Fig 2, a_1 and a_2),thus, each unit cell has one atom from corners ($8 \times \frac{1}{8} = 1$). For FCC there is one atom which belongs to two closed cubic but for BCC one atom locates in the center of each unit cell. So, FCC and BCC lattice have respectively 3 atoms from all 6 sites ($6 \times \frac{1}{2} = 3$) and one atom from its center. Therefore, FCC and BCC have four(1 + 3 = 4) and two (1 + 1 = 2) atoms for each unit cell respectively. HCP lattice: In each unit cell of HCP (see fig.2,a₃), there are two atoms on the top and down sides that are shared between two closed unit cells $\left(2 \times \frac{1}{2} = 1\right)$, on the other sides of the unit cell there are six atoms. Each atom belong two closed unit cells $\left(6 \times \frac{1}{2} = 3\right)$. There are twelve atoms in the corners that are collaborating between three closed unit cells $\left(12 \times \frac{1}{3} = 4\right)$. Consequently, there are eight atoms that are completely belonging to one unit cell. In this lattice there are two lattice constants: c height of unit cell and a, the face of hexagonal.

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Figure 2: Shape of unit cell; a₁: FCC unit cell, a₂: BCC unit cell, a₃:HCP unit cell.



$$v_{cell} = \begin{cases} \frac{a^3}{4} & FCC\\ \frac{a^3}{2} & BCC\\ \frac{3\sqrt{3}}{16}a^2c & HCP \end{cases} , (a,c:lattice constant)$$
(31)

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195 4. Lattice Effect in Solid State Internal Conversion

196 **4.1. Cross section theory of LEISSIC**

Since particles in the crystal are placed in specific sites, we can estimate fusion cross section (FCS) reactions using Block theorem for describing initial and final states of this system (palladium environment). In all formulas subscripts 1, 2 and 3 are respectively pointed at incoming, sublattice and host particles. Also, the state of particles in the lattice is determined by Block function [47]

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$$\varphi_{k_{3,i}}(r_3) = \frac{1}{\sqrt{N}} \sum_{l_s} e^{ik_{3,i} \cdot l_s} a_3(r_3 - l_s - u_3(l_s))(1)$$

where, r_3 , $k_{3,I}$ and a_3 are respectively introduced host-particle coordinate, a wave vector of the first Brillouan zone of the reciprocal lattice, and Wannier function. Here, Pd (palladium), d (duetron) and e (electron) are considered as host particles. Lattice site and the displacement of the atom located at lattice site are symbols to represent l_s and $u_3(l_s)$. Here N is the number of lattice point. The sublattice particle also is described by Block function (Eq 2). Lattice contains N_2 fusionable particles, for palladium system it is assumed that $N_2 = N$.

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$$\varphi_{k_{2,i}}(r_2) = \frac{1}{\sqrt{N_2}} \sum_{l_s} e^{ik_{2,i} \cdot l_s} a_2 (r_2 - l_s - u_2(l_s)) (2)$$

210 Here, a_2 and a_3 are Wannier functions for sublattice and host particles respectively that are

211 determinated by equation 3[]

$$a_j(x) = \left(\frac{\beta_j^2}{\pi}\right)^{3/4} e^{-\frac{\beta_j^2}{2}x^2} (x = r_2 - l_s), j = 2,3$$
(3)

In the above formula, $\beta_j = \sqrt{m_j \omega_j / \hbar}$ [22]. The initial state Ψ_i for the three particles that participate in solid state assisted fusion reaction is described by,

214
$$\Psi_i = \varphi_{k_{2,i}}(r_2)\varphi_{k_{3,i}}(r_3)\varphi_1(r_1 - r_2)(4)$$

where, $\varphi_1(r_1 - r_2)$ is the Coulomb wave function corresponding to the state of a sublattice and incoming particle. The Coulomb wave function is[],

$$\varphi_1(r_1 - r_2) = e^{ik_1 \cdot (r_1 - r_2)} \frac{f(k_1, r_1 - r_2)}{\sqrt{V}}$$
(5)

V is the volume of normalization, k_1 is the wave vector, r_1 is the coordinate of incoming particle, and f function is defined as the following:

219 $f(k_1, x) = e^{-\pi\eta/2} \Gamma(1 + i\eta) {}_1F_1(-i\eta, 1; i[k_1x - k_1 \cdot x])(6) {}_1F_1$ Is the confluent hyper geometric 220 function [19]. η is determined by using the eq. 7 and 8 [46].

$$\eta = 0.1575 \, z_1 z_2 \left(\frac{A}{E}\right)^{1/2} (7)$$

$$A = \frac{A_1 A_2}{A_1 + A_2} (amu) \tag{8}$$

221 Where z_1 and z_2 are the charge number of particles 1 and 2 and E is the energy of incoming

- 222 particle. A_1 and A_2 are the mass of incident and sublattice particles that are measured in amu unit.
- The final state of this three- body system is defined by,

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$$\Psi_f = \psi_f(r_1, r_2)\varphi_f(r_3)F_{Cb}(z_3, z_{12}, v_{3,12})$$
(9)

225 Where φ_f is a plane wave of wave vector k_3 that is corresponded to an outgoing particle 3.

$$\varphi_f(r_3) = \frac{1}{\sqrt{V}} e^{ik_3 \cdot r_3} \tag{12}$$

226 ψ_f stands for the outgoing fusion product leaving a deuteron lattice point vacant that is given in

the relative coordinate $(r = r_1 - r_2)$ and the center of mass coordinate $(R = m_1r_1 + m_2r_2/m)$ of the particles of the rest masses m_1 and m_2 , then we have

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$$\psi_f(r,R) = \frac{1}{\sqrt{V}} e^{iK.R} \chi(r)$$
 (13)

230 Where K and $\chi(r)$ are the wave vector of fusion product and a nuclear wave function, 231 respectively.

$$\chi(r) = \left(\frac{\lambda^2}{\pi}\right)^{3/4} e^{-\lambda^2 r^2/2} \tag{14}$$

(16)

We determine the Coulomb interaction between host particle and the product of the incident and sublattice reaction using the Fermi correction;

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$$F_{Cb} = \sqrt{2\pi\xi} \frac{e^{-\pi\xi}}{\sqrt{1 - e^{-2\pi\xi}}}$$
 (15)

235 Where, $\xi = z_3 z_{12} \alpha_f \sqrt{\mu c^2/2Q}$ and α_f is the fine structure constant. μ is the reduced mass $\mu = \frac{(m_1 + m_2)m_3}{m_1 + m_2 + m_3}$

the element of s-matrix that is used for determining of the cross section of the different fusion

237 reaction is known as,

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$$S_{fi} = \frac{2\pi}{i\hbar} \iiint \Psi_f^* \frac{z_1 z_3 e^2}{|r_1 - r_3|} \Psi_i d^3 r_1 d^3 r_2 d^3 r_3 \delta(E/\hbar)$$
(17)

With a little simplification on this integral and using the Hatree-Fok approximation for Coulombinteraction part of integral, we have

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$$\frac{z_1 z_3 e^2}{|r_1 - r_3|} = \frac{z_1 z_3 e^2}{2\pi^2} \int d^3 q \, \frac{1}{q^2} e^{iq.(r_1 - r_2)}$$
(18)

242 Putting the Fourier transform of Eq.13 in Eq.16 , and applying the approximation 17 and

comparing it with $\langle \sigma v \rangle$ formula, the cross section of fusion reaction between host and target fusionable particles is obtained as the following,

$$\sigma_2 = C_0 \frac{\exp\left(-2\pi\eta\right)}{E} \tag{19}$$

E is the energy of incoming particle and C_0 is determined by,

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$$C_0 = |F_{Cb}|^2 A_0 k_\mu \left(\frac{\beta_2}{K_Q}\right)^3 \langle |\tilde{\chi}|_{K=K_Q}^2 \rangle_{\Omega_K}$$
(20)

247 With Ω_K denoting the solid angle in the K space, $\beta_2 = \sqrt{m_d \omega/\hbar}$, $A_0 = 128\alpha_f^3 z_1^3 z_3^2 z_2 m_1 c^2 \sqrt{\pi}$, 248 $K_Q = \sqrt{2\mu c^2 Q}/(\hbar c)$, Q is the energy of the reaction, $k_\mu = \mu c/\hbar$.

the average of nuclear wave function is defined by,

$$\langle |\tilde{\chi}|_{K=K_Q}^2 \rangle_{\Omega_K} = \left| \tilde{\chi} \left(\frac{m_2}{m} K \right) \right|^2 = \frac{8\pi^{3/2}}{\lambda^3} e^{-\frac{4K^2}{9\lambda^2}}$$
(21)

250 m_n, nucleons mass, ω_n angular frequent of binding energy are calculated for each reaction 251 separately (table 4).

$$\lambda = \frac{\sqrt{m_n \omega_n}}{\hbar} \tag{22}$$

$$m_n = m_i + m_{He}$$
, $i = d \text{ or } t$ (23)
hinding energy of $He(MeV)$

$$\omega_n = \frac{binding\ energy\ of\ He(MeV)}{\hbar} (24)$$

Here, C_0 is calculated for one d or one Pd. In order to compare C_0 with astrophysical factor (S(0)) in ordinary state, it must be calculated considering the density of these particles. So, we use the Eq.24

$$NC_0 = A\Delta R_h C_1 \tag{25}$$

255 In this case, N is defined by,

$$N(Pd) = V_{eff} / v_{cell}$$
(26)
Where $v_{cell} = d^3/4$, $V_{eff} = A\Delta R_h$ and $d = 3.89 \times 10^{-8} cm$ is the lattice constant
 $N(d) = u V_{eff} / v_{cell}$
(27)

In Eq.23, u is the ratio of deuteron to palladium number density. For electron u = 10 which is the number of electron valence in palladium. C_0 contains all the properties of the lattice. For comparison the fusion cross section with and without LEISSIC we have to determine the macroscopic cross section.

$$\Sigma = N\sigma_2 \tag{28}$$

4.2. Results of numerical calculations for each reaction

There are two tables for all reactions that can aid in plotting the cross section and comparing with the ordinary state. The suppositions of host, sublattice and incoming particles are expressed for all reactions in this way: the host particles are Pd,d,e for Palladium. The sublattice is deuterium for all reactions. The incoming particles are proton (p) in $D(p,\gamma)^{3}He$, deuterium (d) in D(d,p)T and $D(d,\gamma)^{4}He$ and tritium (t) in $T(d,n)^{4}He$. Our calculation for obtaining the cross section for all three kind of host particles are accomplished by using equations: 13,14,18,20 and our obtained results are given in tables 1 and 2.

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Table 1: our numerical calculation of necessary quantities for obtaining C_0 for all chosen reactions

Type of Reactions	host partic les	A ₀ (MeV)	μ(gr)	$K_Q(cm^{-1})$	$\frac{ \widetilde{\chi} _{K=K_Q}^2}{(cm^3)}$	Ę
	Pd	175	5.013×10^{-24}	8.91 × 10 ¹²	3.95×10^{-38}	10.755
D(p,y)3He	d	0.0827	2.005×10^{-24}	5.64×10^{12}	5.13×10^{-38}	0.1477
	e	0.0103		2.78×10^{11}	6.11×10^{-38}	-560382
	pd	349	6.686×10^{-24}	8.82×10^{12}	3.15×10^{-38}	14.462
D(d,p)T	d	0.165	2.229×10^{-24}	5.09×10^{12}	3.97×10^{-38}	0.181
	e	0.021	() of the second second	2.05×10^{11}	4.45×10^{-38}	-0.0011
	Pd	349	6.686×10^{-24}	7.93×10^{12}	3.69×10^{-38}	16.075
D(d, y)4He	d	0.165	2.229×10^{-24}	4.58×10^{12}	4.51×10^{-38}	0.202
	e	0.021		1.65×10^{11}	4.98×10^{-38}	-0.0022
T <mark>(d,n)4He</mark>	Pd	524	8.35×10^{-24}	2.05×10^{13}	2.89×10^{-39}	5.863
	d	0.248	2.387×10^{-24}	1.10×10^{13}	4.24×10^{-39}	0.09
	е	0.031		8.90×10^{11}	4.30×10^{-38}	-4.228

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From the results of table 1 and Eqs.18 and 28 for different reactions and host particle, we can

calculate the required parameters such as C_0 and C_1 which are important for estimating cross section of the fusion reactions.

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Table 2: our numerical calculation C_0 and C_1 for different host particle and different reactions

Type of Reactions	host parti cles	$\frac{k_{\mu}}{(cm^{-1})}$	$ F_{Cb} ^2$	C ₀ (MeV b)	C ₁ (MeV b)
	Pd	1.42×10^{14}	3.14×10^{-28}	4.92×10^{-38}	3.36×10^{-24}
D(p, y)3He	d	0.57×10^{14}	0.61	2.30×10^{-13}	u × 15.6
	e		1	9.10×10^{-13}	6.18×10^{2}
	Pd	1.90×10^{14}	3.27×10^{-38}	1.11×10^{-47}	7.53×10^{-34}
D(d,p)T	d	0.63×10^{14}	0.5371	1.88×10^{-13}	u × 12.78
	е		1	2.48×10^{-12}	1.687×10^{3}
	Pd	1.90×10^{14}	7.02×10^{-41}	3.83×10^{-50}	0.26×10^{-35}
D(d, y)4He	d	0.63×10^{14}	0.4964	2.70×10^{-13}	u × 18.35
01 (0.023)	е		1	4.31×10^{-36}	2.93×10^{-21}
T(d,n)4He	Pd	2.37×10^{14}	4.44×10^{-15}	2.05×10^{-25}	1.39×10^{-12}
	d	0.68×10^{14}	0.7438	4.45×10^{-15}	u × 0.3024
	e		1	1.87×10^{-13}	127.1

Since each palladium unit cell has 4 Pd atoms purely and since we suppose that the number of host and sublattice particles are equal, then we have

$$N_{Pd} = \frac{1}{4} \times 4.22 \times 10^{22} \tag{29}$$

289 The other quantities such as, m_n , $\beta 2$ and Q which is mentioned before are calculated and 290 numerical results are summarized in table 3.

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Table 3: our obtaining required quantities which are calculated for determination of different fusion

Type of Reactions	λ (cm ⁻¹)	$\beta_2(cm^{-1})$	Q (MeV)	Binding Energy (MeV)
$D(p,\gamma)^{3}He$	9 × 10 ¹²	4.81×10^{14}	5.49	7.718
D(d,p)T	10×10^{12}	4.81×10^{14}	4.04	<mark>8.48</mark> 2
$D(d,\gamma)^4$ He	9.63×10^{12}	4.81×10^{14}	3.27	28.3
T(d,n) ⁴ He	21.8×10^{12}	4.81×10^{14}	17.59	28.3

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4.3. Calculations the solid state internal conversion coefficient for different fusion reactions in Palladium crystal environment

With regarding to definition that exists in Ref.12, we can write $v_{eff} = A\Delta R_h$, where A is the cross section of the beam, ΔR_h is the "differential" range, that is, the distance within which the energy of the incoming particle can be considered unchanged. The $\Delta R_h \ll R_h$ condition helps in an order of magnitude estimate of ΔR_h , where R_h is the stopping range of a proton which is about $8 \times 10^{-2} \mu m$ at $E = 0.01 \, MeV$ in Pd [20]. The quantities A and R_h were measured in mm^2 and $10^{-3} \mu m$ units. The solid state internal conversion coefficient is introduced as,

$$\alpha_{SSIC} = A \Delta R_h C_1 / S(0) \tag{30}$$

S(0) is the astrophysical factor and the amounts of S(0) were calculated completely in the ref 44. Here since the issue is studied on the low energy (5-30 eV), the amounts of S(0) for each reaction is a constant that are shown in table 4.

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Table 4: the amounts of astrophysical S-factor for different reactions in ordinary state in low energy

Reactions Astrophysical factor	$D(p,\gamma)^3He$	D(d,p)T	D(d,γ) ⁴ He	T(d,n)⁴He
S(0) MeV barn	0.2 × 10 ⁻⁶	0.056	0.054	10

By using the amounts exist in tables 2, 4 and replacing them into Eq.29 the solid state internal

307 conversion coefficient for different reactions can be found. This coefficient indicates the internal

308 conversion rate in different reactions. The result of the calculations summarize in table 5.

Reactions	$\alpha_{SSIC,d} A \Delta R_h$	$\alpha_{SSIC,e,4d} A \Delta R_h$
D(p, y)3He	$u \times 7.8 \times 10^5$	3.1×10^{9}
D(d,p)T	$u \times 3.03 \times 10^{4}$	3.2×10^{6}
D(d,γ) ⁴ He	$u \times 3.398 \times 10^{2}$	5.42×10^{-20}
T(d,n) ⁴ He	$u \times 0.03$	12.7

Table 5: solid state internal conversion coefficient in different reactions for e, 4d and d channels

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311 We find out the solid state internal conversion happens in $D(p,\gamma)$ 3HeandD(d,p)T reactions with

more rates. All calculations in this part are shown for palladium. In the next part we show the results for other elements in detailed.

5. Calculations of LEISSIC forother elements

5.1. Tables of Calculation for Different Elements and Reactions

By using all formulas in section 3, such as what we have done for palladium, all required

quantities can be computed for mentioned elements. Because the other host particles (deuterium

and electron) don't change in these calculations and the only thing that changes is the first row of

the Table.1. Meanwhile, C_1 and C_0 which changes only for the elements are respectively showed

320 in Table 6 and 7.

Table 6: Our numerical calculations of C ₀ for different elements and reactions with FCC, BCC and HCP
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Quantity Elements	$C_{0,D(p,\gamma)3He}$ (MeV barn)	$C_{0,D(d,p)T}$ (MeV barn)	$C_{0,D(d,\gamma)4He}$ (MeV barn)	$C_{0,T(d,n)4He}$ (MeV barn)
Pd (FCC)	4.92×10^{-38}	1.11×10^{-47}	3.83×10^{-50}	2.05×10^{-25}
Ni (FCC)	3.44×10^{-27}	6.79×10^{-33}	2.56×10^{-35}	6.98×10^{-23}
Pt (FCC)	1.34×10^{-57}	1.95×10^{-74}	1.21×10^{-81}	1.63×10^{-45}
Rh (FCC)	1.08×10^{-36}	7.43×10^{-47}	6.61×10^{-51}	1.38×10^{-24}
Ru (HCP)	8.49×10^{-37}	5.07×10^{-46}	5.56×10^{-50}	1.21×10^{-30}
Ti (HCP)	1.10×10^{-23}	4.63×10^{-28}	6.49×10^{-30}	1.93×10^{-21}
Zr (HCP)	2.25×10^{-34}	1.01×10^{-42}	2.69×10^{-46}	6.27×10^{-29}
Ta (BCC)	1.30×10^{-54}	3.10×10^{-70}	5.79×10^{-77}	2.64×10^{-43}

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Quantity	(C _{1,D(p,γ)3He} MeV barn)	$C_{1,D(d,p)T}$ (MeV barn)	$\frac{C_{1,D(d,\gamma)^{4}He}}{(MeV \ barn)}$	$C_{1,T(d,n)4He}$ (MeV barn)
	Pd	3.36×10^{-24}	7.53×10^{-34}	0.26×10^{-35}	1.39×10^{-12}
Pd	d	u × 15.6	u × 12.78	u × 18.35	u × 0.30
(rcc)	e	6.18×10^{2}	1.68×10^{3}	2.93×10^{-21}	127.1
	Ni	3.15×10^{-13}	6.23×10^{-19}	2.35×10^{-21}	6.40×10^{-9}
NI	d	u × 21.1	u × 17.25	u × 24.8	u × 4.08
(FCC)	c	8.35×10^{2}	2.27×10^{3}	3.96×10^{-21}	1.71×10^{2}
	Pt	6.86×10^{-44}	1.30×10^{-60}	8.07×10^{-68}	1.08×10^{-31}
PI	d	u × 15.27	u × 12.48	u × 17.93	$u \times 2.955 \times 10^{-1}$
(FCC)	c	6.04×10^2	1.65×10^{3}	2.86×10^{-21}	1.242×10^{2}
Rh (FCC)	Rh	7.93×10^{-23}	5.41×10^{-33}	4.82×10^{-37}	1.01×10^{-30}
	d	u × 16.76	u × 13.71	u × 19.68	$u \times 3.24 \times 10^{-1}$
	c	5.97×10^{2}	1.63×10^{3}	2.83×10^{-21}	122.75
Du	Ru	5.20×10^{-23}	3.10×10^{-32}	3.40×10^{-36}	7.41×10^{-17}
(HCP)	d	u × 14.08	u × 11.51	u × 16.53	u × 0.27
(ner)	e	4.46×10^{2}	1.21×10^{3}	2.11×10^{-21}	91.60
101	Tì	5.21×10^{-10}	2.19×10^{-14}	3.07×10^{-16}	9.12×10^{-8}
(UCP)	d	u × 10.86	u × 8.88	u × 12.76	u × 0.21
(HCF)	c	172.02	469.22	8.15×10^{-22}	3.53×10^{2}
-	Zr	8.05×10^{-21}	3.61×10^{-29}	9.62×10^{-33}	2.25×10^{-15}
(HCP)	d	u × 8.24	u × 6.73	u × 9.67	u × 16.12
(ner)	c	1.30×10^{2}	3.55×10^{2}	6.18×10^{-22}	26.80
212	Ta	7.17×10^{-41}	1.71×10^{-56}	3.19×10^{-63}	1.46×10^{-29}
(PCC)	d	u × 12.68	u × 10.37	u × 14.89	u × 0.25
(BCC)	c	251×10^{2}	6.84×10^{2}	1.19×10^{-21}	51 59

325 Table 7: Our numerical calculations of C₁ for different elements and reactions with FCC, BCC and HCP lattice

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For comparing C_0 , the micFCS of these metallic environments for all elements, numerical values from Table.6 can be useful. For studying the comparison of the C_1 quantity see table 7.

According to table 7, we find out that: wherever elements themselves are considered as host particles, the results of C₁ from large too small values for all reactions are: Ti, Ni, Zr, Ru, Rh, Pd, Ta and Pt. For cases that deuterium and electron are host particles, our comparing values lead to Ru, Ni, Ti, Rh, Pd, Pt, Zr, Ta and Ni, Ru, Pd, Pt, Rh, Ti, Ta, Zr respectively. In case that electron is host the number of electrons in capacity layer is too important indeed whatever the numbers of electrons increases the screening effect is enhanced. Between all reactions, D(p, γ)3He , D(d,p)T and D(d, γ)4He have larger values of C₁ than T(d,n)4He.

(According Table.7 the result of comparing C₁ for different host particles in different metallic environments are: element host particle, $C_{1,Ti} > C_{1,Ni} > C_{1,Zr} > C_{1,Ru} > C_{1,Rh} > C_{1,Pd} > C_{1,Ta} >$ $C_{1,Pt}$; deuterium host particle, $C_{1,Ru} > C_{1,Ni} > C_{1,Ti} > C_{1,Rh} > C_{1,Pd} > C_{1,Zr} > C_{1,Ta};$ electron host particle, $C_{1,Ni} > C_{1,Pd} > C_{1,Pt} > C_{1,Ta} > C_{$

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Table 8: Our numerical calculations of LEISSIC for all elements in different reactions

Quantit		$\alpha_{D(p,\gamma)3He} \times A\Delta R_h$	$\begin{array}{c} \alpha \\ \ge \\ \Delta D(d,p) \\ \times \\ A \Delta R_h \end{array}$	$\alpha_{D(d,\gamma)4He} \times A\Delta R_h$	$\alpha_{T(d,n)4He} \times A\Delta R_h$
nurce	d	$u \times 7.80 \times 10^{5}$	$u \times 3.03 \times 10^{4}$	$u \times 3.40 \times 10^{2}$	$u \times 0.03$
Pd (FCC)	e	3.1×10^{9}	3.2×10^{6}	5.42×10^{-20}	12.7
NUCCO	d	$u \times 1.05 \times 10^{8}$	$u \times 3.08 \times 10^2$	$u \times 4.59 \times 10^{2}$	$u \times 0.41$
Ni (FCC)	e	4.17×10^{9}	4.07×10^{4}	7.33×10^{-20}	17.15
	d	$u \times 7.63 \times 10^{7}$	$u \times 2.23 \times 10^2$	$u \times 3.32 \times 10^2$	$u \times 0.029$
Pt (FCC)	e	3.02×10^{8}	2.94×10^{4}	5.3×10^{-20}	12.42
Rh	d	$u \times 8.38 \times 10^{7}$	$u \times 2.45 \times 10^{2}$	$u \times 3.65 \times 10^2$	$u \times 0.032$
(FCC)	e	3.00×10^{9}	2.91×10^{4}	0.52	12.27
Ru	d	$u \times 7.04 \times 10^{7}$	$u \times 2.06 \times 10^{2}$	$u \times 3.06 \times 10^2$	$u \times 0.027$
(HCP)	e	2.23×10^{9}	2.17×10^{4}	3.91×10^{-20}	9.17
THORE	d	$u \times 5.43 \times 10^{7}$	$u \times 1.59 \times 10^2$	$u \times 2.36 \times 10^{2}$	$u \times 0.021$
Ti (HCP)	e	8.60×10^{8}	8.38×10^{3}	1.51×10^{-20}	35.37
7.000	d	$u \times 4.12 \times 10^{7}$	$u \times 1.20 \times 10^2$	$u \times 1.79 \times 10^{-2}$	$u \times 1.61$
Zr (HCP)	e	6.52×10^{8}	6.35×10^{3}	1.14×10^{-20}	2.68
T. (DCC)	d	$u \times 6.34 \times 10^{7}$	$u \times 1.85 \times 10^2$	$u \times 2.76 \times 10^{2}$	$u \times 0.025$
Ta (BCC)	e	1.25×10^{9}	1.22×10^{4}	2.20×10^{-20}	5.16

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347 In the each environmentIC coefficient shows internal conversion rate and determined the cross

section enhancement in each environment. By studying table 8, we find out that the internal

349 conversion coefficient of deuterium for $D(p,\gamma)$ 3He is the largest one. IC coefficient for

350 $D(p,\gamma)$ 3He for different reactions from larger to smaller value is: Ru, Ni, Rh, Pt, Zr, Ta, Ti and

Pd. As you see in this reaction Pd has the last rank. In D (d,p)T, the arrangement of the elements

is: Pd, Ru, Ni, Ti, Rh, Pt, Zr and Ta.

353 Electronicinternal conversion coefficientarrangementfor different elements is: Ni, Ru, Pd, Rh, Ti,

354 Ta, Zr, Pt.
$$(\propto_{e,Ni} > \propto_{e,Ru} > \propto_{e,Pd} > \propto_{e,Rh} > \propto_{e,Ti} > \propto_{e,Zr} > \propto_{e,Pt})$$

355 (According to Table.8, comparing ICC values of deuterium host particle for the two largest

reactions D(p, γ)3He and D(d,p)T are respectively: $\propto_{d,Ru} > \propto_{d,Ni} > \propto_{d,Rh} > \propto_{d,Pt} > \propto_{d,Zr} > \propto_{d,Ta} > \infty_{d,Ta} > \infty$

357 $\propto_{d,Ti} > \propto_{d,Pd}$ and $\propto_{d,Pd} > \propto_{d,Ru} > \propto_{d,Ni} > \propto_{d,Ti} > \propto_{d,Rh} > \propto_{d,Pt} > \propto_{d,Zr} > \propto_{d,Ta}$)

6. Microscopic cross section for all elements in different reactions

micFCS for all metallic environment when metal is a host particle are plotted by replacing numerical values in Table 6 and Eq.17. All FCS are divided into two groups in order to show changes clearly: 16 maximum and 16 minimum which are respectively shown in Fig 5 and Fig 6. Numbers 1 to 4 besides the name of the elements shows $D(p,\gamma)$ 3He, D(d,p)T, $D(d,\gamma)$ 4He and T(d,n)4He.







Figure 5:16 maximum of micFCS in terms of incoming energy for all reactions

In the above graph, different colors shows kinds of elements and the styles of shape introduce kinds of reactions. $D(p,\gamma)$ 3He by "dash", D(d,p)T by "dashdot", $D(d,\gamma)$ 4He by "longdash" and T(d,n)4He by "dot" are shown. The color of Pd, Ni, Pt, Rh, Ru, Ti, Zr, and Ta are respectively: Green, red, navy, cyan, dark pink, coral, aquamarine and brown. As you see Ti and Ni have the

lager cross section. After them palladium shows up just in the T(d,n)4He reaction.



- 383 To realize the best kinds of lattice structure, micFCS related to element host particles are plotted
- 384 for each fusion reactions separately.Here in these graphs colors shows kinds of elements and the
- styles of the graph indicate the kind of the lattice. BCC by "dot", FCC by "long dash" and HCP
- 386 by "dashpot".



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Figure 7: micFCS of all elements for $D(p,\gamma)3He$.





Figure 8: micFCS of all elements for D(d,p)T



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Figure 9: micFCS of all elements for $D(d,\gamma)$ 4He



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Figure 10: micFCS of all elements for T(d,n)4He

For $D(p,\gamma)$ 3He, D(d,p)T, $D(d,\gamma)$ 4He (Figs. 7,8,9), Ti with HCP lattice has the largest micFCS and Pd with FCC lattice is respectively in the sixth, second and fifth place. From Fig.10 we can understand that Ni with FCC lattice is in the first place of micFCS and Pd is the fifth. Now the data that are correspond to figures 7, 8, 9 and 10 are summarized in table 9.



-Quantity Element	$\sigma_{element}$ D(p, γ)3Hc (MeV)	σ _{element} D(d,p)T (MeV)	$\sigma_{element}$ D(d, γ)4He (MeV)	σ _{element} T(d,n)4He (MeV)
Pd (FCC)	1.19×10^{-38}	8.35×10^{-49}	2.89×10^{-51}	8.51×10^{-28}
Ni (FCC)	8.19×10^{-28}	5.12×10^{-34}	1.93×10^{-36}	2.89×10^{-24}
Pt (FCC)	2.46×10^{-58}	1.48×10^{-75}	9.18×10^{-83}	6.78×10^{-47}
Rh (FCC)	2.59×10^{-37}	5.61×10^{-48}	5.02×10^{-52}	5.77×10^{-46}
Ru (HCP)	2.02×10^{-37}	3.81×10^{-47}	4.21×10^{-51}	5.02×10^{-32}
Ti (HCP)	2.62×10^{-24}	3.50×10^{-29}	4.93×10^{-31}	7.97×10^{-23}
Zr (HCP)	5.37×10^{-37}	7.59×10^{-44}	2.03×10^{-47}	2.61×10^{-30}
Ta (BCC)	3.10×10^{-55}	2.34×10^{-71}	4.36×10^{-78}	1.10×10^{-44}

7. Conclusion

As you see, Titanium and Nickel are chosen for using them in the next options in experimental works. By studying the internal conversion coefficient, we find out that Ni and Ru might beta good options. By collecting these results together we understand that the Nickel can be the4best option. We can neglect Ta and the BCC lattice because of its worse results. 415

The other investigations show that: FCC and HCP lattice have a much closed results. Pallattiem shows good results just in the $D(p,\gamma)$ 3He and $D(d,\gamma)$ 4He. After Ni, the next option could be **T** i.

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